

## Turing's machine model

Machine models of a computer always have

- means to store data
  - e.g. objects in Java, files and variables in UNIX
- means to manipulate data
  - e.g. methods in Java, processes in UNIX
- ways to program data manipulation
  - e.g. JAVA programs, UNIX shell scripts

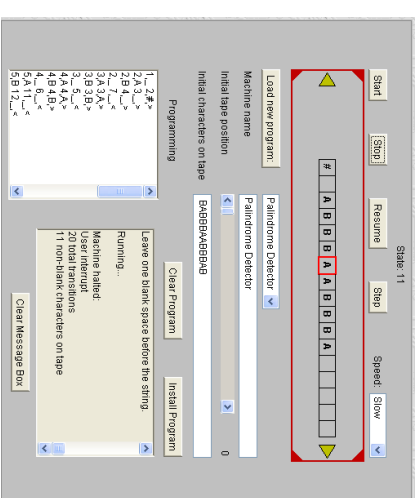
## The Turing Machine model (1936)

- store is represented by an unbounded tape
- processor is represented by a read/write head
- program is represented by a set of rules

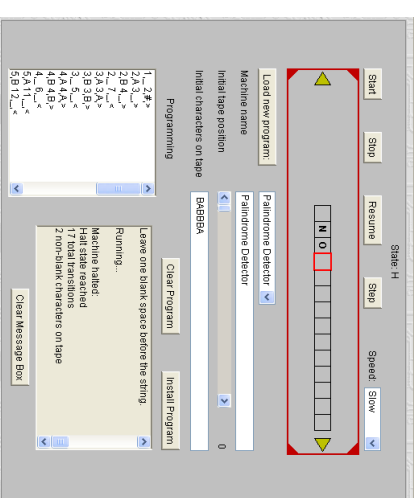
Suzanne Skinner (1996) Java applet simulator at:

<http://ironphoenix.org/tril/tm/>

A Turing computation in progress ... recognising a palindromic string



A Turing computation in the halt state ... rejecting a non-palindromic string



## The Church-Turing thesis

There is no computational model that is in principle more powerful than the Turing machine ...

... all algorithmic data processing is equivalent to Turing computation

... by this criterion, very simple notations can define “a full programming language”

## Functional programming (FP)

A “functional” program to compute prime numbers:

```
factors n = [r | r<-[1..n div 2]; n mod r = 0]
isprime q = (# factors q) = 1
```

functional  $\equiv$  based on specifying functions

The functions in this context are

*factors()* and *isprime()*

The programming language is **Miranda**

## Procedural version of isprime

```
func factors {
  para n;
  auto r,result;
  result = [];
  for (r=1; r<=n/2; r++)
    if (n % r == 0) result = result // [r];
  return result;
}

func isprime {
  para n;
  return ((factors[n])# == 1);
}
```

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