# **Detection of Voids in Additive** Manufacturing Using X-rays

Sherman E. Lo, Statistics, University of Warwick Warnett, J.M., Gibbons, G.J., Williams, M.A., Nichols, T.E., and Brettschneider, J.A.

### **1. Introduction**

In x-ray computed tomography, multiple angular projections are obtained to reconstruct the object in 3D space to look for defects. The process can be time-consuming.

The aim is to investigate if defect detection can be done using a single angular projection. An additive manufactured test sample was created with voids to see if they can be detected.



Figure 1: X-ray computed tomography Source: Warnett et al. (2016)



Figure 2: Log frequency density histogram of the mean and variance grey values from projections of the test sample.

## 2. Compound Poisson

The projection was modelled using a compound Poisson distribution because x-ray photon arrivals are a Poisson process. This result in a linear relationship between the mean and variance.

A gamma distributed generalised linear model was fitted and used for variance prediction.

### **3. Inference**

 $\times 10^{4}$ 

A simulation of the projection was compared with the obtained projection under the face of uncertainty.

$$\frac{\operatorname{projection}_{x,y} - \operatorname{simulation}_{x,y}}{\sqrt{\operatorname{Var}\left[\operatorname{projection}_{x,y}\right]}} \sim \operatorname{N}\left(\widehat{\mu}_{0,x,y}, \widehat{\sigma}_{0,x,y}^2\right)$$

To overcome the imperfections of the simulation, the empirical null filter was used to cater for model misspecification so that sensible inference was achieved.

![](_page_0_Figure_18.jpeg)

#### Figure 3: X-ray projection of the test sample, highlighted in red are positive pixels at the 5% FDR level.

#### Funded by EPSRC EP/L016710/1