#### Flavour Physics in the LHC Era Lecture 2 of 3

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#### Contents

- Part 1
  - Why is flavour physics interesting?
- Part 2
  - What do we know from previous experiments?
- Part 3
  - What do we hope to learn from current and future heavy flavour experiments?

Today hope to cover Part 2 & start Part 3



# What do we know about heavy quark flavour physics as of today?



#### CKM Matrix: parametrizations

- Many different possible choices of 4 parameters
- PDG: 3 mixing angles and 1 phase

PRL 53 (1984) 1802

$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix}$$

- Apparent hierarchy:  $s_{12} \sim 0.2$ ,  $s_{23} \sim 0.04$ ,  $s_{13} \sim 0.004$ 
  - Wolfenstein parametrization (expansion parameter  $\lambda \sim \sin \theta_c \sim 0.22$ )

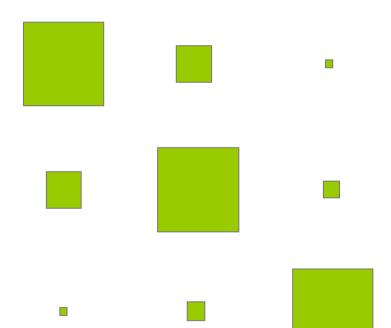
$$V = \left( \begin{array}{ccc} 1 - \frac{1}{2}\lambda^2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{array} \right) + \mathcal{O}\left(\lambda^4\right)$$

Other choices, eg. based on CP violating phases



## Hierarchy in quark mixing

$$V = \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}\left(\lambda^4\right)$$



Very suggestive pattern

No known underlying reason

Situation for leptons (vs) is
completely different



## CKM matrix to $O(\lambda^5)$

$$V_{\text{CKM}} = \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 - \frac{1}{8}\lambda^4 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda + \frac{1}{2}A^2\lambda^5[1 - 2(\rho + i\eta)] & 1 - \frac{1}{2}\lambda^2 - \frac{1}{8}\lambda^4(1 + 4A^2) & A\lambda^2 \\ A\lambda^3[1 - (1 - \frac{1}{2}\lambda^2)(\rho + i\eta)] & -A\lambda^2 + \frac{1}{2}A\lambda^4[1 - 2(\rho + i\eta)] & 1 - \frac{1}{2}A^2\lambda^4 \end{pmatrix}$$
 imaginary part at  $O(\lambda^3)$  imaginary part at  $O(\lambda^5)$ 

Remember – only *relative* phases are observable



#### **Unitarity Tests**

The CKM matrix must be unitary

$$V_{CKM}^+ V_{CKM} = V_{CKM} V_{CKM}^+ = 1$$

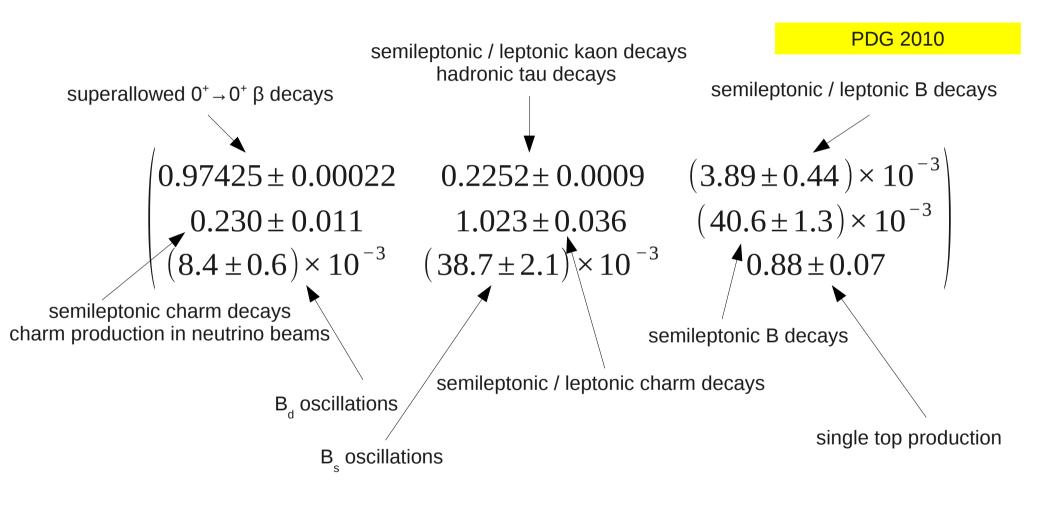
 Provides numerous tests of constraints between independent observables, such as

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1$$

$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$



## CKM Matrix – Magnitudes

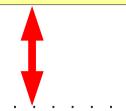


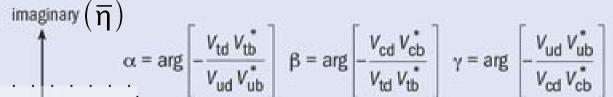
theory inputs (eg., lattice calculations) required



## The Unitarity Triangle

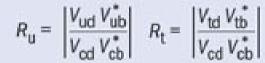
$$V_{ud} V_{ub}^* + V_{cd} V_{cb}^* + V_{td} V_{tb}^* = 0$$





Three complex numbers add to zero

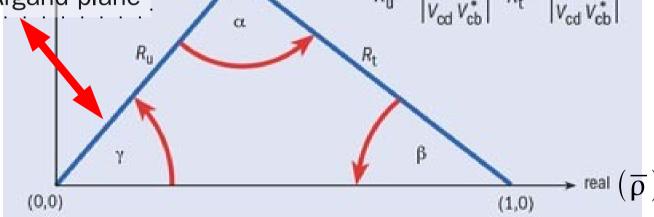
⇒ triangle in Argand plane



Axes are  $\overline{\rho}$  and  $\overline{\eta}$  where

$$\overline{\rho} + i \overline{\eta} \equiv -\frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*}$$

$$\rho + i\eta = \frac{\sqrt{1 - A^2 \lambda^4} (\overline{\rho} + i\overline{\eta})}{\sqrt{1 - \lambda^2} [1 - A^2 \lambda^4 (\overline{\rho} + i\overline{\eta})]}$$





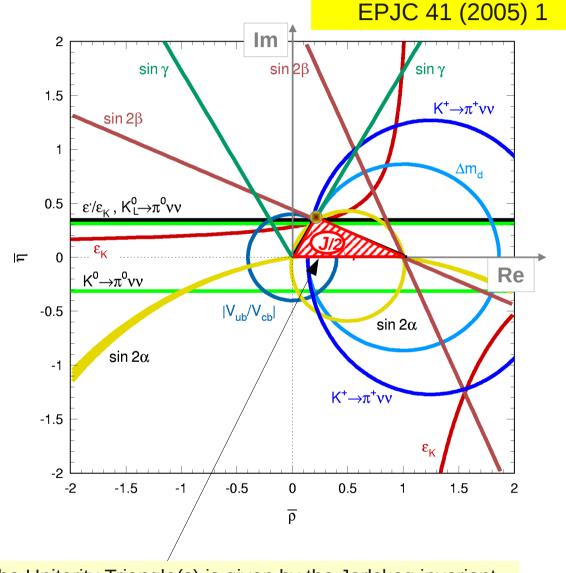
#### Predictive nature of KM mechanism

In the Standard Model the KM phase is the sole origin of CP violation

#### Hence:

all measurements must agree on the position of the apex of the Unitarity Triangle

(Illustration shown assumes no experimental or theoretical uncertainties)

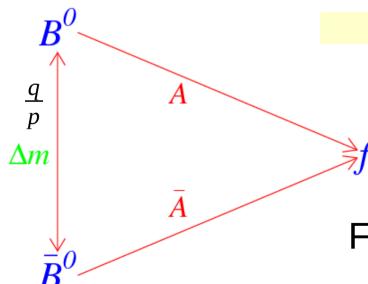




# Time-Dependent CP Violation in the $B^0-\overline{B}^0$ System

• For a B meson known to be 1)  $B^0$  or 2)  $\overline{B}^0$  at time t=0, then at later time t:

$$\Gamma\left(B_{phys}^{0} \to f_{CP}(t)\right) \propto e^{-\Gamma t} \left[1 - \left(S\sin\left(\Delta m t\right) - C\cos\left(\Delta m t\right)\right)\right]$$
  
$$\Gamma\left(\overline{B}_{phys}^{0} \to f_{CP}(t)\right) \propto e^{-\Gamma t} \left[1 + \left(S\sin\left(\Delta m t\right) - C\cos\left(\Delta m t\right)\right)\right]$$



here assume  $\Delta\Gamma$  negligible – will see full expressions later

$$S = \frac{2\Im(\lambda_{CP})}{1 + \left|\lambda_{CP}^{2}\right|} \qquad C = \frac{1 - \left|\lambda_{CP}^{2}\right|}{1 + \left|\lambda_{CP}^{2}\right|} \qquad \lambda_{CP} = \frac{q\overline{A}}{pA}$$

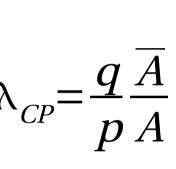
For  $B^0 \rightarrow J/\psi K_s$ ,  $S = \sin(2\beta)$ , C=0

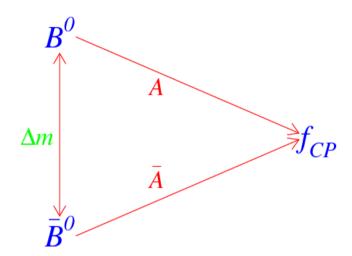
NPB 193 (1981) 85



### Categories of CP violation

 Consider decay of neutral particle to a CP eigenstate





$$|\frac{q}{p}| \neq 1$$

$$|\frac{\overline{A}}{A}| \neq 1$$

**CP violation in mixing** 

**CP violation in decay (direct CPV)** 

**CP** violation in interference between mixing and decay



## Asymmetric B factory principle

To measure t require B meson to be moving

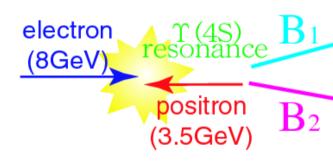
→ e<sup>+</sup>e<sup>-</sup> at threshold with asymmetric collisions (Oddone)

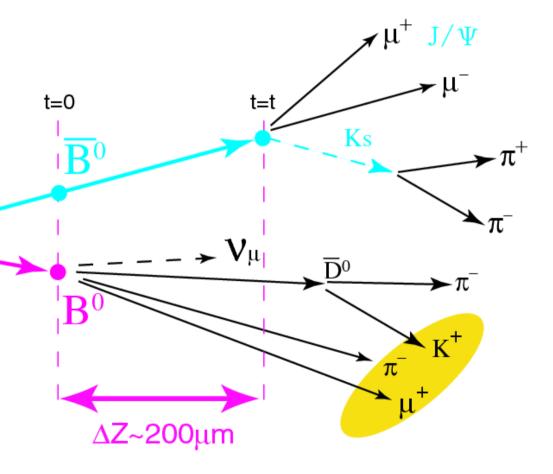
Other possibilities considered

→ fixed target production?

→ hadron collider?

→ e<sup>+</sup>e<sup>-</sup> at high energy?





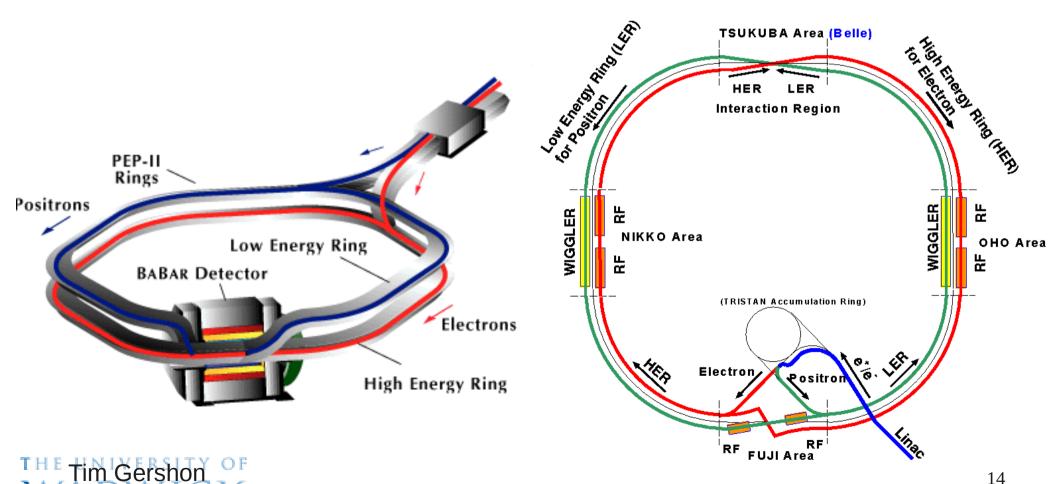


#### Asymmetric B Factories

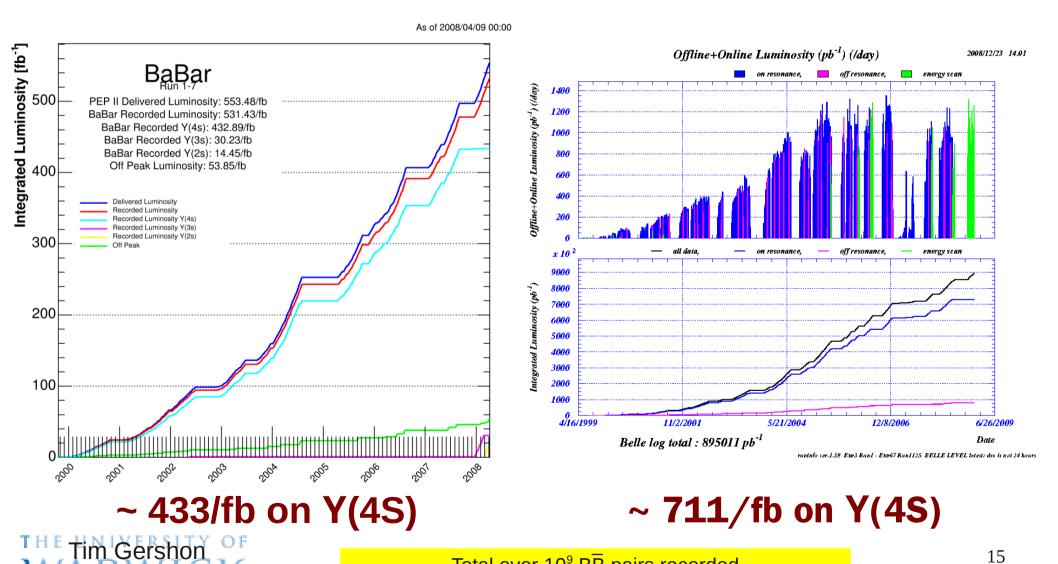
PEPII at SLAC

Flavour Physics

KEKB at KEK 9.0 GeV  $e^{-}$  on 3.1 GeV  $e^{+}$  8.0 GeV  $e^{-}$  on 3.5 GeV  $e^{+}$ 

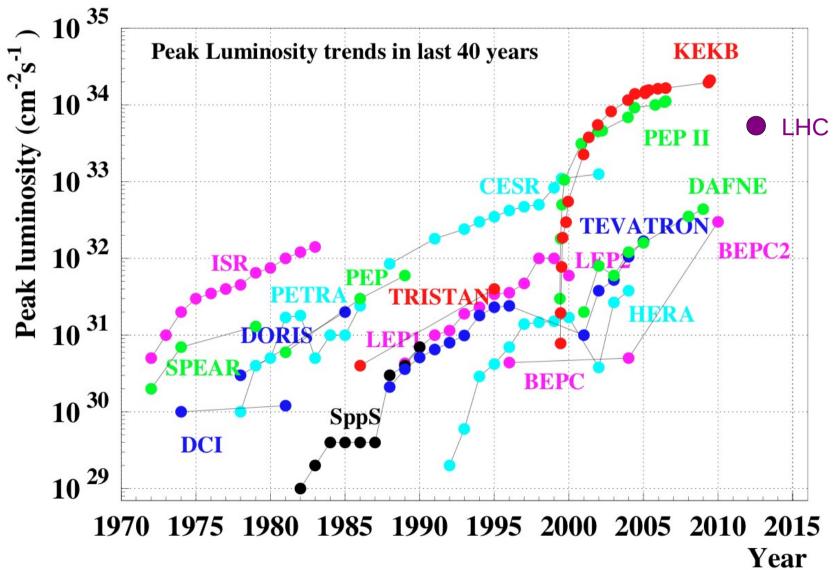


#### B factories – world record luminosities



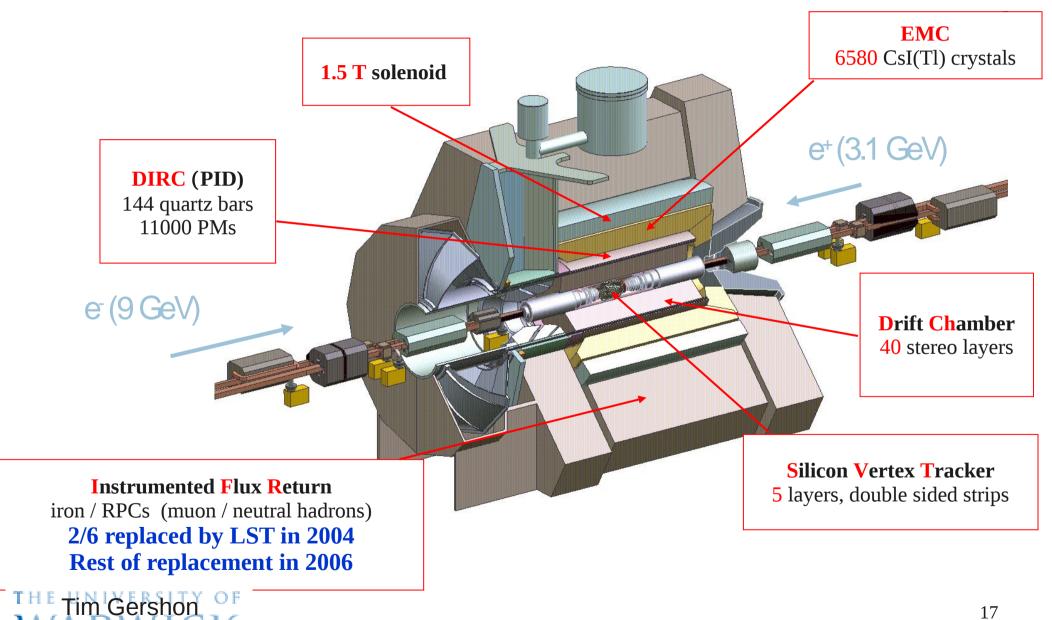
Flavour Physics

#### World record luminosities (2)



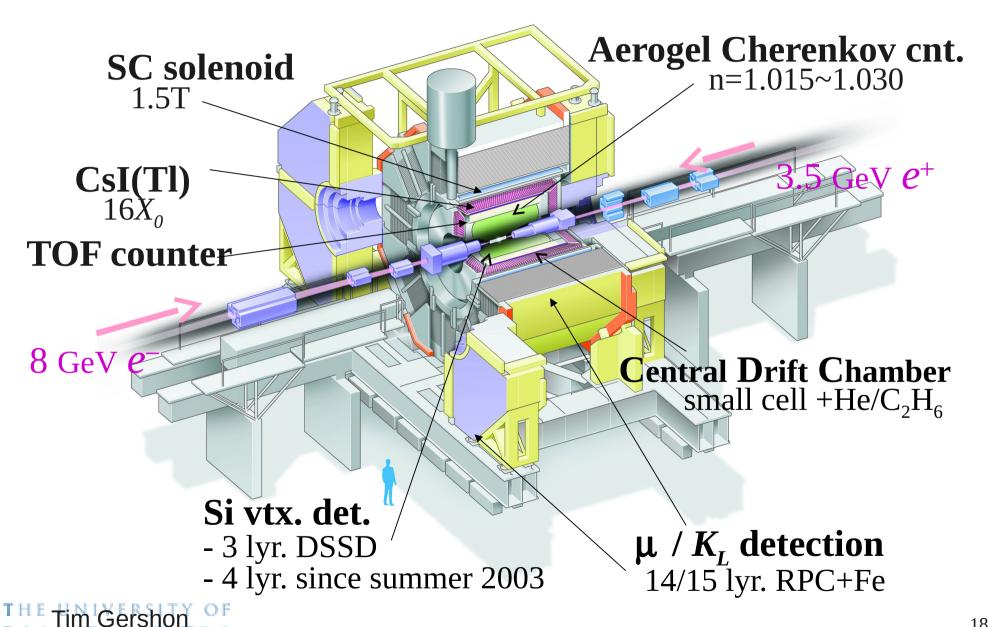


#### BaBar Detector



Flavour Physics

#### Belle Detector



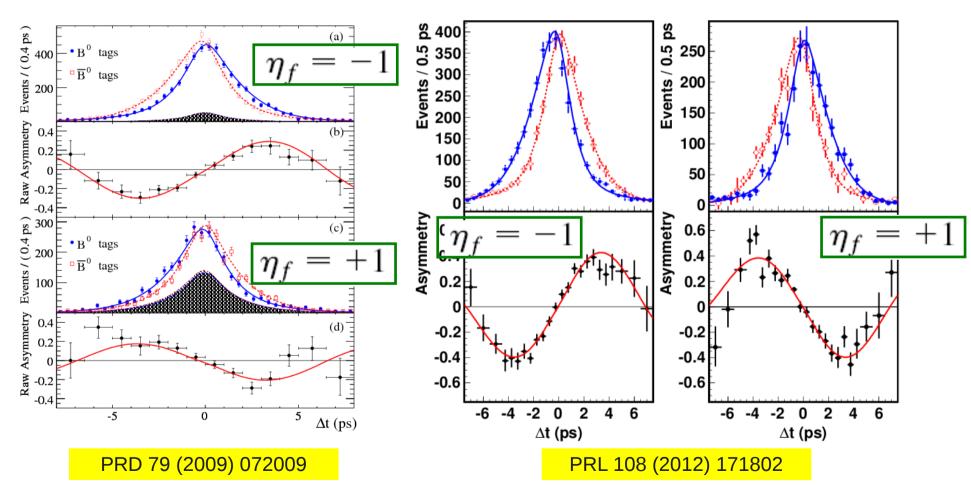
Flavour Physics

## Results for the golden mode

 $B^0 \to J/\psi K^0$ 

**BABAR** 

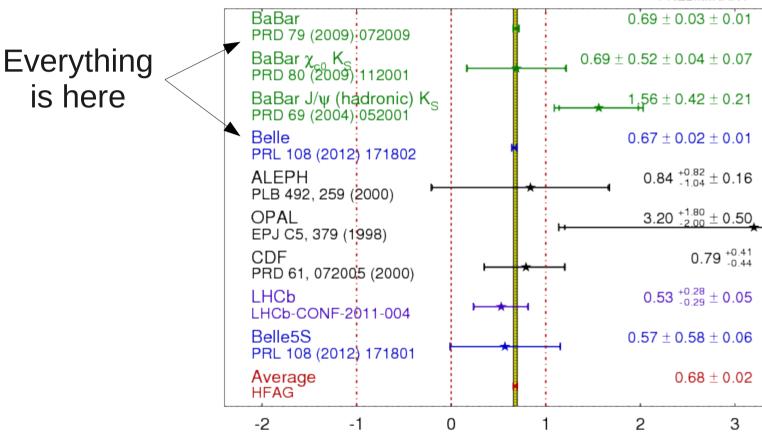
**BELLE** 





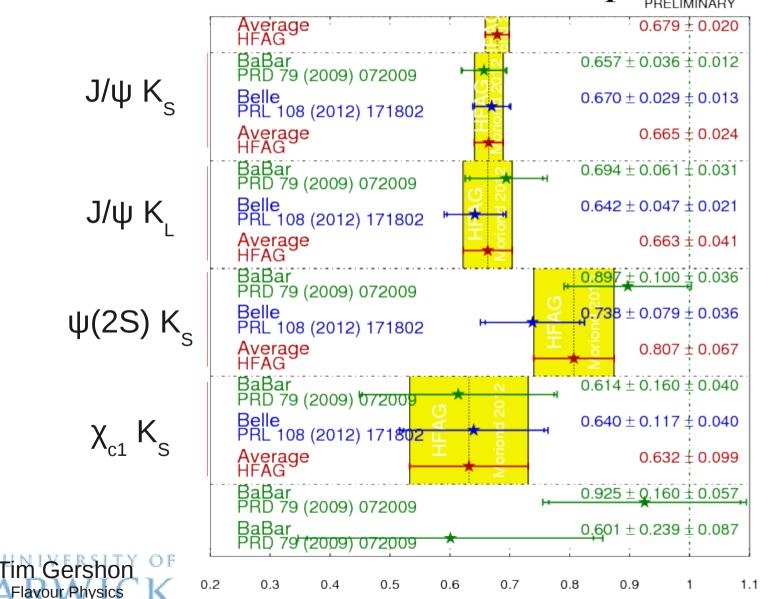
### Compilation of results







# Compilation of results $\sin(2\beta) \equiv \sin(2\phi_1)$ HFAG Moriond 2012



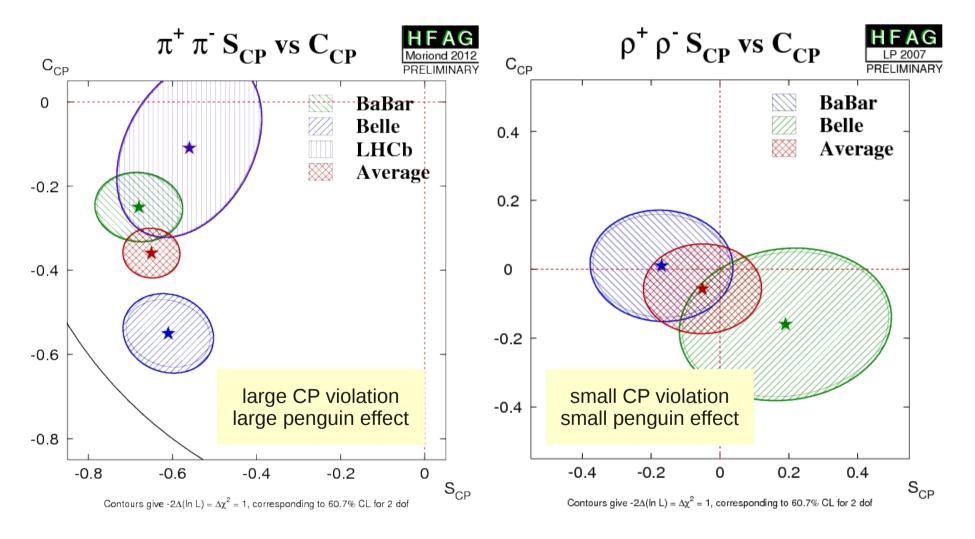
#### Measurement of a

- Similar analysis using b  $\rightarrow$  u $\overline{u}$ d decays (e.g.  $B_d^0 \rightarrow \pi^+\pi^-$ ) probes  $\pi$ –( $\beta$ + $\gamma$ ) =  $\alpha$ 
  - but b → duū penguin transitions contribute to same final states ⇒ "penguin pollution"
  - C ≠ 0 ⇔ direct CP violation can occur
  - S ≠ + $\eta_{CP}$  sin(2α)
- Two approaches (optimal approach combines both)
  - try to use modes with small penguin contribution
  - correct for penguin effect (isospin analysis)

PRL 65 (1990) 3381

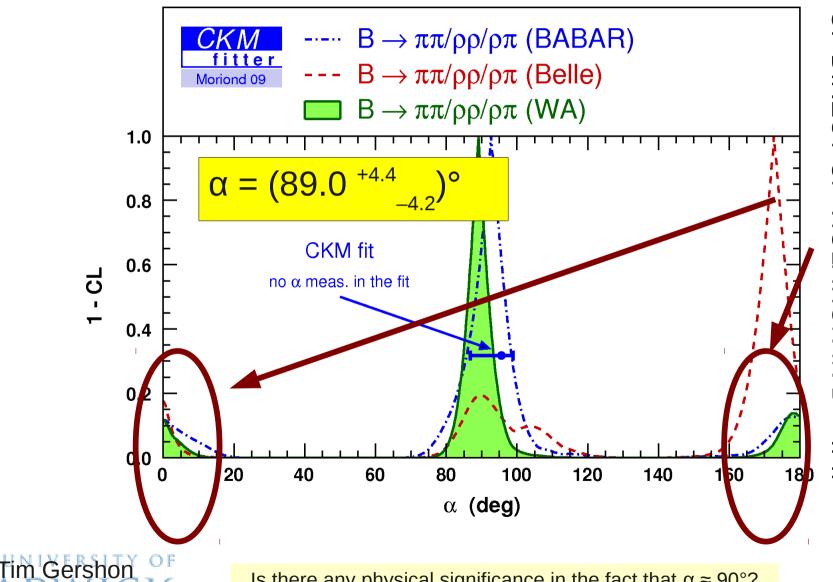


#### **Experimental Situation**





#### Measurement of a



Is there any physical significance in the fact that  $\alpha \approx 90^{\circ}$ ?

Flavour Physics

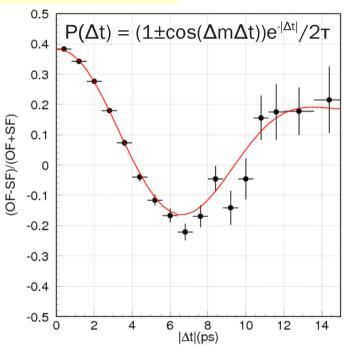
OF DIRECT CP VIOLATION IN B°. RULED BY **OBSERVATION** 

## R<sub>side</sub> from B<sup>0</sup>–B<sup>0</sup> mixing

$$R_t = \left| \frac{V_{td} V_{tb}^*}{V_{cd} V_{cb}^*} \right|$$

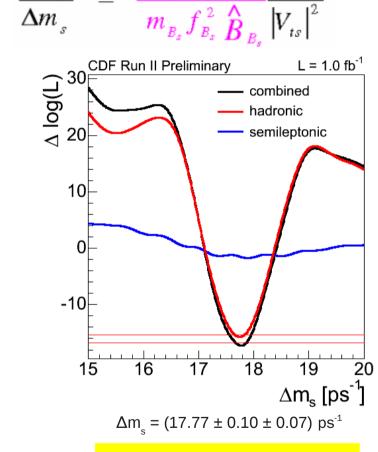
$$R_{t} = \left| \frac{V_{td} V_{tb}^{*}}{V_{cd} V_{cb}^{*}} \right| & & \frac{\Delta m_{d}}{\Delta m_{s}} = \frac{m_{B_{d}} f_{B_{d}}^{2} \stackrel{\wedge}{B}_{B_{d}} |V_{td}|^{2}}{m_{B_{s}} f_{B_{s}}^{2} \stackrel{\wedge}{B}_{B_{c}} |V_{ts}|^{2}}$$

World average based on many measurements



 $\Delta m_a = (0.511 \pm 0.005 \pm 0.006) \text{ ps}^{-1}$ 

PRD 71, 072003 (2005)



PRL 97, 242003 (2006)



$$\left|V_{td}/V_{ts}\right| = 0.211 \pm 0.001 \pm 0.005$$

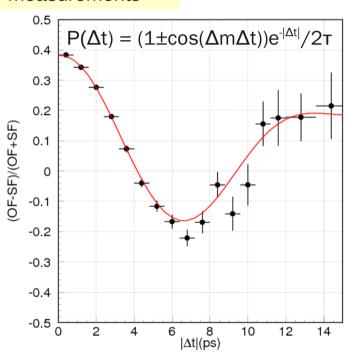
experimental theoretical uncertainty uncertainty

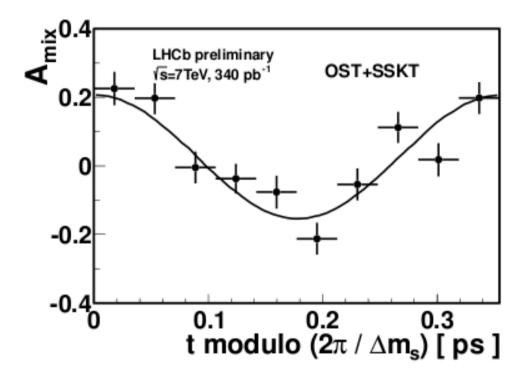
# R<sub>1</sub> side from B<sup>0</sup>–B<sup>0</sup> mixing

$$R_t = \left| \frac{V_{td} V_{tb}^*}{V_{cd} V_{cb}^*} \right|$$

$$R_{t} = \frac{\left| \frac{V_{td} V_{tb}^{*}}{V_{cd} V_{cb}^{*}} \right| & \frac{\Delta m_{d}}{\Delta m_{s}} = \frac{m_{B_{d}} f_{B_{d}}^{2} \stackrel{\wedge}{B}_{B_{d}} \left| V_{td} \right|^{2}}{m_{B_{s}} f_{B_{s}}^{2} \stackrel{\wedge}{B}_{B_{d}} \left| V_{ts} \right|^{2}}$$

World average based on many measurements





 $\Delta m_{\perp} = (0.511 \pm 0.005 \pm 0.006) \text{ ps}^{-1}$ 

PRD 71, 072003 (2005)

 $\Delta m_a = (17.725 \pm 0.041 \pm 0.026) \text{ ps}^{-1}$ 

LHCb-CONF-2011-050



$$\left|V_{td}/V_{ts}\right| = 0.211 \pm 0.001 \pm 0.005$$

experimental theoretical uncertainty uncertainty

## R side from semileptonic decays

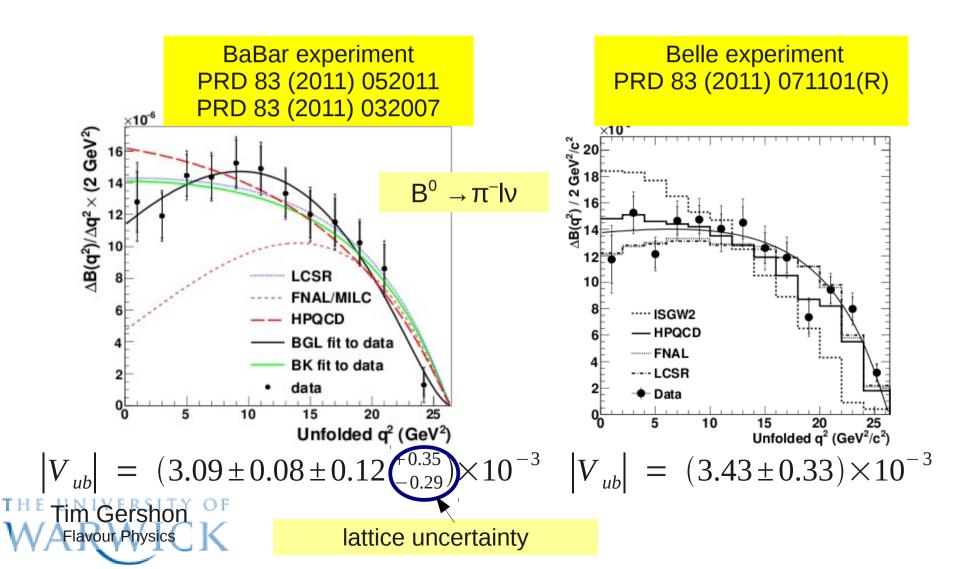
$$R_{u} = \left| \frac{V_{ud} V_{ub}^{*}}{V_{cd} V_{cb}^{*}} \right|$$
Parton level
$$b = \overline{V}_{ub}, \overline{V}_{cb}$$
Hadron level
$$\overline{V}_{ub}, \overline{V}_{cb}$$
Parton level

- Approaches:
  - exclusive semileptonic B decays, eg.  $B^0 \rightarrow \pi^- e^+ \nu$ 
    - require knowledge of form factors
      - can be calculated in lattice QCD at kinematical limit
  - inclusive semileptonic B decays, eg. B → X e<sup>+</sup> ν
    - clean theory, based on Operator Product Expansion
    - experimentally challenging:
      - need to reject b → c background
        - cuts re-introduce theoretical uncertainties



## |V<sub>III</sub>| from exclusive semileptonic decays

Current best measurements use  $B^0 \rightarrow \pi^- I^+ \nu$ 



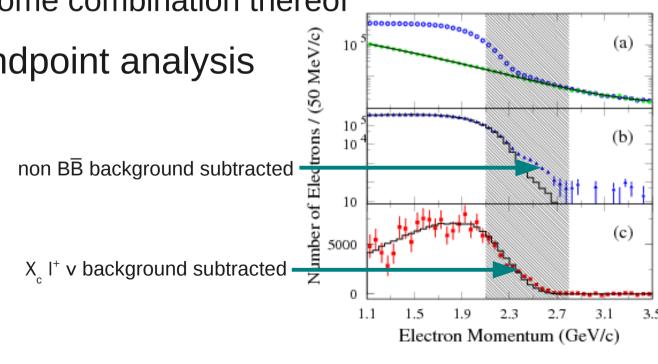
# |V<sub>ub</sub>| from inclusive semileptonic decays

- Main difficulty to measure inclusive B → X<sub>...</sub> I<sup>+</sup> ν
  - background from B  $\rightarrow X_{c} I^{+} v$
- Approaches

- cut on  $E_1$  (lepton endpoint),  $q^2$  (lv invariant mass squared),

 $M(X_{\perp})$ , or some combination thereof

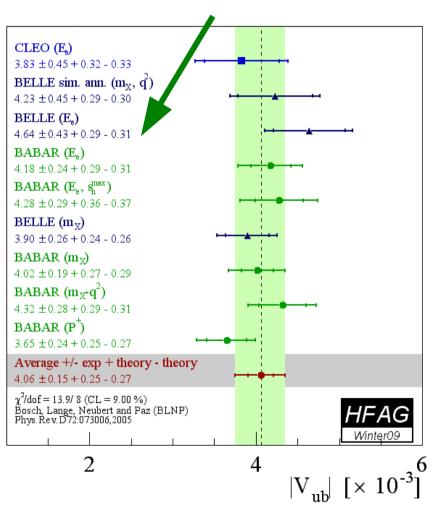
• Example: endpoint analysis

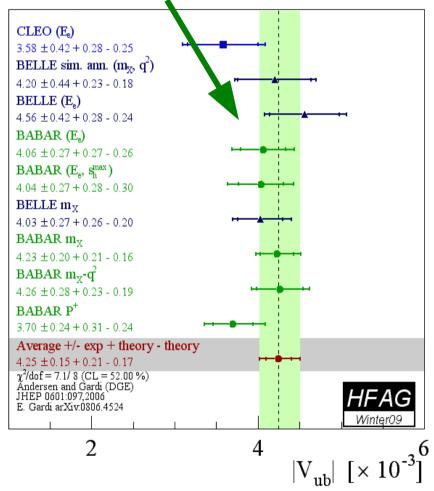




# |V<sub>ub</sub>| inclusive - compilation

Different theoretical approaches (2 of 4 used by HFAG)







## |V<sub>ub</sub>| average

• Averages on  $|V_{ub}|$  from both exclusive and inclusive approaches

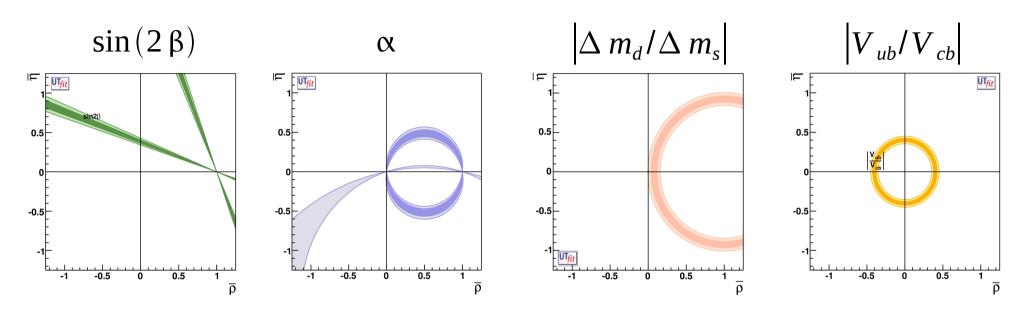
- exclusive: 
$$|V_{ub}| = (3.23 \pm 0.31) \times 10^{-3}$$

- inclusive: 
$$|V_{ub}| = (4.41 \pm 0.22) \times 10^{-3}$$

- slight tension between these results
- in both cases theoretical errors are dominant
  - but some "theory" errors can be improved with more data
- PDG2012 does naïve average rescaling due to inconsistency to obtain  $|V_{ub}| = (4.15 \pm 0.49) \times 10^{-3}$

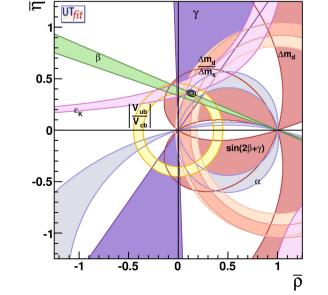


#### Partial summary



Adding a few other constraints we find

$$\bar{\rho} = 0.132 \pm 0.020$$
 $\bar{\eta} = 0.358 \pm 0.012$ 



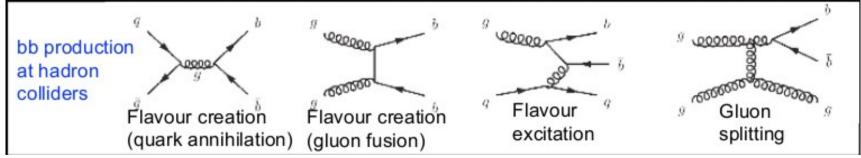
Consistent with Standard Model fit

• some "tensions"

Still plenty of room for new physics

## Flavour physics at hadron colliders

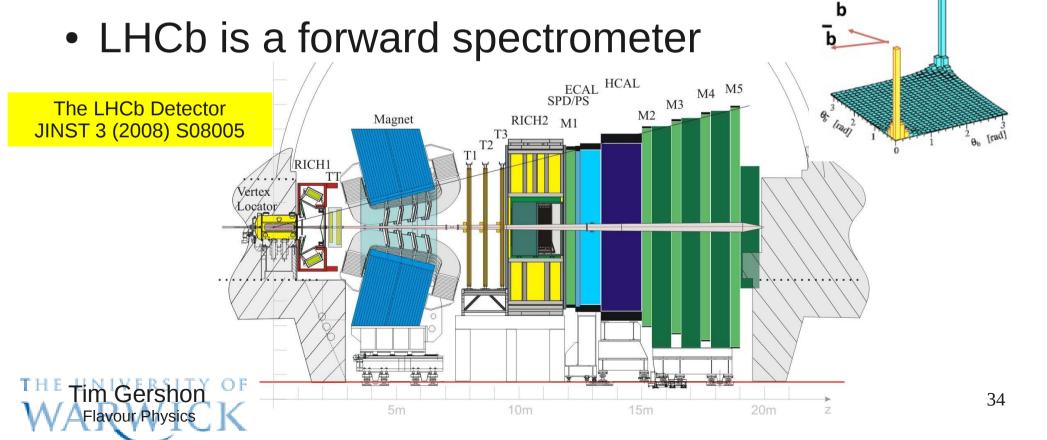
	$e^+e^- \rightarrow \Upsilon(4s) \rightarrow B\overline{B}$ PEP-II, KEK-B	$p\overline{p} \rightarrow b\overline{b}X  (\sqrt{s} = 2 \text{ TeV})$ <b>TeVatron</b>	$pp \rightarrow b\bar{b}X  (\sqrt{s} = 14 \text{ TeV})$
prod	1 nb	~100 µb	~500 μb
typ. $b\bar{b}$ rate	10 Hz	~100 kHz	~500 kHz
purity	~1/4	$\sigma_{b\bar{b}}/\sigma_{inel} \approx 0.2\%$	$\sigma_{b\bar{b}}/\sigma_{inel} \approx 0.6\%$
pile-up	0	1.7	0.5-20
B content	$B^{+}B^{-}(50\%), B^{0}\overline{B}^{0}(50\%)$	$B^+(40\%), B^0(40\%), B_s(10\%), B_c(<1\%), b - baryons(10\%)$	
B boost	small, βγ~0.56	large, decay vertices are displaced	
event structure	BB pair alone	many particles non-associated to $bar{b}$	
prod. vertex	Not reconstructed	reconstructed with many tracks	
$B^0\overline{B}^0$ mixing	coherent	incoherent→ flavour tagging dilution	





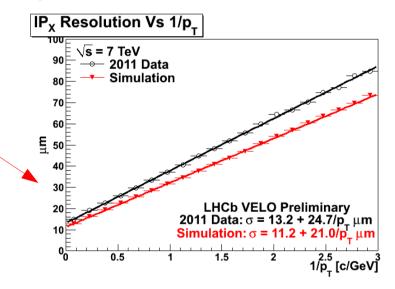
#### Geometry

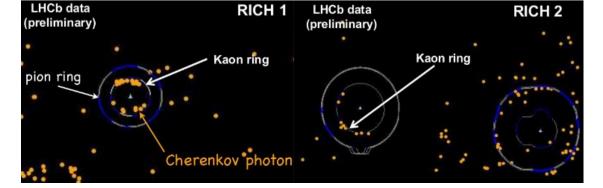
 In high energy collisions, bb pairs produced predominantly in forward or backward directions



#### LHCb detector features

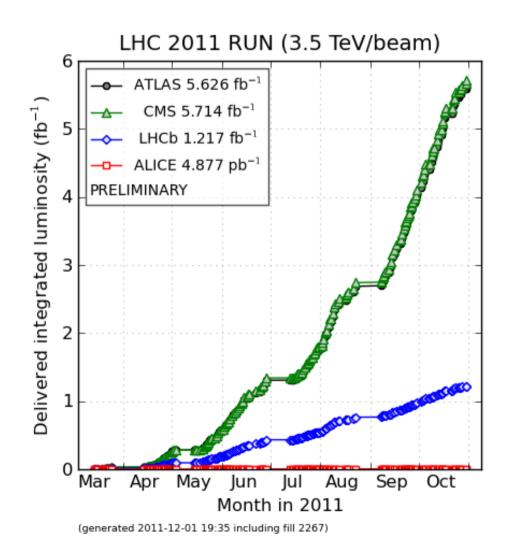
- Tracking and calorimetry
  - basic essentials of any collider experiment!
  - muon chambers
- VELO
  - reconstruct displaced vertices
- RICH
  - particle ID (K/ $\pi$  separation)
- Trigger
  - fast and efficient

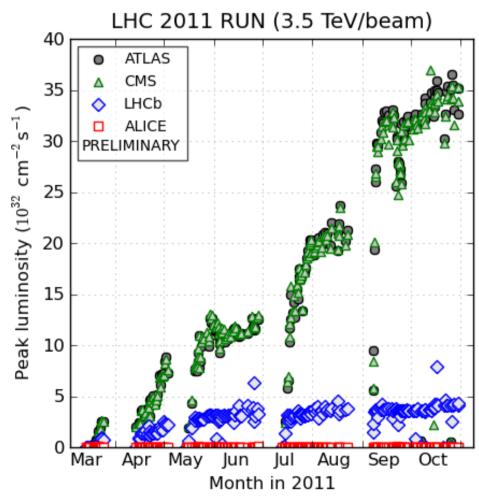






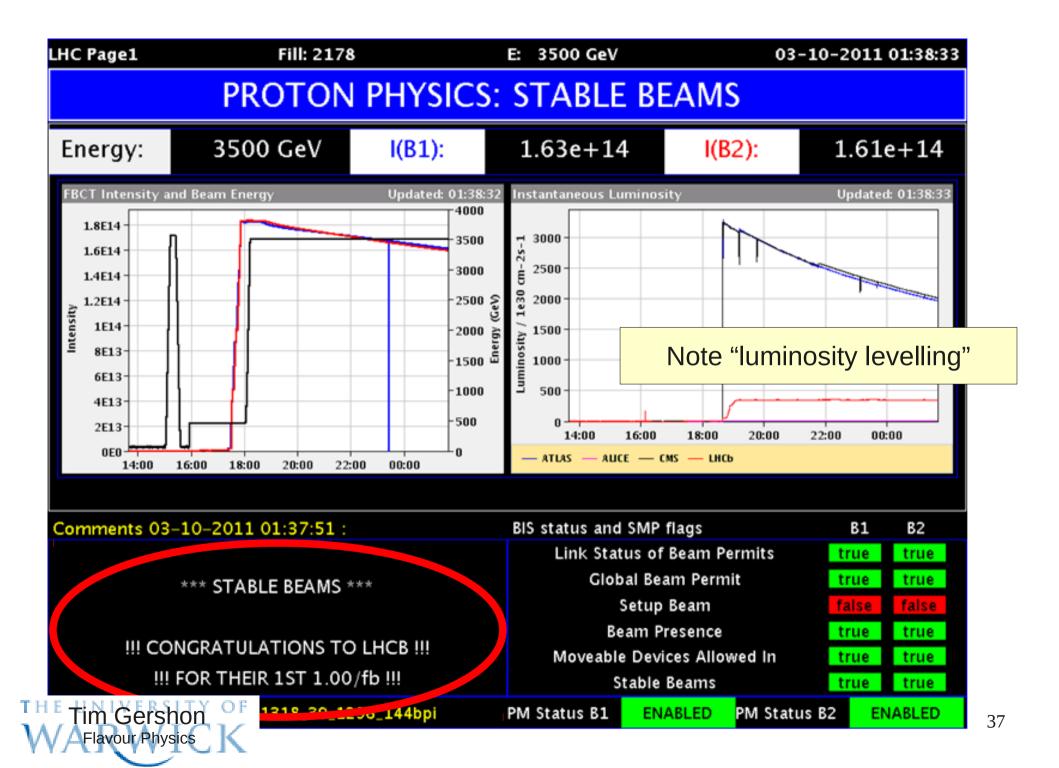
#### LHC performance 2011



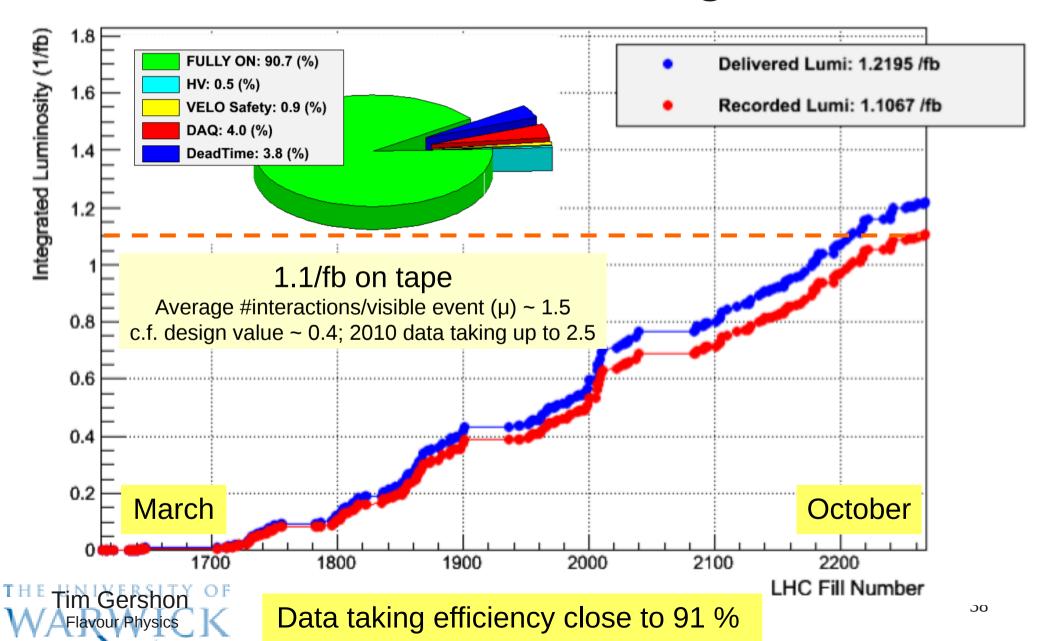


(generated 2011-12-01 19:35 including fill 2267)



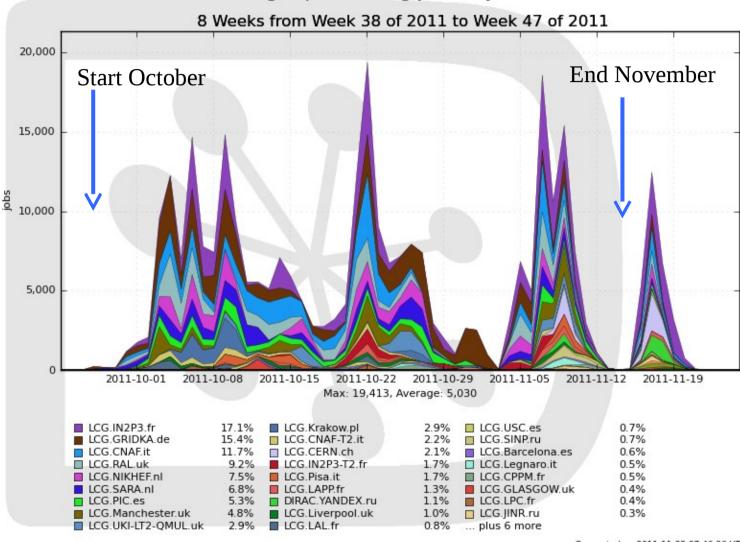


## 2011 data taking



## 2011 data reprocessing

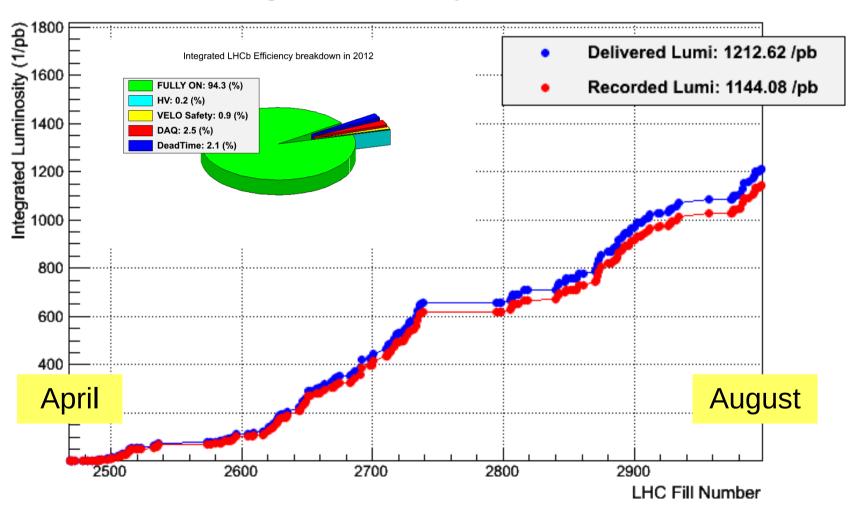
Running reprocessing jobs, by site





## 2012 data taking

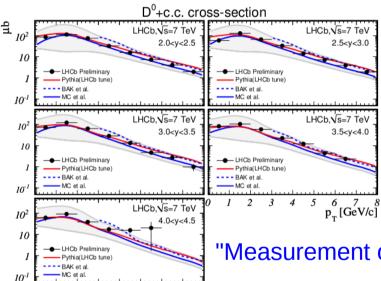
#### LHCb Integrated Luminosity at 4 TeV in 2012





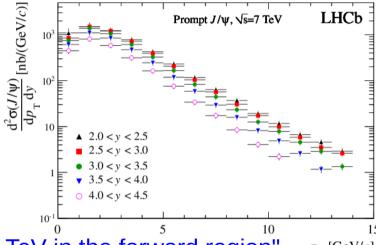
## Heavy flavour production @ LHCb

"Prompt charm production in pp collisions at √s = 7 TeV" LHCb-CONF-2010-013

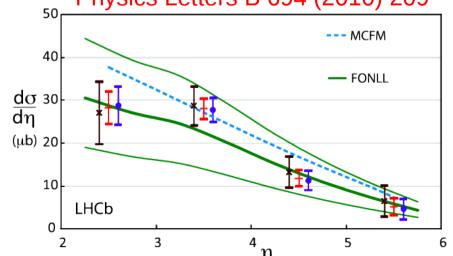


p<sub>T</sub> [GeV/c]

"Measurement of J/ψ production in pp collisions at  $\sqrt{s} = 7$  TeV" Eur. Phys. J. C 71 (2011) 1645



"Measurement of  $\sigma(pp \to bbX)$  at  $\sqrt{s} = 7$  TeV in the forward region"  $p_T[GeV/c]$  Physics Letters B 694 (2010) 209





2 3

#### What does $\int L dt = 1/fb$ mean?

Measured cross-section, in LHCb acceptance

$$\sigma(pp \rightarrow b\overline{b}X) = (75.3 \pm 5.4 \pm 13.0) \,\mu b$$

PLB 694 (2010) 209

• So, number of bb pairs produced

$$10^{15} \times 75.3 \ 10^{-6} \sim 10^{11}$$

Compare to combined data sample of e<sup>+</sup>e<sup>-</sup> "B factories" BaBar and Belle of ~ 10<sup>9</sup> BB pairs

for any channel where the (trigger, reconstruction, stripping, offline) efficiency is not too small, LHCb has world's largest data sample

• p.s.: for charm,  $\sigma(pp \rightarrow c\overline{c}X) = (6.10 \pm 0.93)$  mb

LHCb-CONF-2010-013



## The all important trigger

#### Challenge is

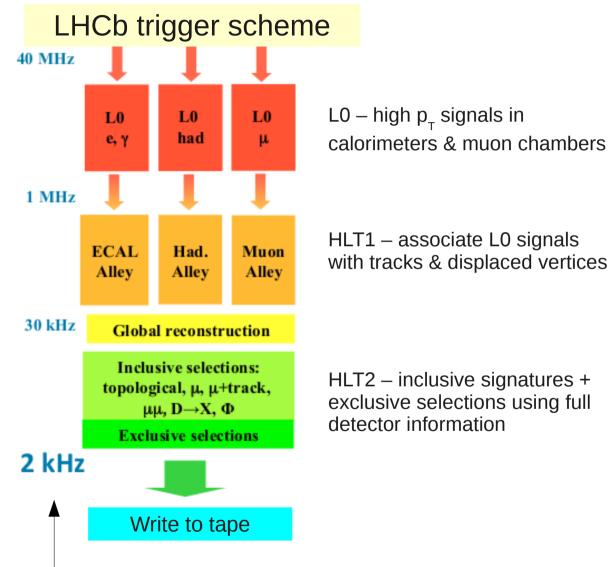
- to efficiently select most interesting B decays
- while maintaining manageable data rates

#### Main backgrounds

- "minimum bias" inelastic pp scattering
- other charm and beauty decays

#### Handles

- high p<sub>T</sub> signals (muons)
- displaced vertices





## Spectroscopy

- I've talked about the headline items of flavour physics
  - CP violation, searches for new physics
  - what we tell the funding agencies, and the press
- But, much of the physics performed by flavour experiments is the study of properties of hadronic states
  - lifetimes, masses, decay channels, quantum numbers
  - and the discoveries of new ones

```
    Observation of a narrow meson decaying to D+(s) pi0 at a mass of 2.32-GeV/c**2.

                                                                                                            Observation of a narrow charmonium - like state in exclusive B+- ---> K+- pi+ pi- J/ psi decays.
By BABAR Collaboration (Bernard Aubert et al.). SLAC-PUB-9711, BABAR-PUB-03-011, Apr 2003, 7pp.
                                                                                                            By Belle Collaboration (S.K. Choi et al.), Sep 2003, 10pp.
Press Release from SLAC
                                                                                                            Press release
Published in Phys.Rev.Lett.90:242001.2003.
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e-Print: hep-ex/0304021
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TOPCITE = 500+
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       References | LaTeX(US) | LaTeX(EU) | Harvmac | BibTeX | Keywords | Cited 521 times
                                                                                                                   References | LaTeX(US) | LaTeX(EU) | Harvmac | BibTeX | Keywords | Cited 514 times
       Abstract and Postscript and PDF from arXiv.org (mirrors: au br cn de es fr il in it jp kr ru tw uk za aps lanl)
                                                                                                                   Abstract and Postscript and PDF from arXiv.org (mirrors: au br cn de es fr il in it jp kr ru tw uk za aps lan!)
       Journal Server [doi:10.1103/PhysRevLett.90.242001]
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Most highly cited papers from BaBar and Belle

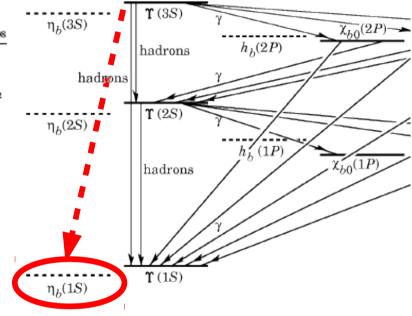
## Discovery of the lightest bb state - 2008

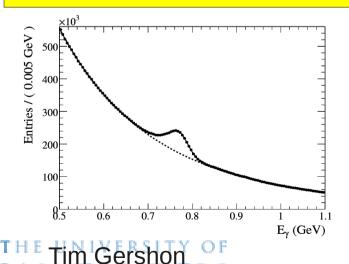
Selected for a Viewpoint in Physics
PHYSICAL REVIEW LETTERS week ending PRL 101, 071801 (2008) Observation of the Bottomonium Ground State in the Decay  $Y(3S) \rightarrow \gamma \eta_h$ 

B. Aubert, M. Bona, Y. I. The BaBar Collaboration | Fisserand, J. Garra Tico, Abrams, M. Battaglia, 5

Only recoil y is reconstructed

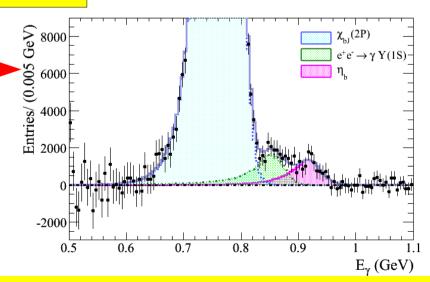
$$m(\eta_b(1S)) = (9388.9^{+3.1}_{-2.3} \pm 2.7) \text{MeV}/c^2$$
  
 $m(\Upsilon(1S)) - m(\eta_b(1S)) = (71.4^{+2.3}_{-3.1} \pm 2.7) \text{MeV}/c^2$   
 $B(\Upsilon(3S) \rightarrow \gamma \eta_b(1S)) = (4.8 \pm 0.5 \pm 1.2) \times 10^{-4}$ 





Flavour Physics

subtract smoothly varying background



45

# Why wasn't the $\eta_b$ discovered at a hadronic experiment?

- Remember: Y(1S) discovered at FNAL in 1977
  - fixed target experiment: p on Be

PRL 39 (1977) 252

- $\eta_b$  is lighter
- Hadron collisions produce all types of b hadrons
- So why couldn't the  $\eta_b$  be discovered, e.g., at the Tevatron?



# Why wasn't the $\eta_b$ discovered at a hadronic experiment?

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PRL 39 (1977) 252

- $\eta_b$  is lighter
- Hadron collisions produce all types of b hadrons
- So why couldn't the  $\eta_b$  be discovered, e.g., at the Tevatron?
- It's all about the trigger!
  - need clean signature for trigger and reconstruction
  - CDF search used  $\eta_h \to J/\psi J/\psi$  decay, with predicted BF ~ 0!



## Digression on a digression: The "Oops Leon"

#### Observation of High-Mass Dilepton Pairs in Hadron Collisions at 400 GeV

D. C. Hom, L. M. Lederman, H. P. Paar, H. D. Snyder, J. M. Weiss, and J. K. Yoh.

Columbia University, New York, New York 10027\*

and

J. A. Appel, B. C. Brown, C. N. Brown, W. R. Innes, and T. Yamanouchi Fermi National Accelerator Laboratory, Botavia, Illinois 60510†

and

D. M. Kaplan

State University of New York at Stony Brook, Stony Brook, New York 11794\*
(Received 28 Sandary 1976)

We report preliminary results on the production of electron-position pairs in the mass range 2.5 to 20 GeV to 400-GeV p-Be interactions. 27 high-mass events are observed in the mass range  $5.5{\pm}10.0$  GeV corresponding to  $\sigma = (1.2 \pm 0.5) \times 10^{-35}$  cm<sup>2</sup> per nucleon. Clustering of 12 of these events between 5.8 and 6.2 GeV suggests that the data contain a new resonance at 6 GeV.

#### Homework exercise:

- 1. Read this paper
- 2. Do you find the "discovery" convincing?
  - 3. Explain what's wrong

PRL 36 (1976) 1236

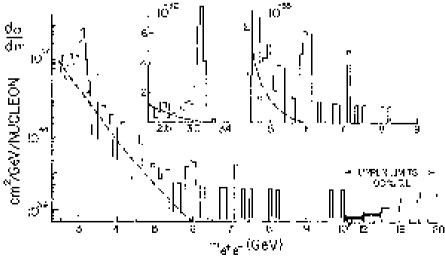


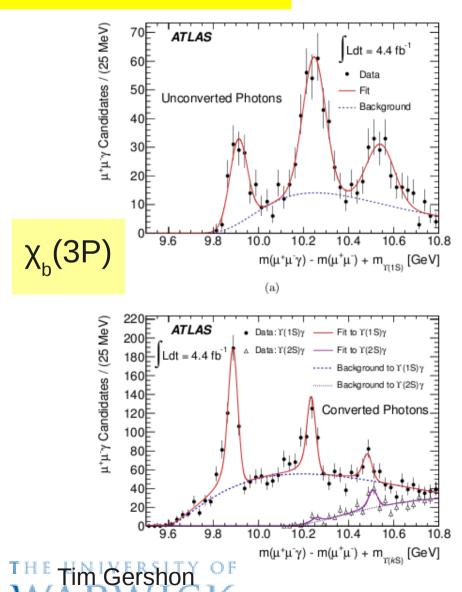
FIG. 2. Electron-positron mass spectrum:  $d\sigma/dm$  per nucleon versus the effective mass. A linear A dependence is assumed. Note bin-width changes.

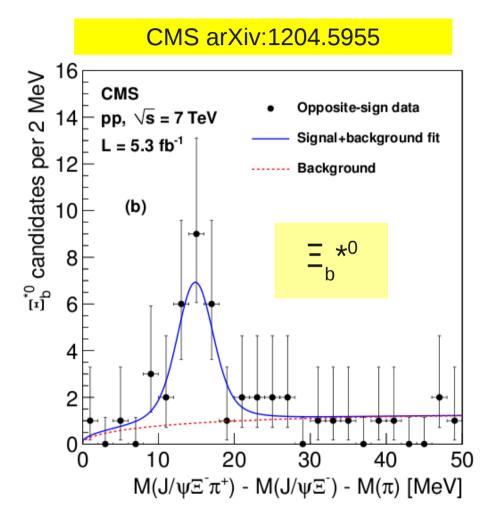


#### More new particles

#### ATLAS arXiv:1112.5154

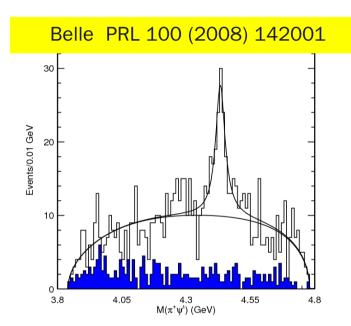
Flavour Physics



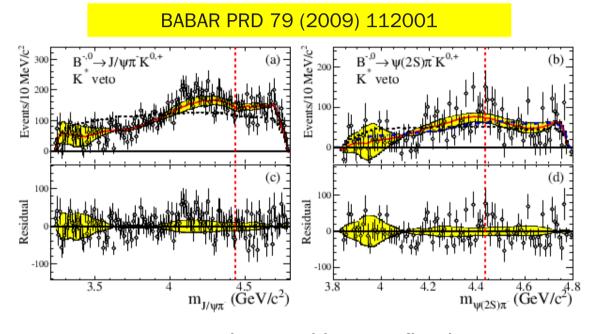


## The smoking gun exotic hadron: A charged charmonium-like state

 $B^0 \rightarrow Z(4430)^- K^+, \ Z(4430)^- \rightarrow \psi' \pi^-$ 



Clear peak Still there in more detailed analysis PRD 80 (2009) 031104



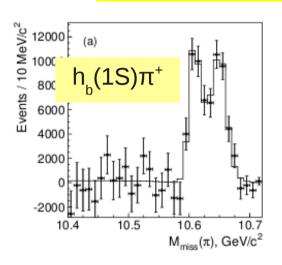
Data consistent with  $K\pi$  reflections Slight peak but no evidence for new state But also consistent with Belle

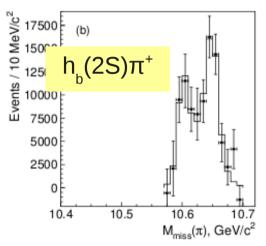


Need more experimental input (CDF, D0, ATLAS, CMS or LHCb)

## Charged bottomonium-like states

Belle PRL 108 (2012) 122001





Final state	$\Upsilon(1S)\pi^{+}\pi^{-}$	$\Upsilon(2S)\pi^{+}\pi^{-}$	$\Upsilon(3S)\pi^{+}\pi^{-}$	$h_b(1P)\pi^+\pi^-$	$h_b(2P)\pi^+\pi^-$
$M[Z_b(10610)], \text{ MeV}/c^2$	$10611 \pm 4 \pm 3$	$10609 \pm 2 \pm 3$	$10608 \pm 2 \pm 3$	$10605 \pm 2^{+3}_{-1}$	10599+6+5
$\Gamma[Z_b(10610)], \text{ MeV}$	$22.3 \pm 7.7^{+3.0}_{-4.0}$	$24.2 \pm 3.1^{+2.0}_{-3.0}$	$17.6 \pm 3.0 \pm 3.0$	$11.4^{+4.5+2.1}_{-3.9-1.2}$	$13^{+10+9}_{-8-7}$
$M[Z_b(10650)], \text{ MeV}/c^2$	$10657 \pm 6 \pm 3$	$10651 \pm 2 \pm 3$	$10652 \pm 1 \pm 2$	$10654 \pm 3^{+1}_{-2}$	$10651^{+2+3}_{-3-2}$
$\Gamma[Z_b(10650)], \text{ MeV}$	$16.3 \pm 9.8^{+6.0}_{-2.0}$	$13.3 \pm 3.3^{+4.0}_{-3.0}$	$8.4 \pm 2.0 \pm 2.0$	$20.9^{+5.4+2.1}_{-4.7-5.7}$	$19 \pm 7^{+11}_{-7}$
Rel. normalization	$0.57 \pm 0.21^{+0.19}_{-0.04}$	$0.86 \pm 0.11^{+0.04}_{-0.10}$	$0.96 \pm 0.14^{+0.08}_{-0.05}$	$1.39 \pm 0.37^{+0.05}_{-0.15}$	$1.6^{+0.6+0.4}_{-0.4-0.6}$
Rel. phase, degrees	$58 \pm 43^{+4}_{-9}$	$-13 \pm 13^{+17}_{-8}$	$-9 \pm 19^{+11}_{-26}$	$187^{+44+3}_{-57-12}$	$181^{+65+74}_{-105-109}$

