



## **Nonadiabatic dynamics in the long timescale**

**The next challenge in computational  
photochemistry**

Mario Barbatti

Aix Marseille University, Institut de Chimie Radicalaire

Institut Universitaire de France

[www.barbatti.org](http://www.barbatti.org)

# The Light and Molecules Group

[www.barbatti.org](http://www.barbatti.org)



## Methods

Mixed quantum-classical  
dynamics



## Software

NEWTON-X  
ULAMDYN  
PYSOC



## Applications

Photoprocesses in

- Fundamental PhysChem
- Molecular biology
- Organic devices
- Environment

# The Light and Molecules Group

[www.barbatti.org](http://www.barbatti.org)

Mario Barbatti (PI)

Baptiste Demoulin (IT researcher)

Josene Toldo (postdoc)

Max Pinheiro Jr (postdoc)

Saikat Mukherjee (postdoc)

Moumita Kar (postdoc)

Mariana Casal (PhD candidate)

Ritam Mansour (PhD candidate)

Rafael Mattos (PhD candidate)

Elizete Ventura (visiting res, Joao Pessoa)

Silmar Monte (visiting res, Joao Pessoa)

Mattia Bondanza (PhD internship, Pisa)

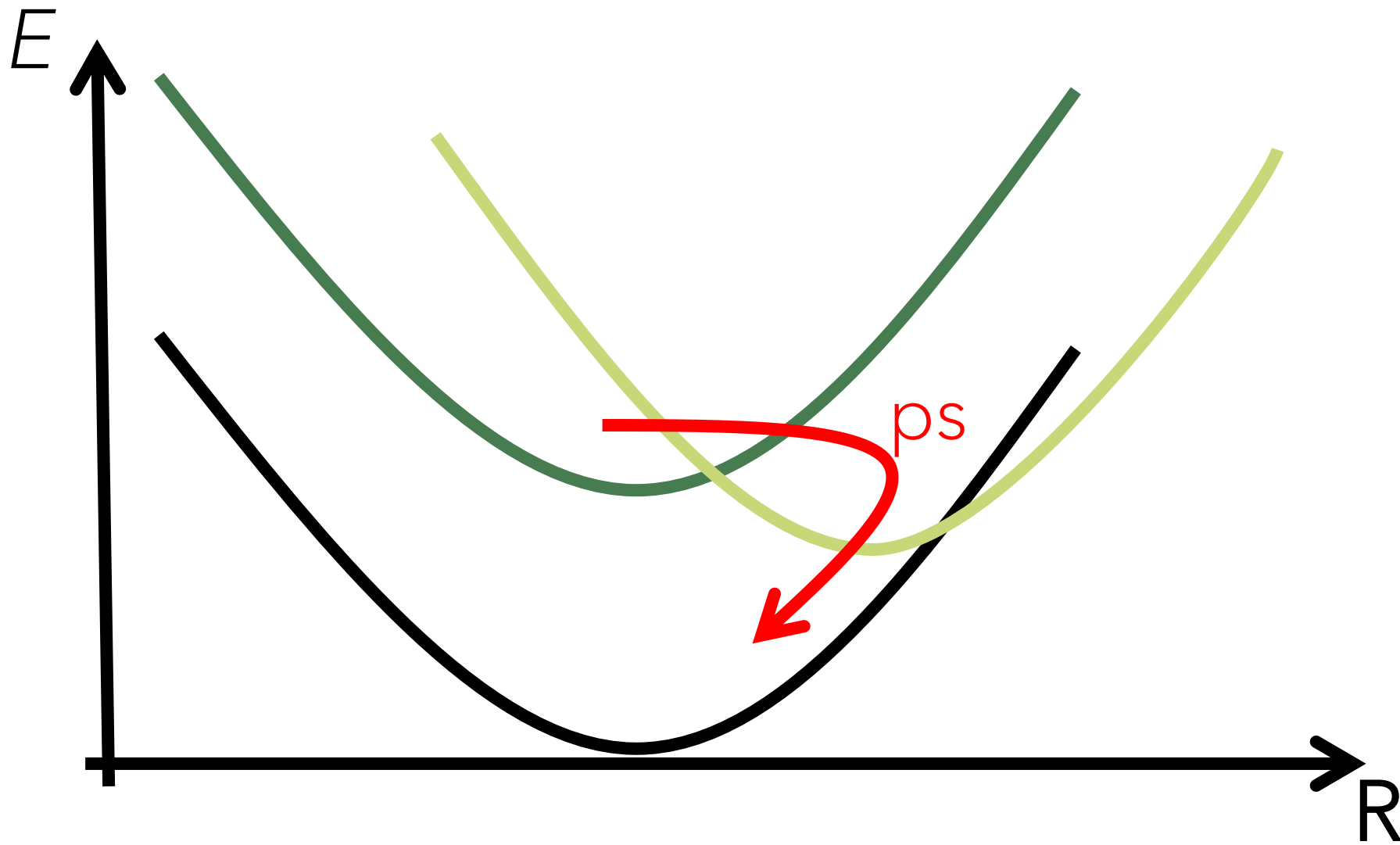
Euarda Gil (PhD insternship, Pisa)

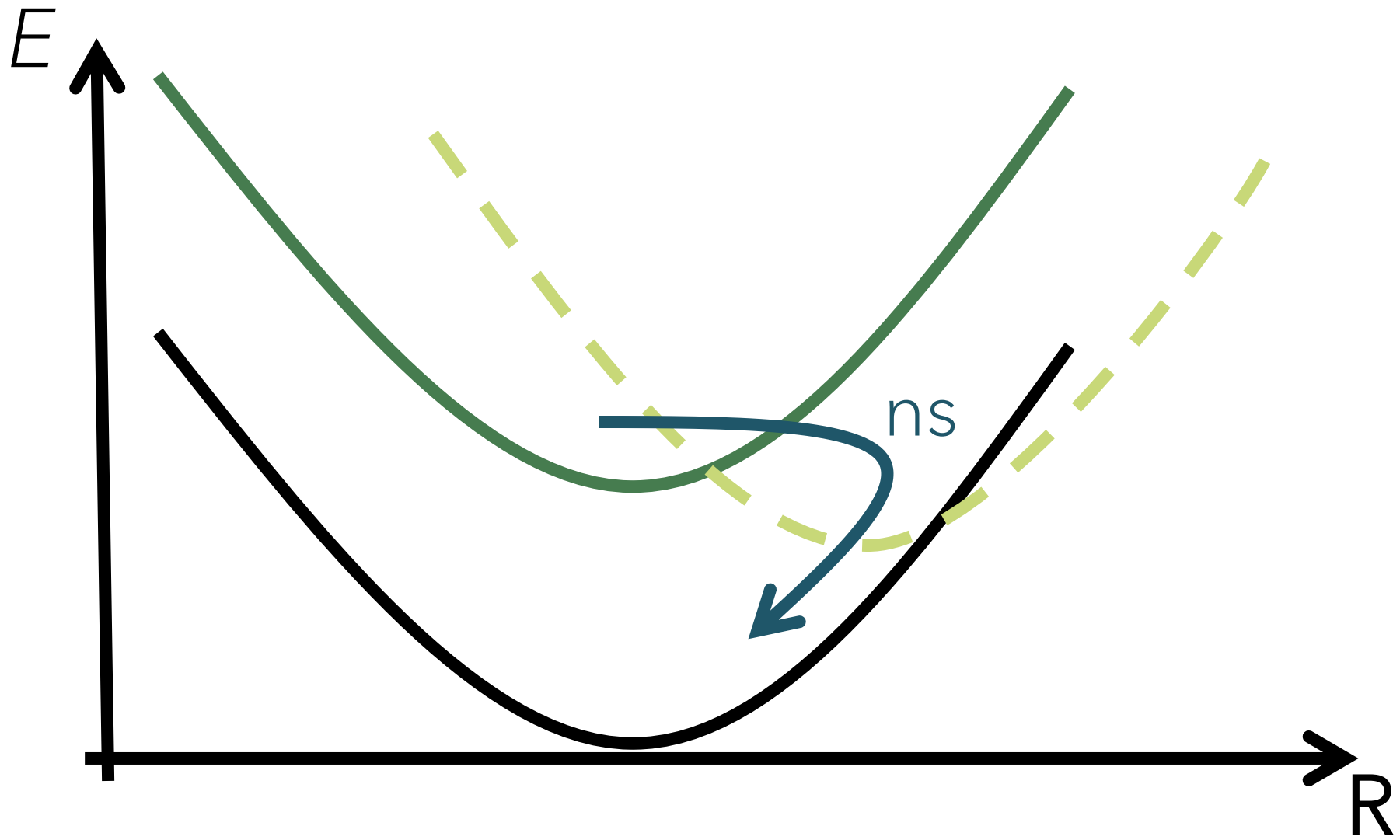
Mansi Bhati (PhD internship, Bohpal)

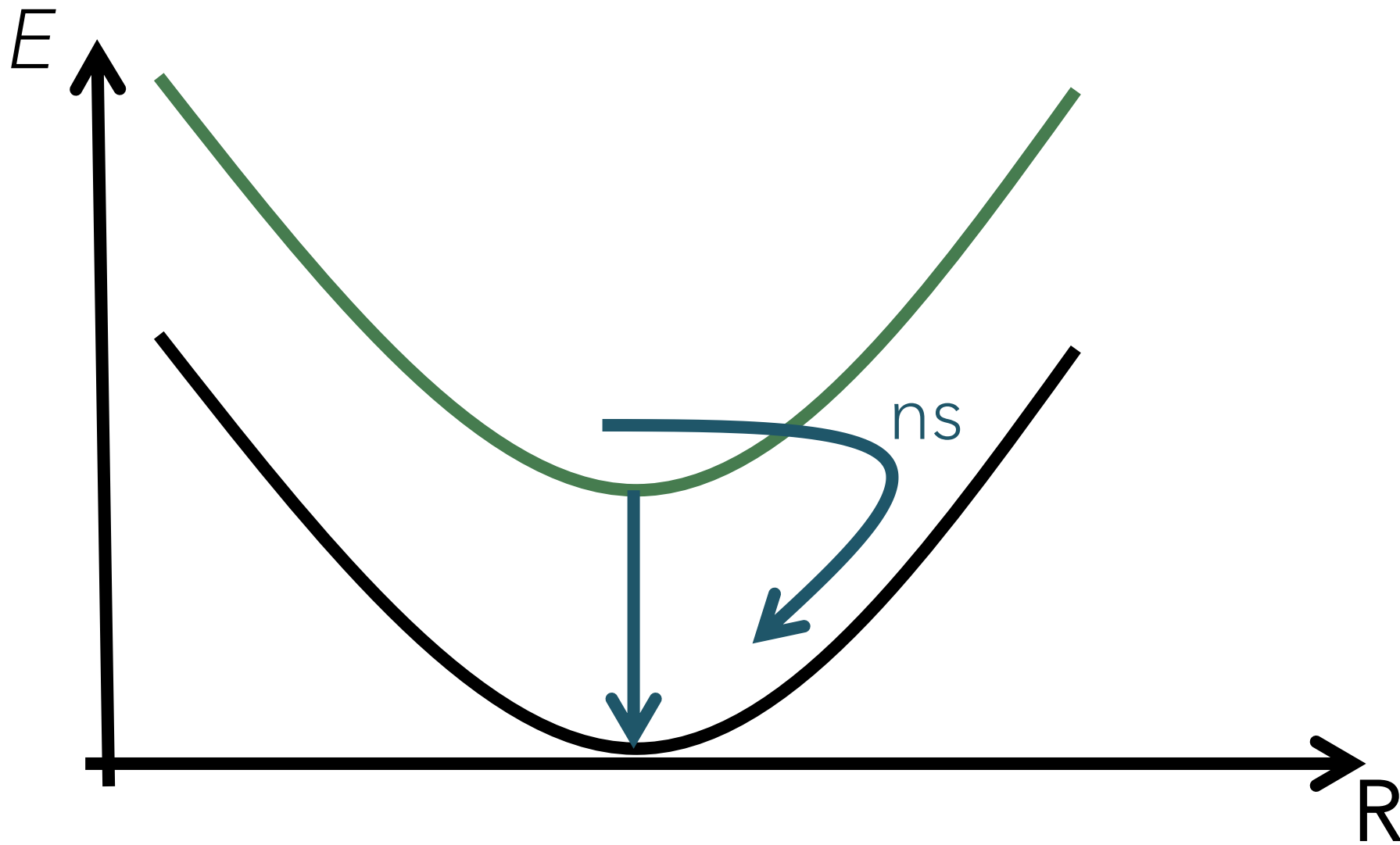
Mithun M (PhD internship, Bathinda)

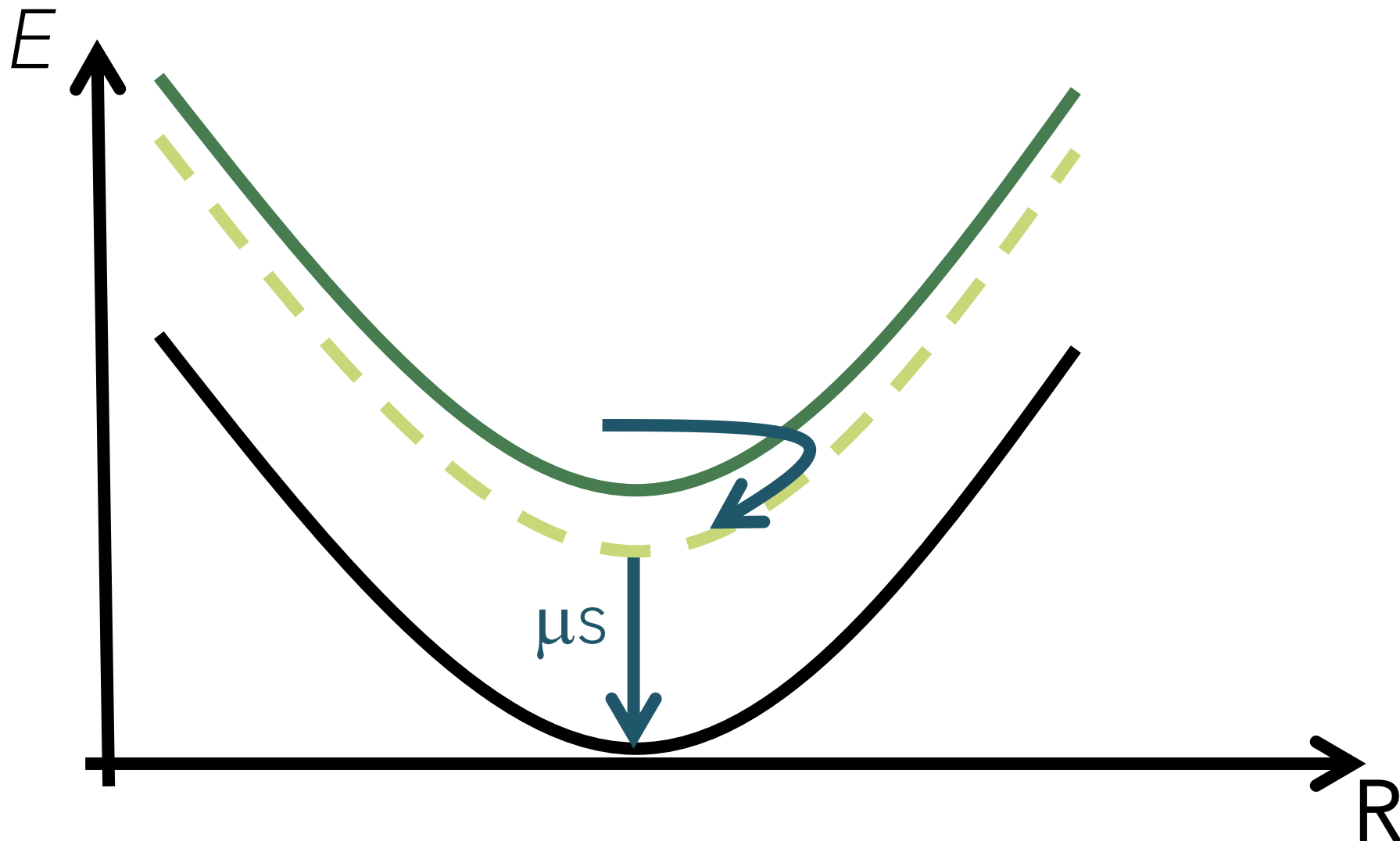
Soumaya Moussa (MSc internship, Marseille)

Nesrine Haddaji (MSc internship, Tunis)









- Akimov. *J Phys Chem Lett* **2017**, 8, 5190
- Westermayr et al. *Chem Sci* **2019**, 10, 8100
- Barbatti. *JCTC* **2020**, 16, 4849
- Li et al. *Chem Sci* **2021**, 12, 5302
- Mukherjee et al. *Philos Trans R Soc A* **2022**, DOI: 10.1098/rsta-2020-0382



**What do we want from a  
long timescale method?**

# What do we want from a long timescale method?

- It should consider all nuclear degrees of freedom
- It can be applied to any type of molecule
- It should not require much more computational resources than we use today

The primary advantage of dynamics is to reveal non-trivial reaction pathways, beyond our chemical intuition.

It loses this edge in reduced dimensionality.

Mixed quantum-classical methods are the best options for nonadiabatic, full dimensional dynamics.

# What do we want from a long timescale method?

- ☑ It should consider all nuclear degrees of freedom
- ☑ It can be applied to any type of molecule
- ☑ It should not require much more computational resources than we use today

# Dynamics is expensive

$$T_{total} \approx N_{\text{Trajectories}} \times \frac{\tau_{\text{chem process}}}{\Delta\tau} \times T_{\text{Single Point}}$$

$$N_{\text{Trajectories}} = 100 \text{ trajectories}$$

$$T_{\text{Single Point}} = 0.1 \text{ CPU.h}$$

$$\tau_{\text{chem process}} = 0.5 \text{ ns}$$

$$\Delta\tau = 0.5 \text{ fs}$$

$$T_{total} \approx 10 \text{ MCPU.h}$$

$$\text{Price 1 CPU.h} = 0.02 \text{ €}$$

$$\text{Price 10 MCPU.h} = 200 \text{ k€}$$

How much does dynamics cost? [tinyurl.com/dyncost](https://tinyurl.com/dyncost)

How many trajectories should we run? [tinyurl.com/trajs](https://tinyurl.com/trajs)

# Dynamics leaves a huge carbon footprint

1 CPU.h =  $4 \times 10^{-5}$  tCO<sub>2</sub>e

10 MCPU.h = 400 tCO<sub>2</sub>e

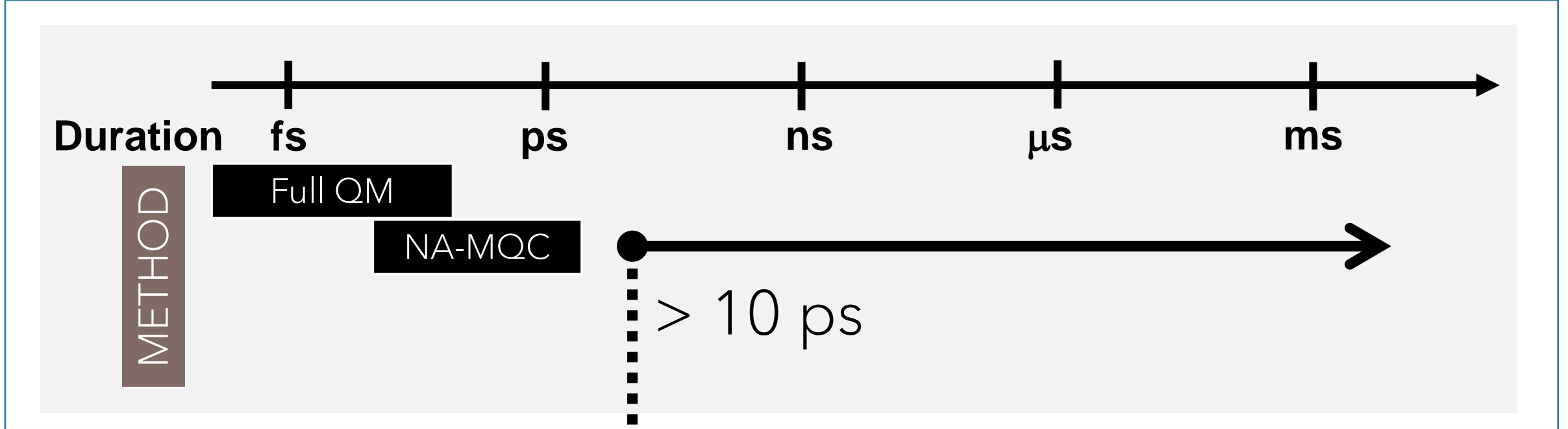


11.5 tCO<sub>2</sub>e/year



35 French people

**What is a *long timescale*  
anyway?**



$$> 10 \text{ ps} / 0.1 \text{ fs} = 100,000 \text{ time steps}$$



Characteristic timestep

$$\Delta\tau = \frac{1}{10} \min \left[ \sqrt{\frac{|\Delta R_{ij}|}{|\Delta a_{ij}|}} \right]$$

Characteristic timestep

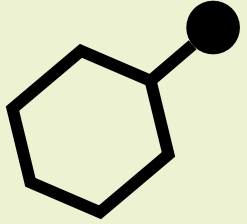
$$\Delta\tau = \frac{1}{10} \min \left[ \sqrt{\frac{|\Delta R_{ij}|}{|\Delta a_{ij}|}} \right]$$

Hamonic oscillator

$$\Delta\tau = \frac{1}{20\pi f}$$

Gravitational motion

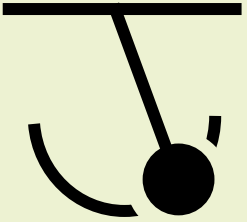
$$\Delta\tau = \frac{1}{10} \min \left[ \sqrt{\frac{\Delta R^3}{GM}} \right]$$



$$\Delta\tau = \frac{1}{20\pi f}$$

$$f = 3000 \text{ cm}^{-1}$$

$$\Delta\tau \approx 0.1 \text{ fs}$$
$$\tau > 10 \text{ ps}$$



$$\Delta\tau = \frac{1}{20\pi f}$$

$$f = 1 \text{ Hz}$$

$$\Delta\tau \approx 0.01 \text{ s}$$
$$\tau > 16 \text{ min}$$



$$\Delta\tau = \frac{1}{10} \text{ min} \left[ \sqrt{\frac{\Delta R^3}{GM}} \right]$$

*Earth orbital motion*

$$\Delta\tau \approx 100 \text{ h}$$
$$\tau > 1100 \text{ years}$$

# How to get there?

# Challenges we must face

- Extreme cost reduction
- Stability of integration
- Accuracy of MQC methods
- Software optimization

# Challenges we must face

- Extreme cost reduction
- Stability of integration
- Accuracy of MQC methods
- Software optimization

# Challenges we must face

- Extreme cost reduction
  - Parameterized quantum chemistry
  - Model Hamiltonians
  - Machine learning potentials

## Excited-state parameterized methods:

- FOMO-CI (Persico, Granucci)
- OM2-MRCI (Thiel)
- TD-SCF (Tretiak et al.)
- TD-DFTB (Niehaus, Mitrić)
- TD-KS (Akimov, Prezhdo)

They are fast, general, and full dimensional.

However, accuracy and parameterization pose serious issues.



# Challenges we must face

- Extreme cost reduction
  - Parameterized quantum chemistry
  - Model Hamiltonians
  - Machine learning potentials

# Example: Adiabatic Spin-Boson Hamiltonian (SBH)

Energies

$$V_i = \frac{1}{2} \sum_{j=1}^N M_j \omega_j^2 R_j^2 + (-1)^i [\eta^2 + v_0^2]^{1/2} \quad (i = 1, 2)$$

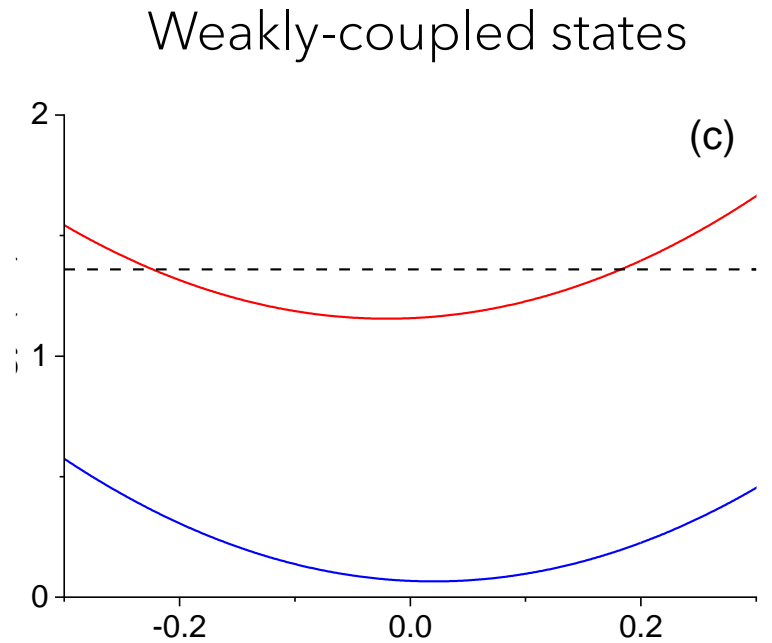
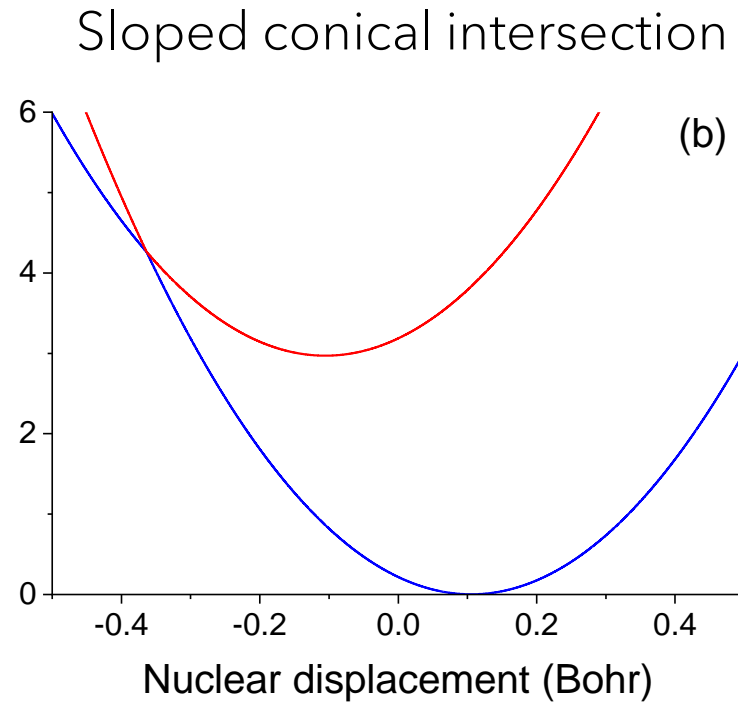
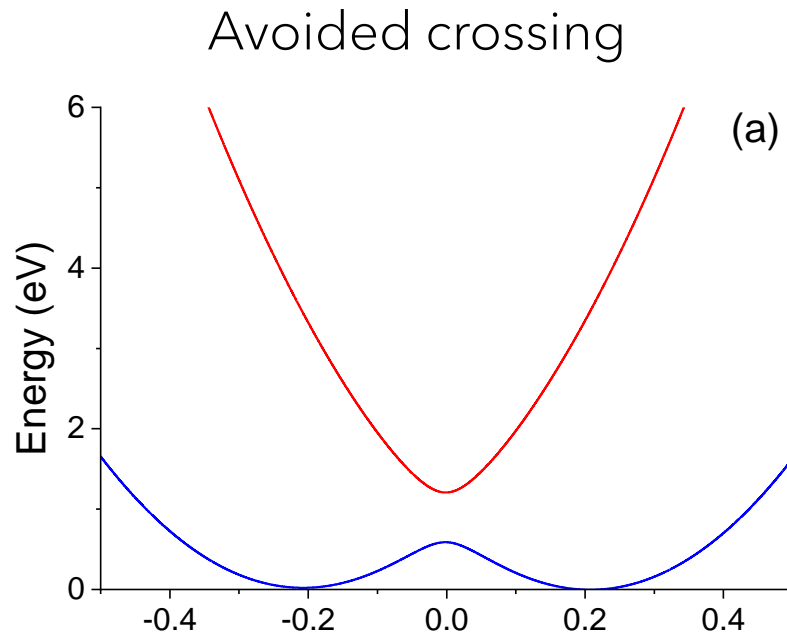
Energy gradients

$$\frac{\partial V_i}{\partial R_k} = M_k \omega_k^2 R_k + (-1)^i g_k \left[ \frac{\eta}{[\eta^2 + v_0^2]^{1/2}} \right] \quad (k = 1 \cdots N)$$

Nonadiabatic couplings

$$h_{12}^k = -h_{21}^k = -\frac{1}{2} g_k \left[ \frac{v_0}{\eta^2 + v_0^2} \right]$$

# 1D cut of different SBH models



# Full dimensional H-models $[(3N_a-6)D]$

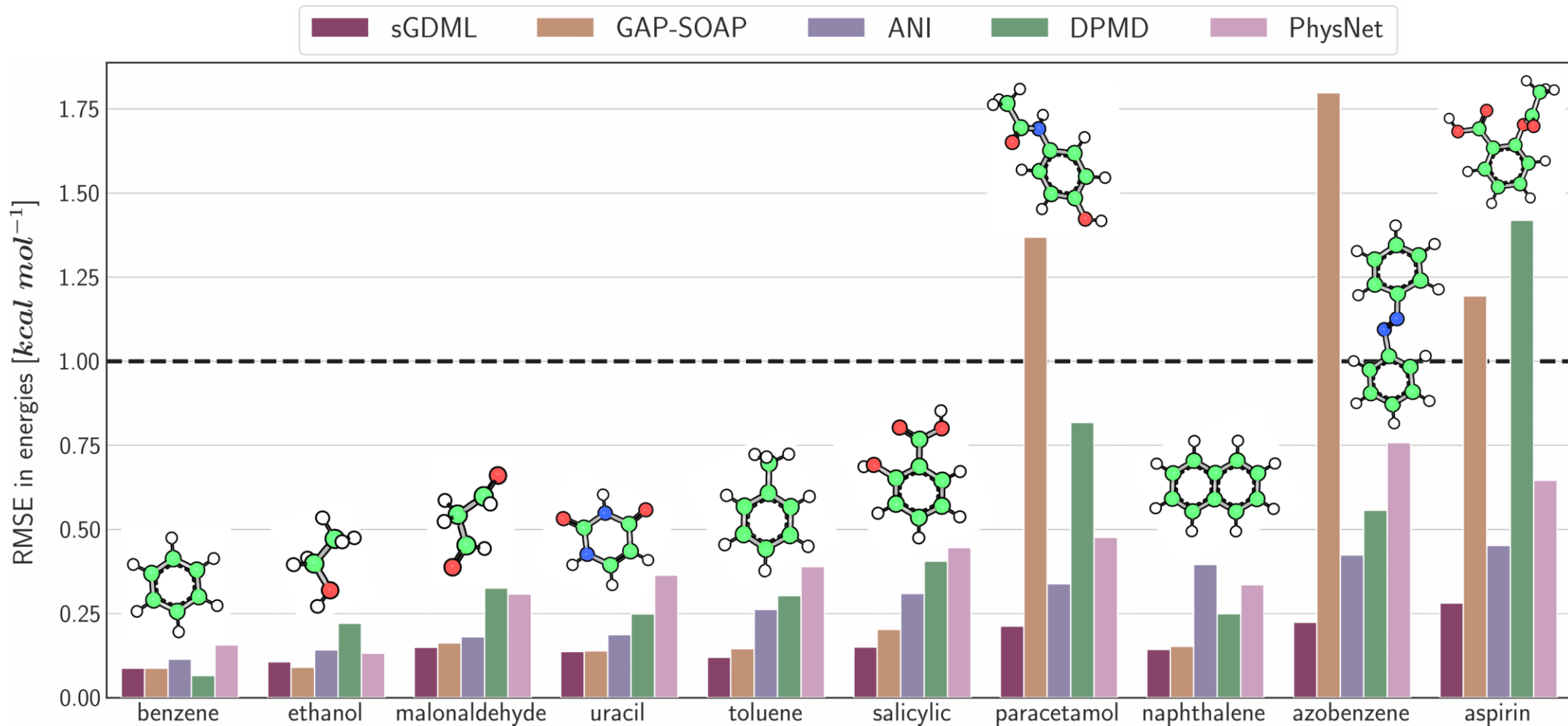
H Model	# states	# parameters	Pros	Cons
SBH	2	$2(3N_a-5)$	Analyt. adiabatic rep.	Low flexibility
LVC	$N_s$	$(3N_a-6)N_s(N_s+1)/2$	Number of states	Parameterization
...				

SBH: Leggett et al. *Rev Mod Phys* **1987**, 59, 1

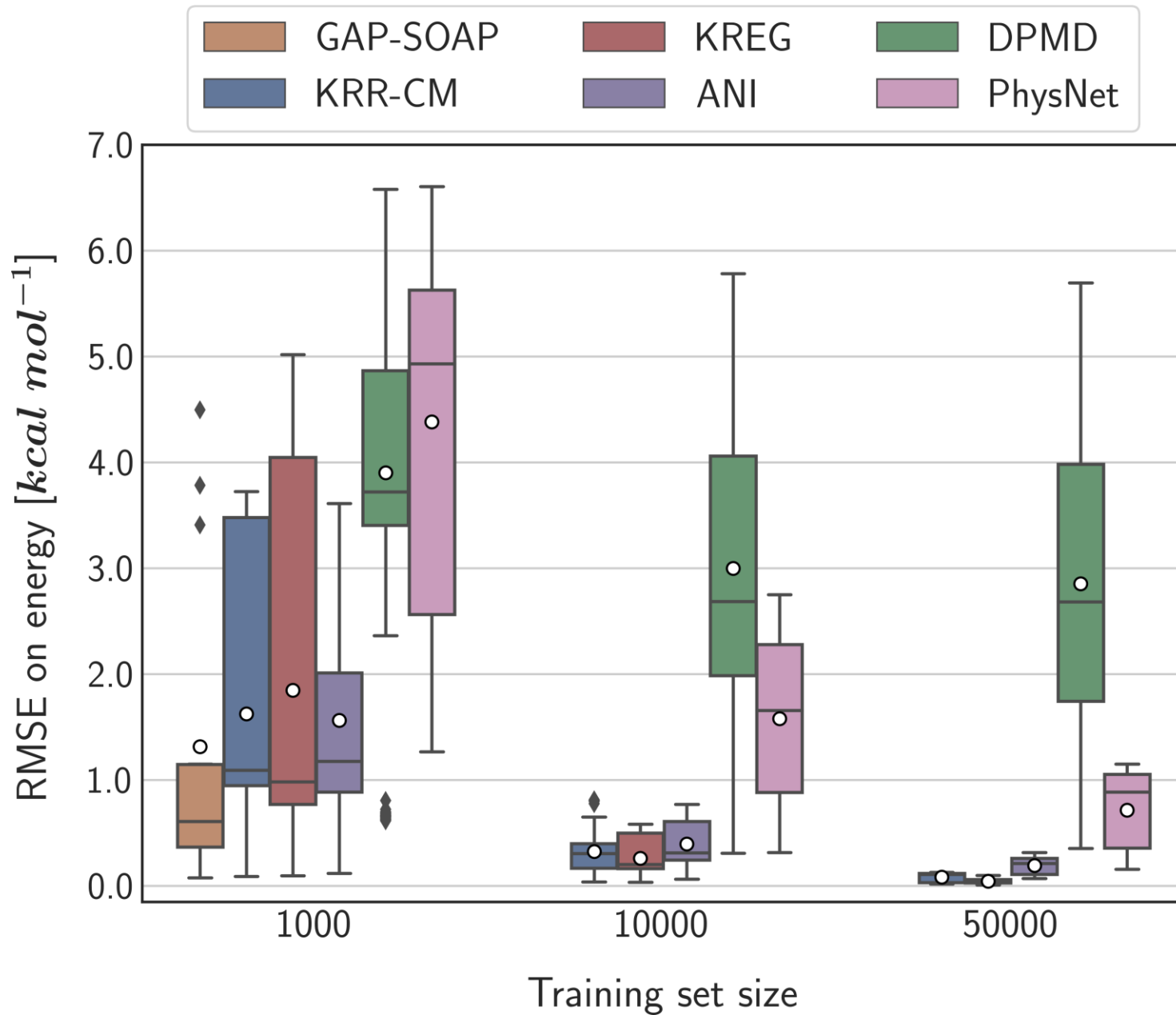
LVC: Koppel; Domcke; Cederbaum. *Adv Chem Phys* **1984**, 57, 59

# Challenges we must face

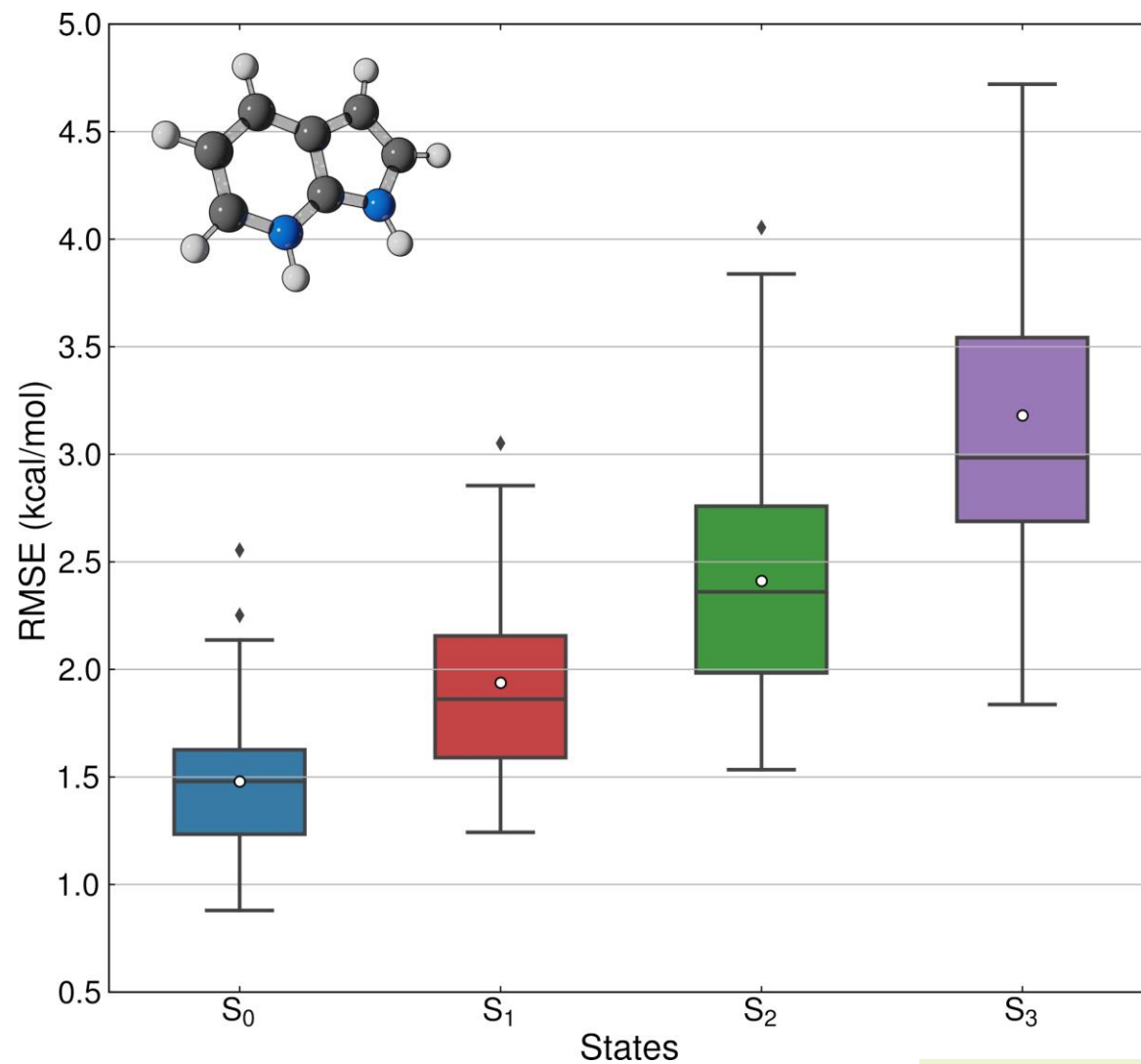
- Extreme cost reduction
  - ☑ Parameterized quantum chemistry
  - ☑ Model Hamiltonians
  - ☑ Machine learning potentials



- MD17 Database
- Energy + Force
- $N_{train} = 1k$ ;  $N_{model} = 20$ ;  $N_{test} = 20k$



- MD17 Database
- Energy only
- $N_{test} = 20k$



- RI-ADC(2)/cc-pVDZ
- DC-FSSH: 50 traj; 0.5 fs; 300 ps



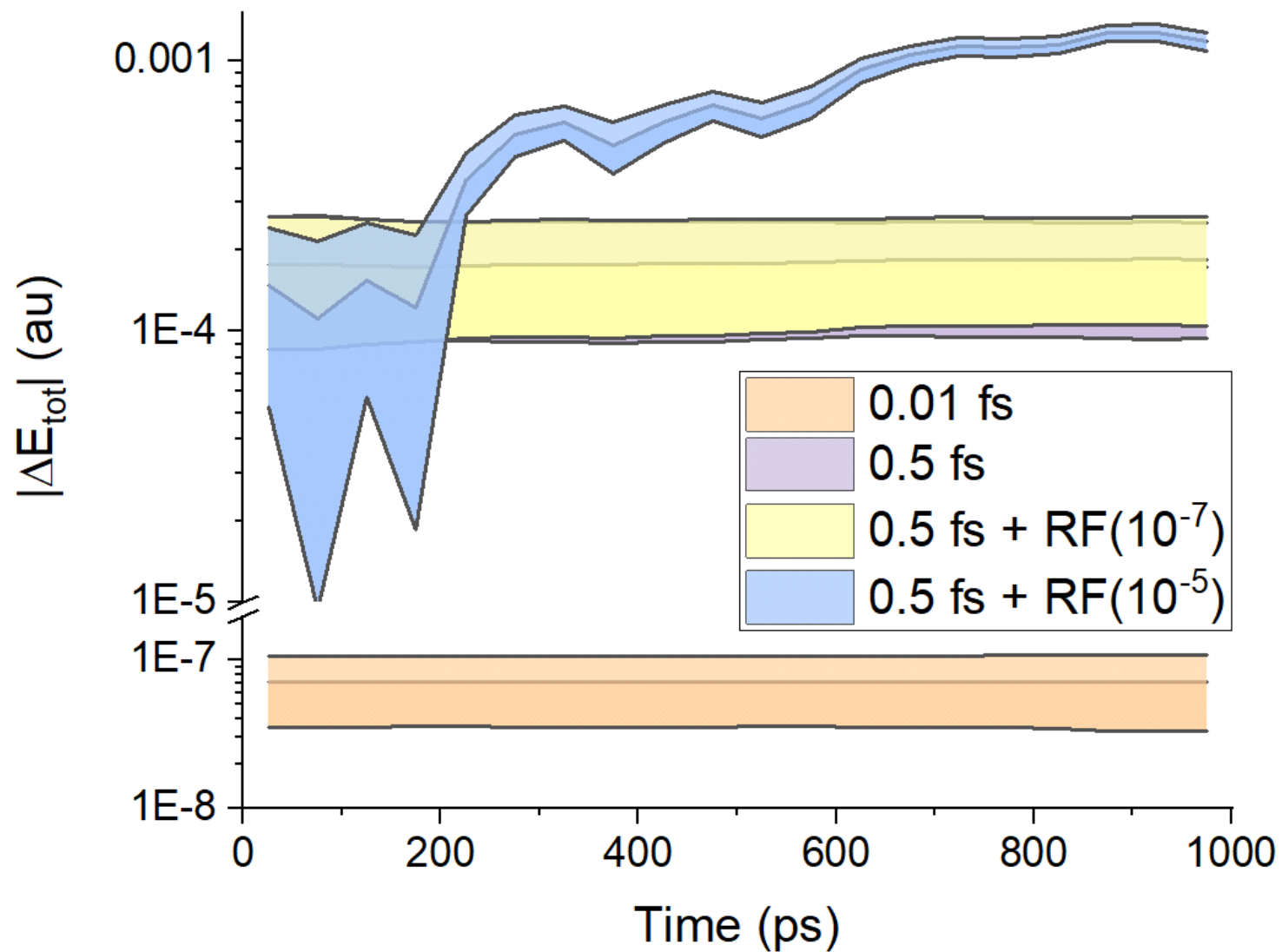
# Challenges we must face

- Extreme cost reduction
- Stability of integration
- Accuracy of MQC methods
- Software optimization

# Challenges we must face

- Stability of integration
  - Performance of integration algorithms
  - ZPE spilling

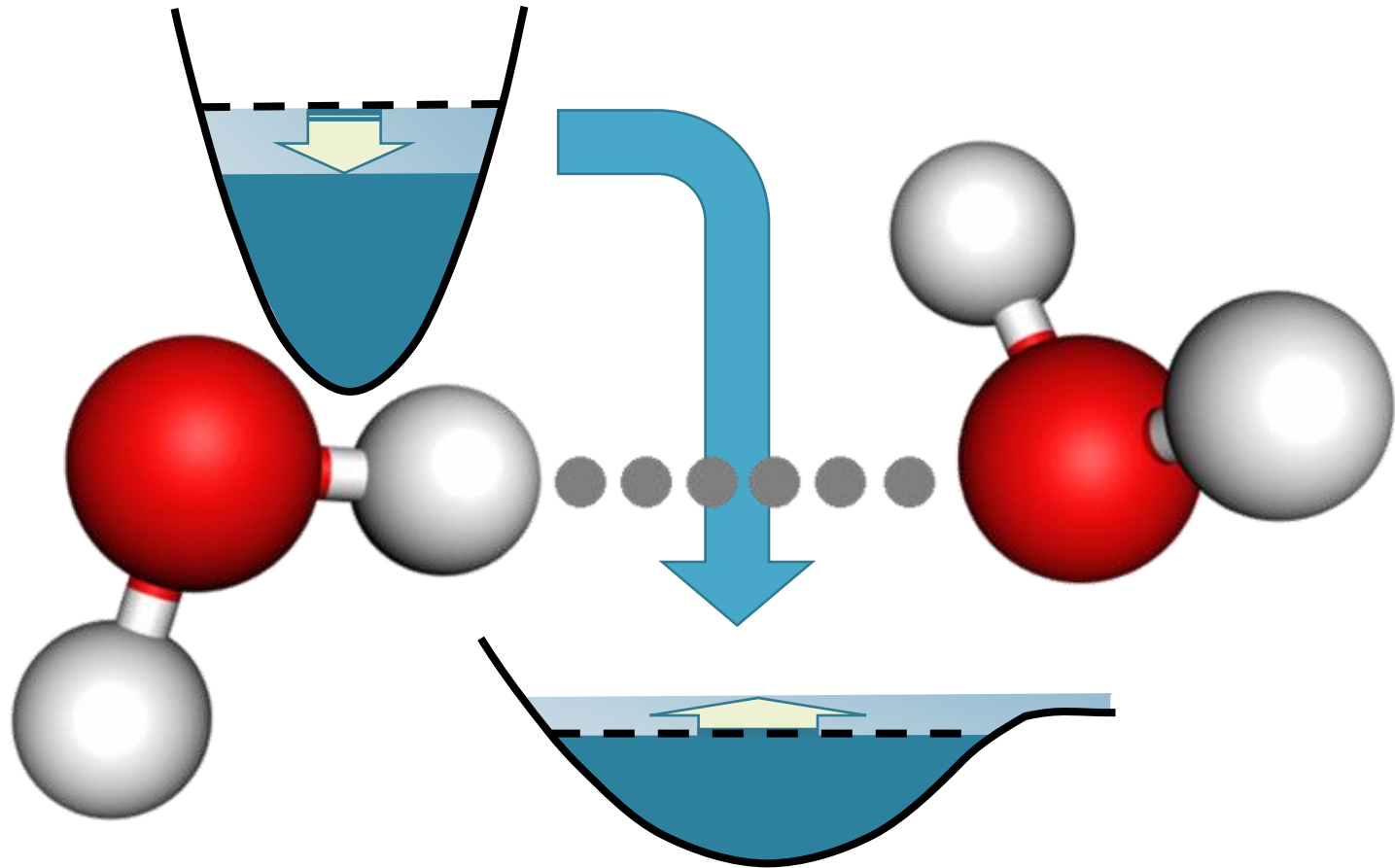
# Velocity Verlet

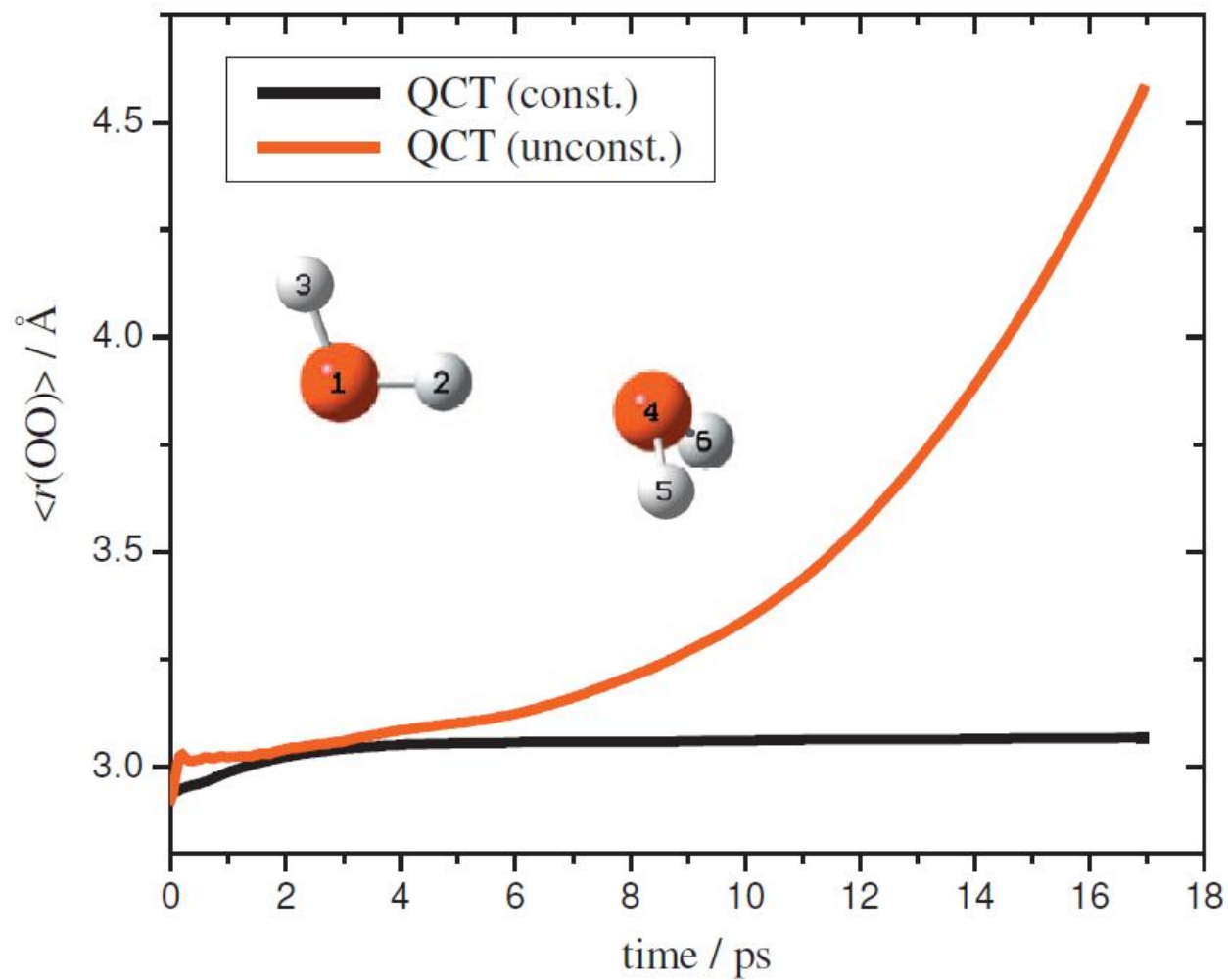


- A-SBH 33D
- dynamics on  $V_2$

# Challenges we must face

- Stability of integration
  - ☑ Performance of integration algorithms
  - ☑ ZPE spilling





There are many ZPE-corrections proposed.

But they either require Hessians  
or introduce statistical biases.

Miller; Hase; Darling. *J Chem Phys* **1989**, 91, 2863

Bowman; Gazdy; Sun. *J Chem Phys* **1989**, 91, 2859

Varandas; Marques. *J Chem Phys* **1994**, 100, 1908

Guo; Thompson; Sewell. *J Chem Phys* **1996**, 104, 576

....

Czakó; Kaledin; Bowman. *J Chem Phys* **2010**, 132, 164103

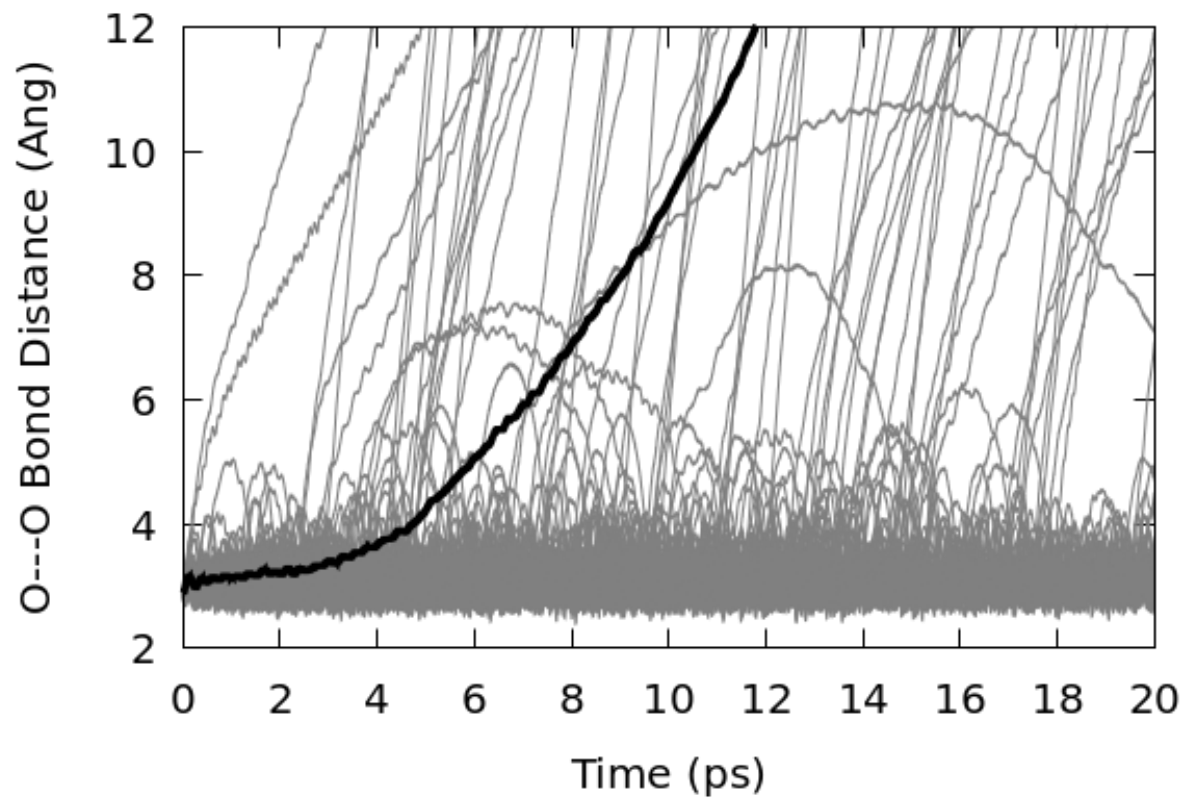
Recently, Saikat Mukherjee and I developed a **Hessian-free ZPE correction**.

It works like a thermostat, transferring kinetic energy from the slow vibrations into fast vibrations, whenever a ZPE drop is detected.

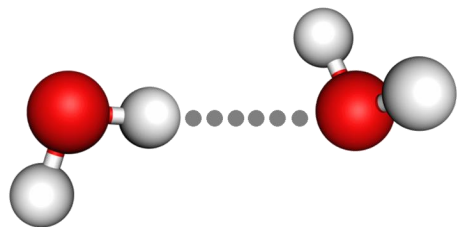
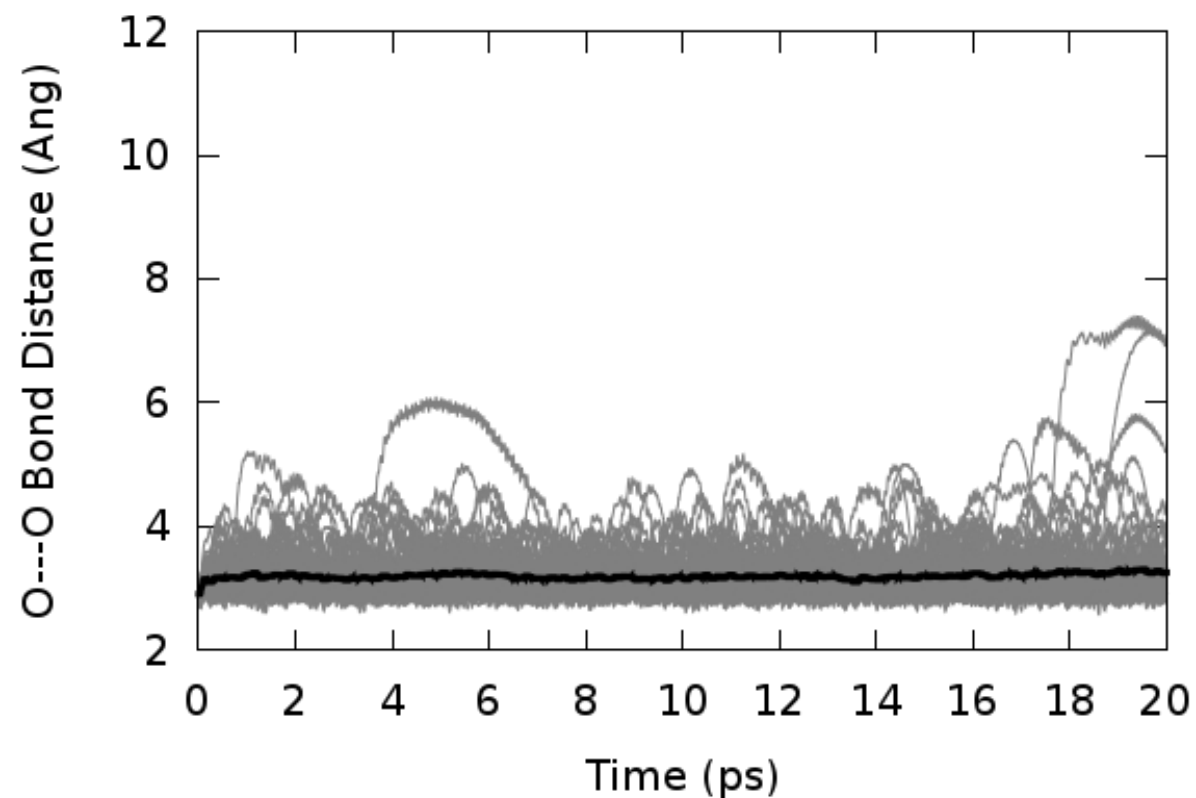
The correction conserves energy, momentum, and CM angular momentum.



No ZPE Correction



Hessian-free ZPE Correction



- $S_0$  MP2/aug-cc-pVDZ
- 100 trajs; 20 ps;  $\Delta t = 0.5$  fs
- ZPE correction every 10 fs

# Challenges we must face

- Extreme cost reduction
- Stability of integration
- Accuracy of MQC methods
- Software optimization

# Terms mediating nonadiabatic transitions

## Full TDSE

$$H_{IJ} \propto \sum_{\alpha=1}^{3N_a} \frac{\hbar^2}{M_\alpha} \left\langle \chi_k^{(J)} \left| \left\langle \Phi_J \left| \frac{\partial}{\partial R_\alpha} \right| \Phi_I \right\rangle_{\mathbf{r}} \frac{\partial}{\partial R_\alpha} \right| \chi_i^{(I)} \right\rangle_{\mathbf{R}} + \sum_{\alpha=1}^{3N_a} \frac{\hbar^2}{2M_\alpha} \left\langle \chi_k^{(J)} \left| \left\langle \Phi_J \left| \frac{\partial^2}{\partial R_\alpha^2} \right| \Phi_I \right\rangle_{\mathbf{r}} \right| \chi_i^{(I)} \right\rangle_{\mathbf{R}}$$

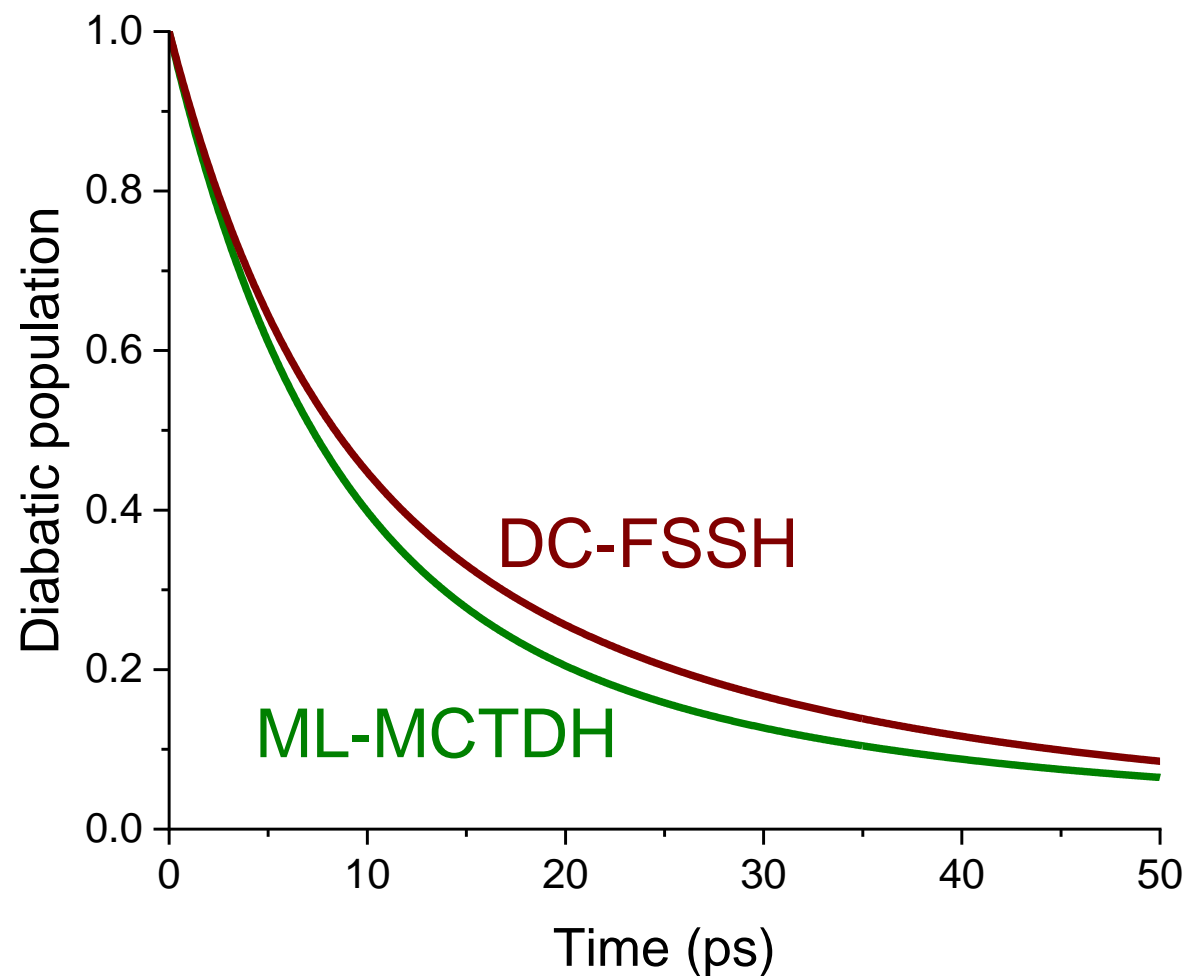
## AIMS

$$H_{IJ} \propto \sum_{\alpha=1}^{3N_a} \frac{\hbar^2}{M_\alpha} \left\langle \chi_k^{(J)} \left| \frac{\partial}{\partial R_\alpha} \right| \chi_i^{(I)} \right\rangle_{\mathbf{R}} \left\langle \Phi_J \left| \frac{\partial}{\partial R_\alpha} \right| \Phi_I \right\rangle_{\mathbf{r}} \Big|_{\bar{\mathbf{R}}}$$

## FSSH

$$H_{IJ} \propto \sum_{\alpha=1}^{3N_a} \frac{\hbar}{M_\alpha} \bar{p}_\alpha \left\langle \Phi_J \left| \frac{\partial}{\partial R_\alpha} \right| \Phi_I \right\rangle_{\mathbf{r}} \Big|_{\bar{\mathbf{R}}}$$

# A-SBH 10D (weak coupling)



- DC-FSSH: 2000 traj; 0.1 fs; 100 ps
- ML-MCTDH: SPFs = 16; Grid size = 64

# Challenges we must face

- Extreme cost reduction
- Stability of integration
- Accuracy of MQC methods
- Software optimization

# Challenges we must face

- Software optimization
  - Fast processing
  - Handling big data
  - Comply with open-data requirements



# Newtonian Dynamics Close to the X-Seam

## The NEWTON-X platform

- Surface hopping & Nuclear ensemble spectrum simulations
- Freeware
- Open source
- Simulations with MRCI, MCSCF, CASPT2, ADC(2), TDDFT, TD-DFTB, Analytical models, Machine learning potentials



Newton-X  
new series

### **Speed-up execution**

- Rewriting core loop
- Minimize I/O

### **Optimize development environment**

- Restructuring variable management
- GitLab UI
- Clear development protocol

### **Comply with new open data standard**

- HDF5 data standard (H5MD)

### **Keep established functionalities**

- Deep-level cleaning & debugging





## Rewriting the core loop

### NEWTON-X CS

**PERL:**

for  $t = 0$  until  $t = t_{max}$

$E_K, \nabla E_K, |\psi_K\rangle =$  **PERL:** call **EXTERNAL PROG ( R )**

$\mathbf{R}, \mathbf{v} =$  call **FORTRAN:** **VELOCITY VERLET ( R, v,  $\nabla E_L$  )**

$\sigma_{LK} =$  call [**PERL:C++**]: **COUPLING (  $|\psi_L\rangle, |\psi_K\rangle$  )**

$L =$  call **FORTRAN:** **SURFACE HOPPING(  $E_K, \sigma_{LK}, \mathbf{v}_L$  )**

$t = t + \Delta t$

### NEWTON-X NS

**FORTRAN:**

for  $t = 0$  until  $t = t_{max}$

$E_K, \nabla E_K, |\psi_K\rangle =$  call **PERL:** **EXTERNAL PROG ( R )**

$\mathbf{R}, \mathbf{v} =$  call **FORTRAN:** **VELOCITY VERLET ( R, v,  $\nabla E_L$  )**

$\sigma_{LK} =$  call [**FORTRAN:C++**]: **COUPLING (  $|\psi_L\rangle, |\psi_K\rangle$  )**

$L =$  call **FORTRAN:** **SURFACE HOPPING(  $E_K, \sigma_{LK}, \mathbf{v}_L$  )**

$t = t + \Delta t$



Newton-X  
new series

**NEWTON-X CS**

**05:40:00**

**NEWTON-X NS**

**00:11:00**

- A-SBH 10D
- DC-FSSH: 1 traj, 0.1 fs; 1 ps
- 1 core

LIGHT AND  
MOLECULES



Newton-X  
new series

## New data format **H5MD: MD-oriented HDF5**

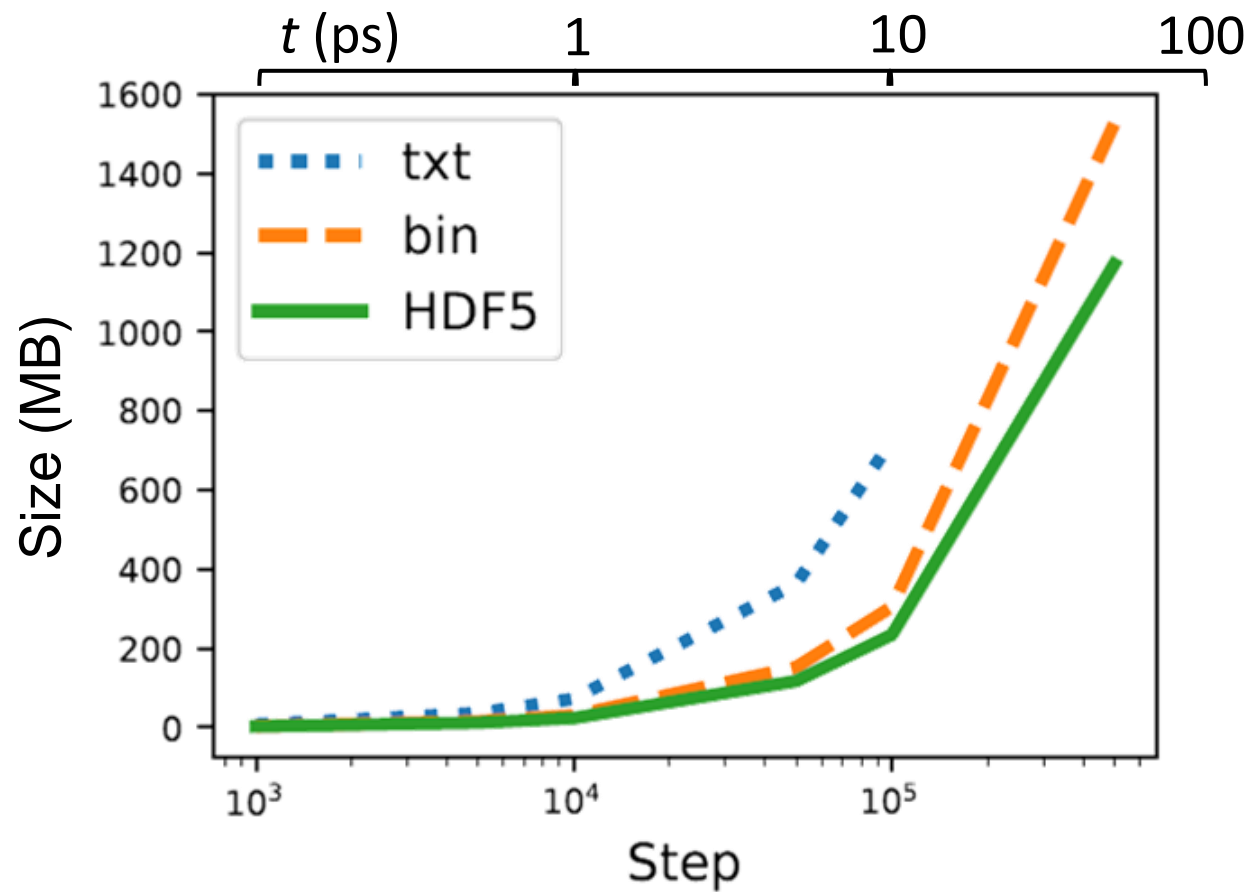
- ✓ Data structured
- ✓ Data compressed
- ✓ Fast and parallel I/O
- ✓ Portable
- ✓ Self-contained

de Buyl; Colberg; Höfling. *Comput Phys Commun* **2014**, 185, 1546

LIGHT AND  
MOLECULES

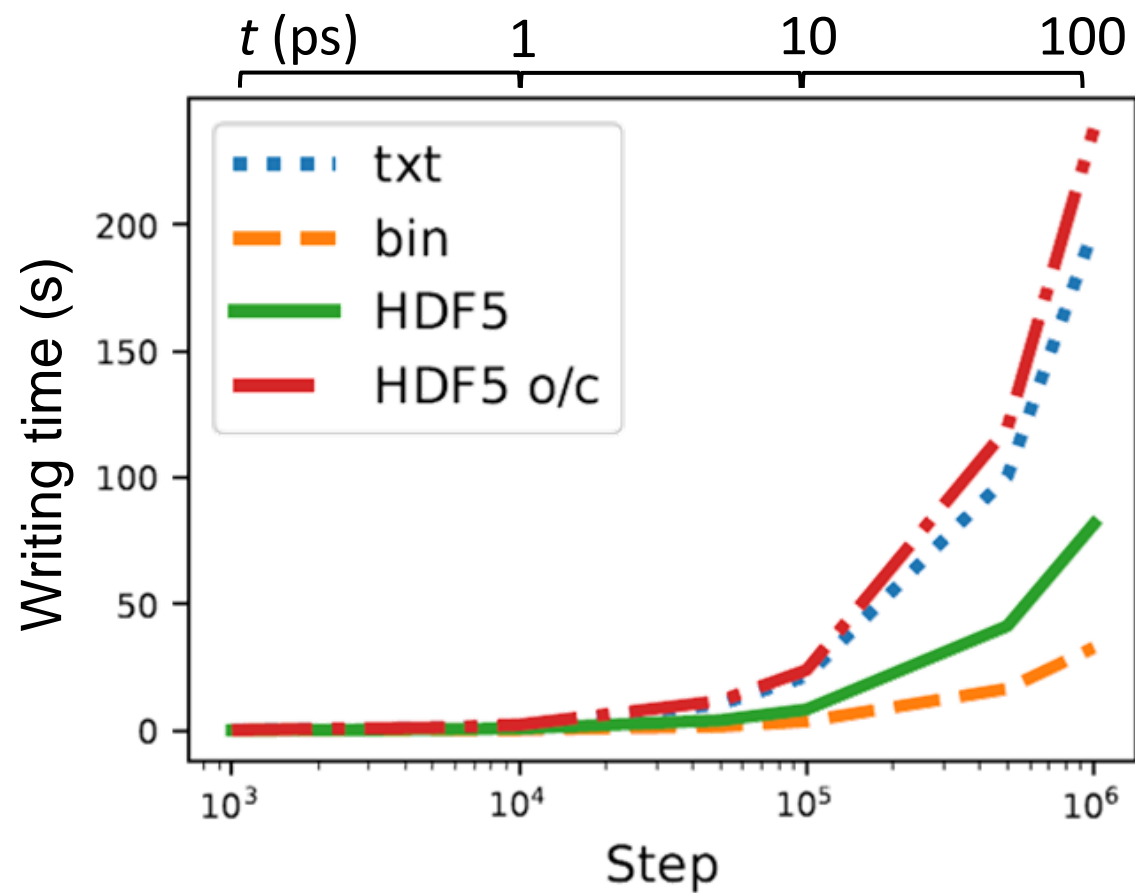


Newton-X  
new series





Newton-X  
new series





Newton-X  
new series

## Open-data compliance

We are developing protocols to guarantee that our simulation results are:

- Searchable (standard format, public repositories)
- Auditable (full dataset available)
- Reproducible (source codes and inputs available)

# What's coming next?

Many nonadiabatic phenomena happen in the long timescale.  
They are inaccessible for current dynamics methods.

Machine learning should be the main driving force for a new generation of methods.

We may expect a publication rush in the field.

We are computing benchmarks, developing methods, proposing protocols, and rewriting Newton-X to face this demand.



**NEWTON-X NS**  
Release in Spring 2022



## **Machine learning and Integration stability:**

Max Pinheiro Jr

## **ZPE corrections and MQCD accuracy:**

Saikat Mukherjee

## **Newton-X NS:**

Baptiste Demoulin



LIGHT AND  
MOLECULES

# Marseille-Xiamen Machine Learning Consortium



**Mario Barbatti**  
Max Pinheiro Jr  
Baptiste Demoulin  
Mithun M



**Pavlo Dral**  
Baixin Xu  
Fuchun Ge  
Lina Zhang  
Yanchi Ou  
Yifan Hou

# SUBNANO



FET OPEN

**BOOST**

**CROP**



**institut  
universitaire  
de France**

LIGHT AND  
MOLECULES

## SciPost Chemistry

[Home](#) [Authoring](#) [Refereeing](#) [Submit a manuscript](#) [About](#)[Latest publications](#)[Accepted Submissions](#)[Most cited](#)[Issues](#)

### Relativistic density-functional theory based on effective quantum electrodynamics

Julien Toulouse

SciPost Chem. 1, 002 (2021) · published 18 May 2021 | [Toggle abstract](#) · [pdf](#)

### The seniority quantum number in Tensor Network States

Klaas Gunst, Dimitri Van Neck, Peter Andreas Limacher, Stijn De Baerdemacker

SciPost Chem. 1, 001 (2021) · published 15 January 2021 | [Toggle abstract](#) · [pdf](#)

Open review  
Open finances  
Diamond Open Access



[www.barbatti.org](http://www.barbatti.org)



[mario.barbatti@univ-amu.fr](mailto:mario.barbatti@univ-amu.fr)



[@MarioBarbatti](https://twitter.com/MarioBarbatti)