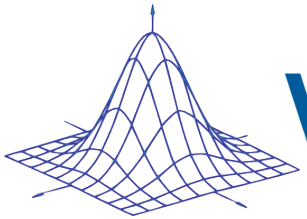
Structural Representations of Materials for Machine Learning using the Novel Materials Discovery Big-Data Analytics Platform

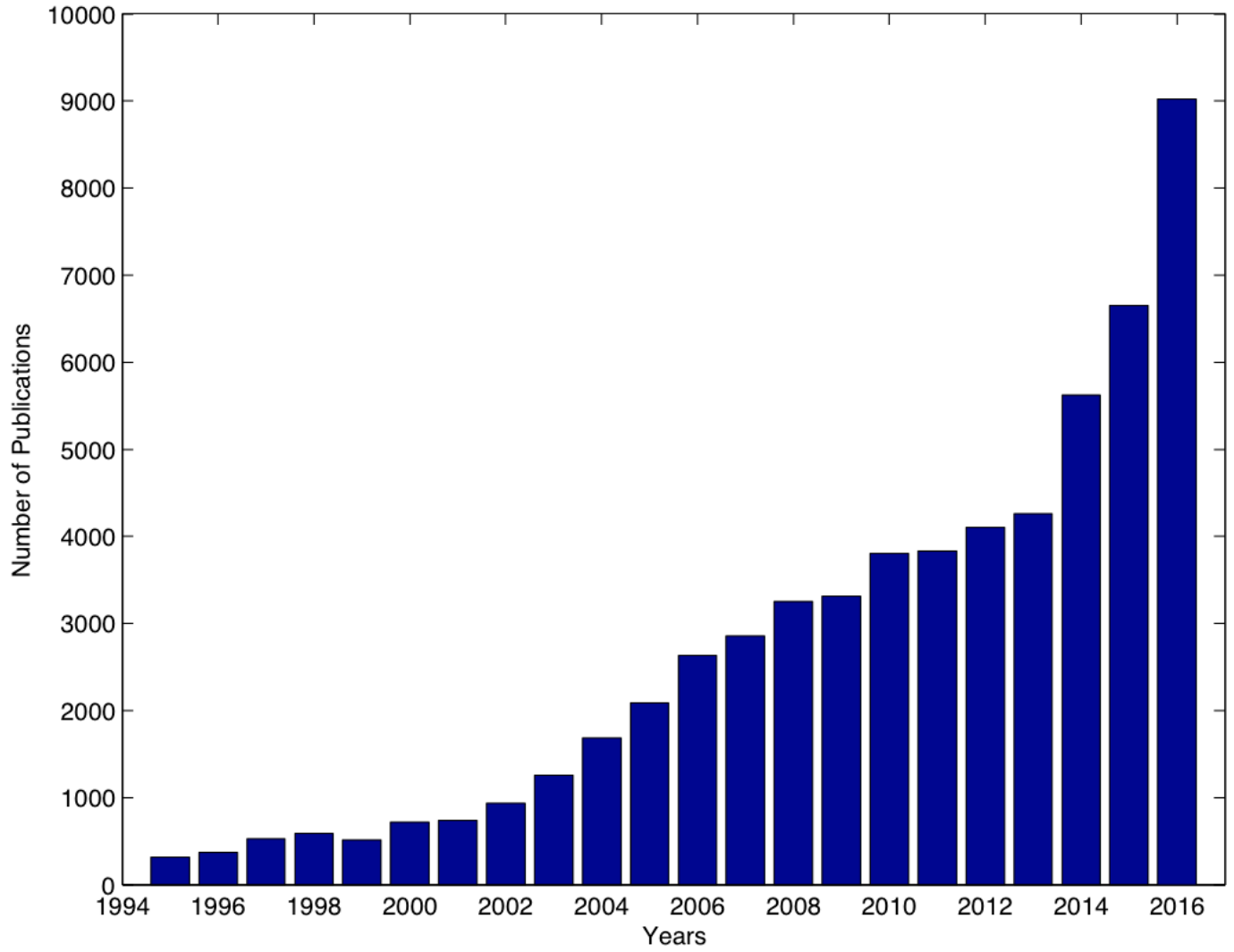
Berk Onat

School of Engineering
University of Warwick



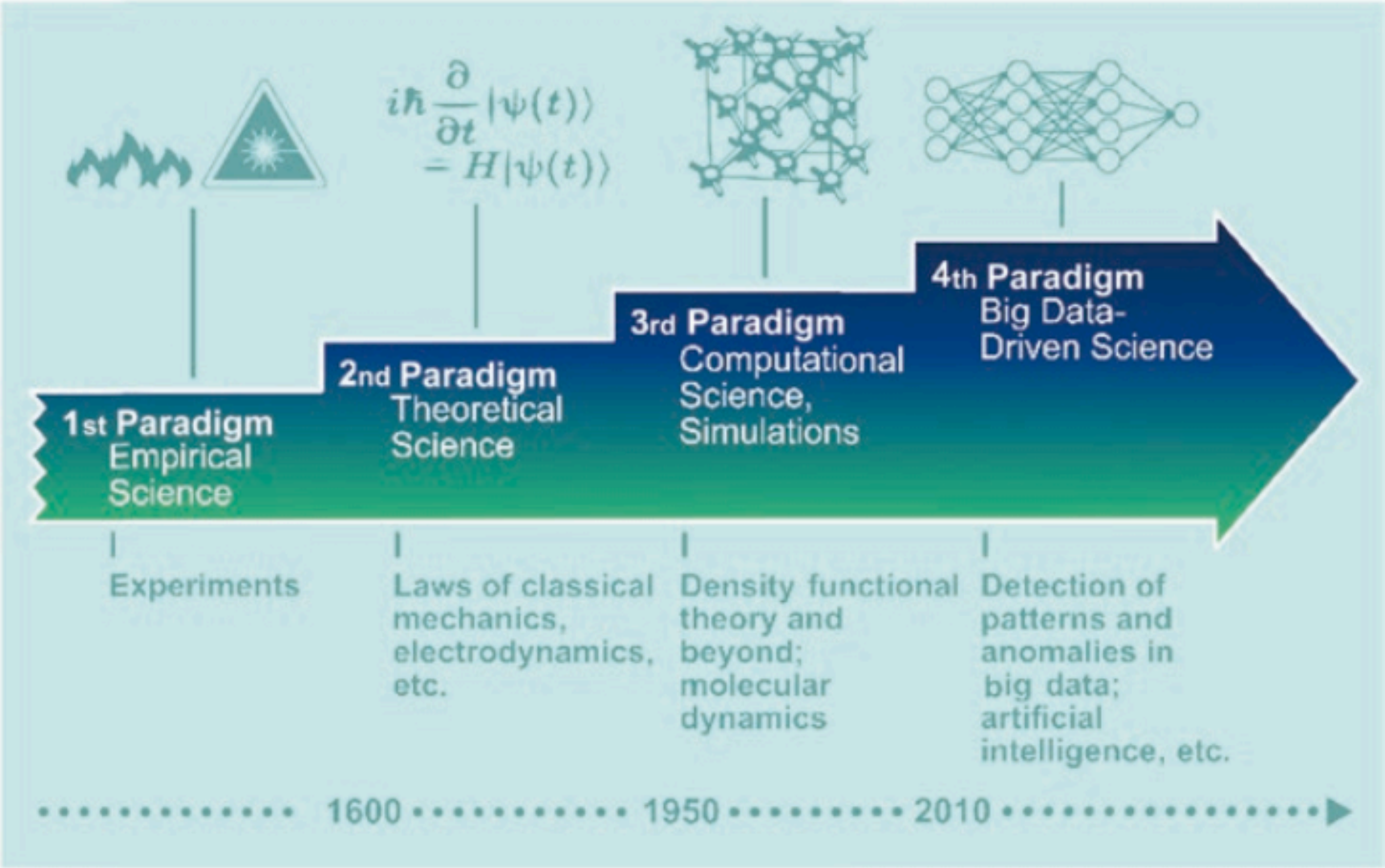
WCPM | Warwick Centre for Predictive Modelling

Why Machine Learning is popular now?



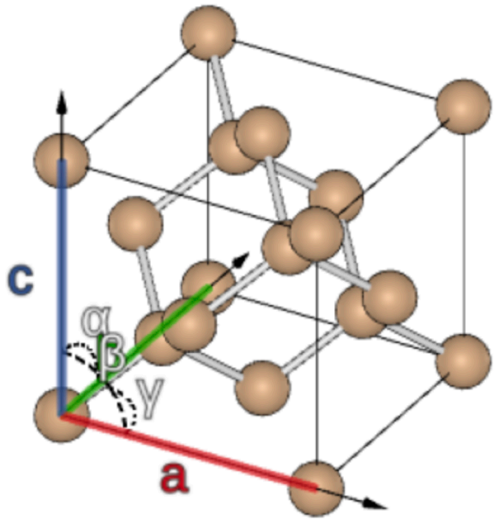
Number of publications per year between 1994 to 2016 (Web of Science)

Paradigms of Material Science and Engineering

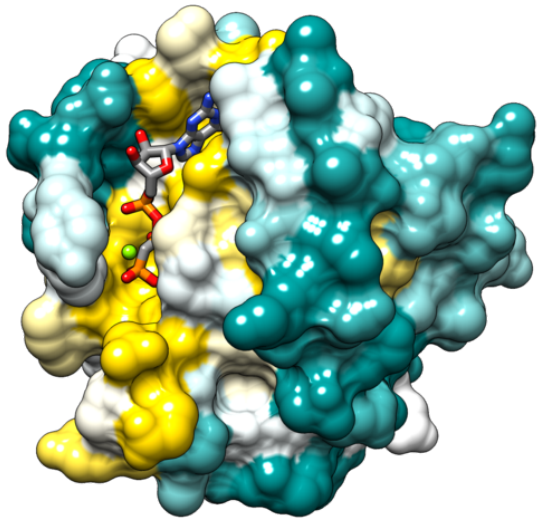


Ref: Claudia Draxl and Matthias Scheffler, “NOMAD: The FAIR concept for big data-driven materials science”, MRS Bulletin, Volume 43, (2018) 676-682.

Big-Data Analytics in Material Science and Engineering



Si Diamond Crystal



HRAS Protein (~7000 Atoms) Ref: Wikipedia / PDB

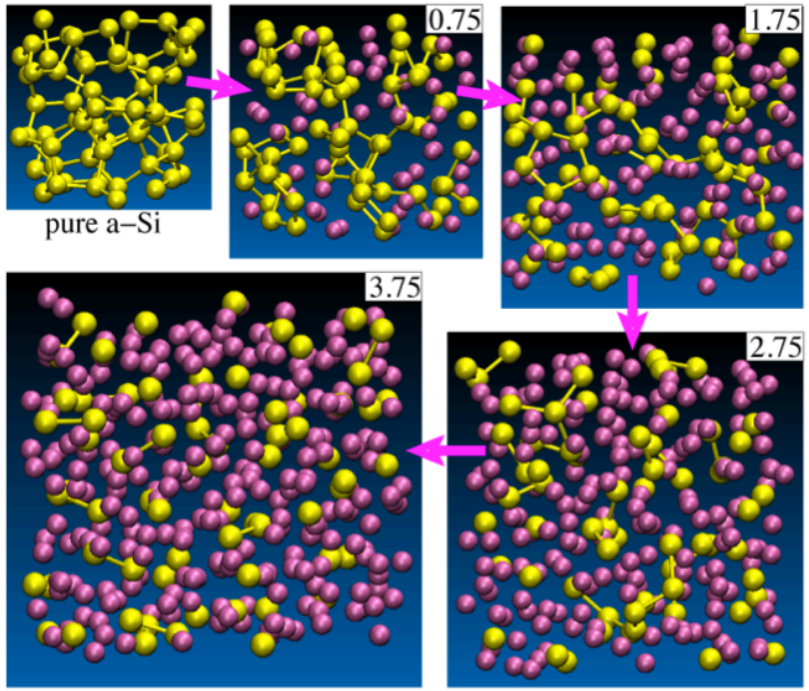
Prediction

Electronic or Structural Properties:

Energies
Forces
Atomic Charges
Magnetization
Band Structure
Band Gap
Density of States
…

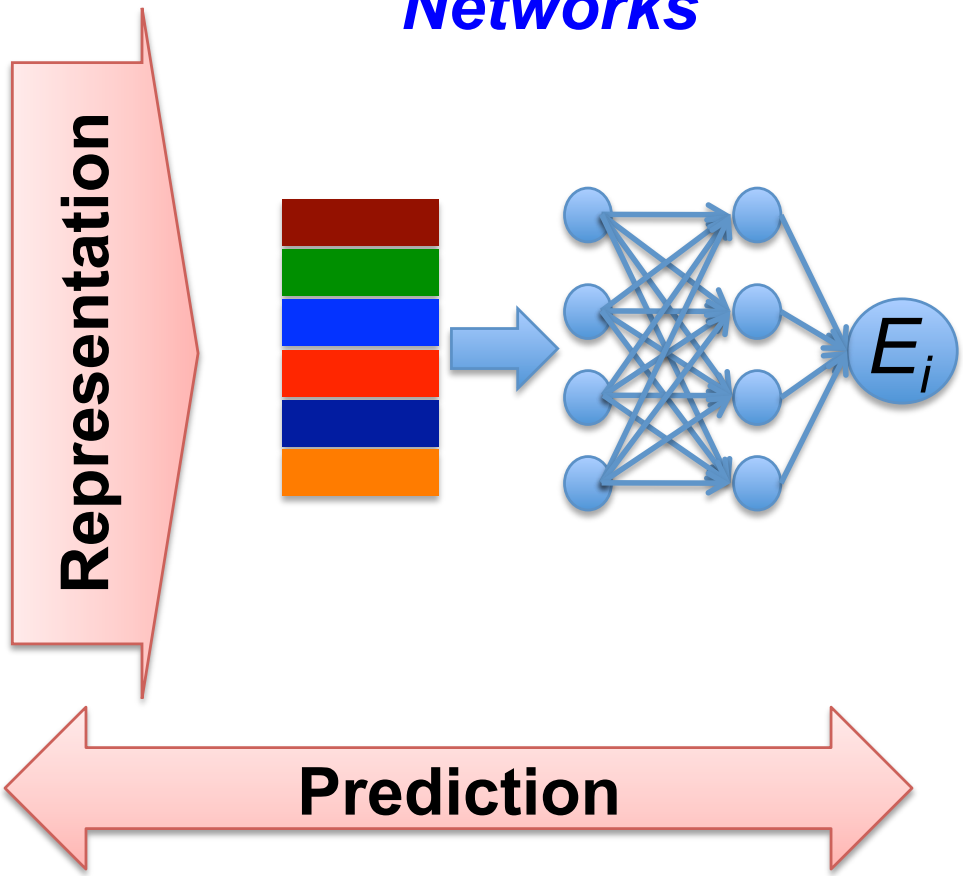
Representation of Potential Energy Surface of Li-Si

Lithiation of Amorphous Si



19000 Structures
SIESTA calculations

Implanted Neural Networks



Ref: Berk Onat, Ekin D. Cubuk, Brad D. Malone, and Efthimios Kaxiras, **PRB 97, 094106 (2018)**

Novel Materials Discovery (NOMAD) Lab

The Novel Materials Discovery (NOMAD) Laboratory maintains the largest Repository, for input and output files of all important
es helping to advance

To learn m
tory CoE at YouTube (

NOMAD

Data is a

Surprisingl
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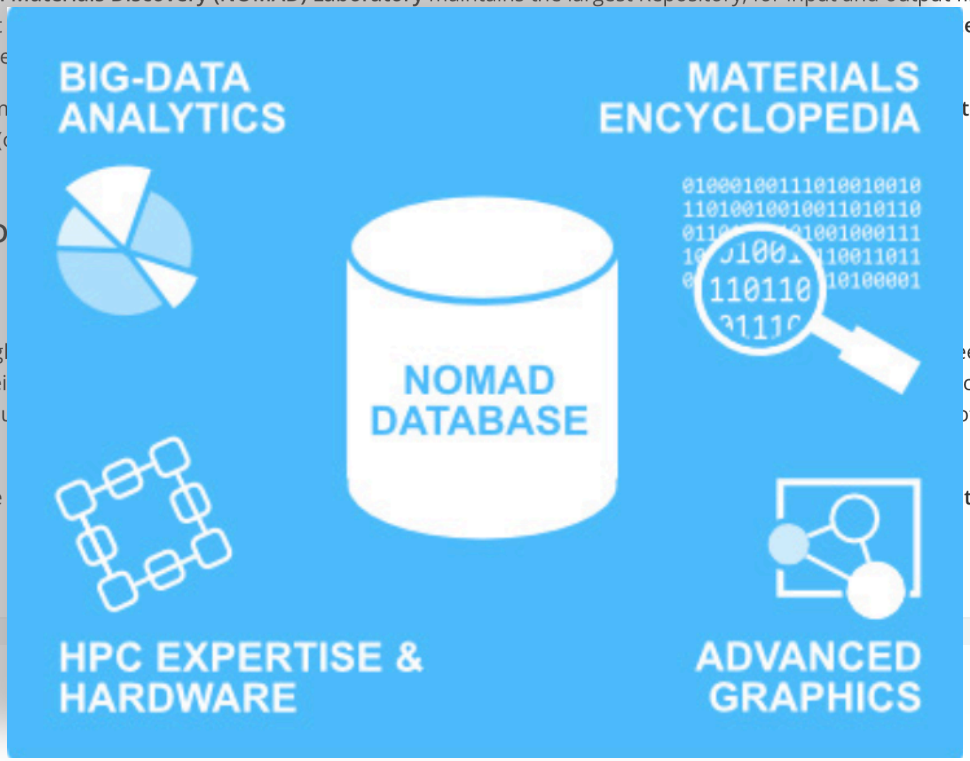
challenges. Clearly, mu
of the results.

This is the
tory .
... more



NOMAD Success Stories

http://www.nomad-coe.eu

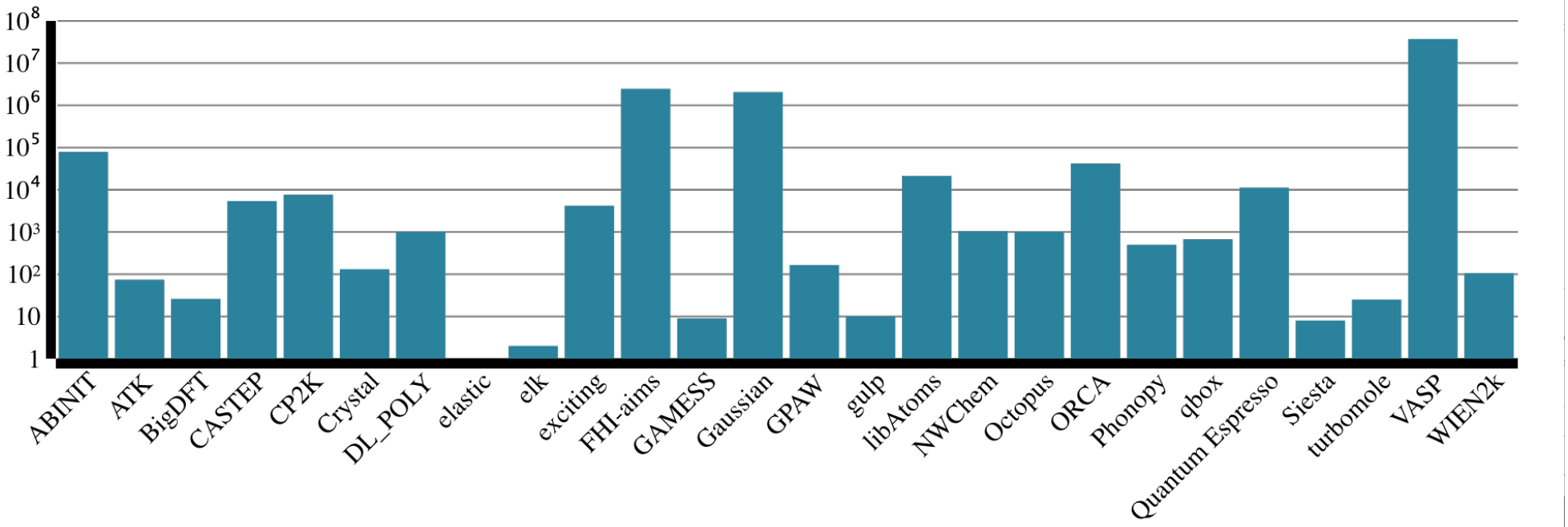
Novel Materials Discovery (NOMAD) Lab

Metric	Value
Total Energy Calculations	50,236,539
Different Geometries	37,376,432
Bulk Crystals	44,993,132
Surfaces	276,704
Molecules/Clusters	4,605,378
Band Structures	1,936,325

NOMAD Archive as of ***March 2018***.

http://www.nomad-coe.eu

Novel Materials Discovery (NOMAD) Lab



Codes with more than 100 uploads to NOMAD Archive as of ***March 2018***.

http://www.nomad-coe.eu

NOMAD Infrastructure

Input/Output of ab-initio and MD codes

NOMAD-LAB Infrastructure (Scala / Python)

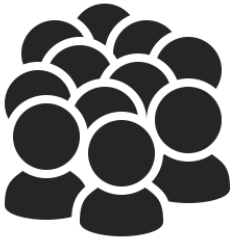
1. **Parsers**
2. **Normalizers**
3. **Metainfo**

Norm.

Metainfo

Parsers

Web
Jupyter/
Beaker
Notebooks



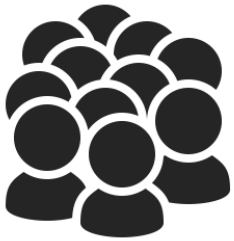
User Access

API
json
hdf5

User Downloads

API

Web
Search
Visualise



User Access

NOMAD Infrastructure

Input/Output of ab-initio and MD codes

Open Access Codes at Gitlab MPCDF

NOMAD-LAB Infrastructure (Scala / Python)

1. Parsers
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Parsers

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json
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Search
Visualise

User Access

NOMAD Parsers

WARWICK

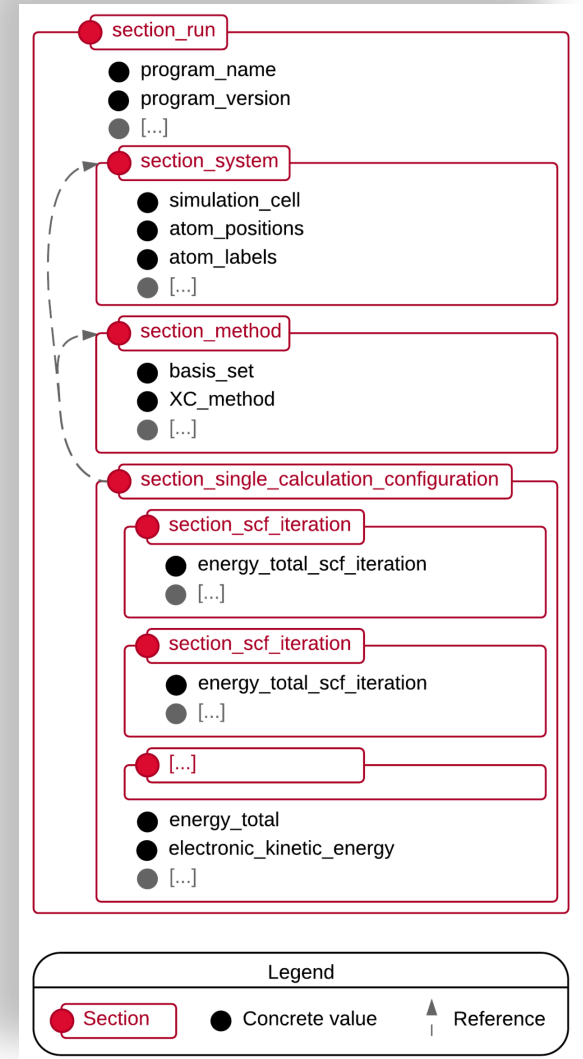
Most cited 15 codes:

Code	Citations (2013-17)	Type	Search Name
Gaussian	19100	DFT	Frisch
VASP	17900	DFT	Kresse
Gromacs	11200	FF	Lindahl
LAMMPS	10300	FF	Plimpton
Amber	9440	FF	Kollman
NAMD	7110	FF	Schulten
GROMOS	7080	FF	Van Gunsteren
Quantum Espresso	6960	DFT	Giannozzi
ASE/ASAP	6650	FF	Jacobsen
CHARMM	6250	FF	Karplus
Discovery Studio	6240	DFT, FF	*Accelyrs*
GAMESS	5780	DFT	Gordon
WIEN2k	5570	DFT	Blaha
CASTEP	5330	DFT	Payne
Molpro	4440	DFT	Werner

Parser codes developed in our group.

Parsers from other groups in NOMAD.

Standard Metadata

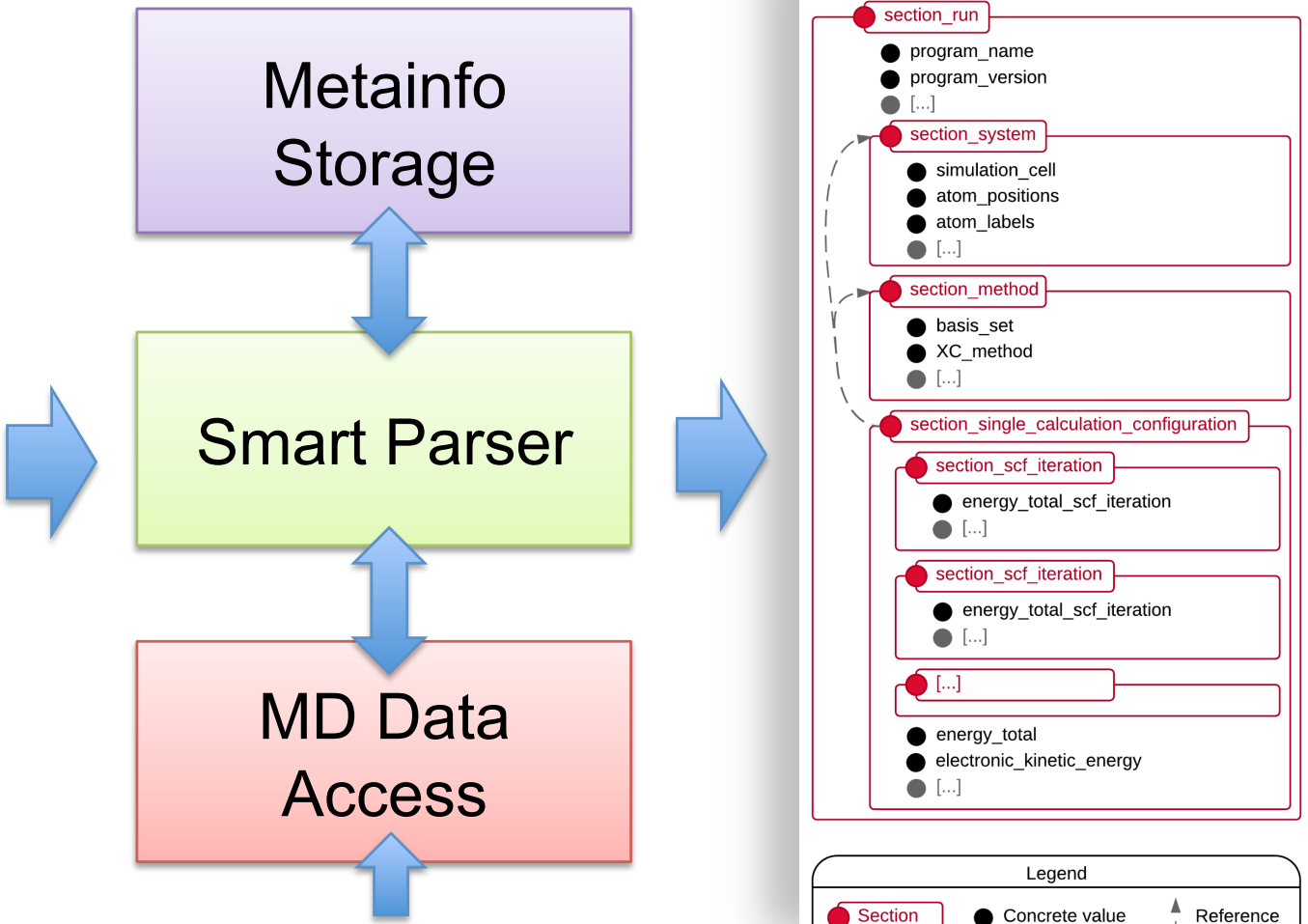


Ref: L.M. Ghiringhelli, C. Carbogno, S. Levchenko, F. Mohamed, G. Huhs, M. Lueders, M. Oliveira, M. Scheffler, arXiv:1607.04738

Metainfo for MD Codes

https://gitlab.mpcdf.mpg.de/nomad-lab/python-common
https://gitlab.mpcdf.mpg.de/nomad-lab/pymolfile

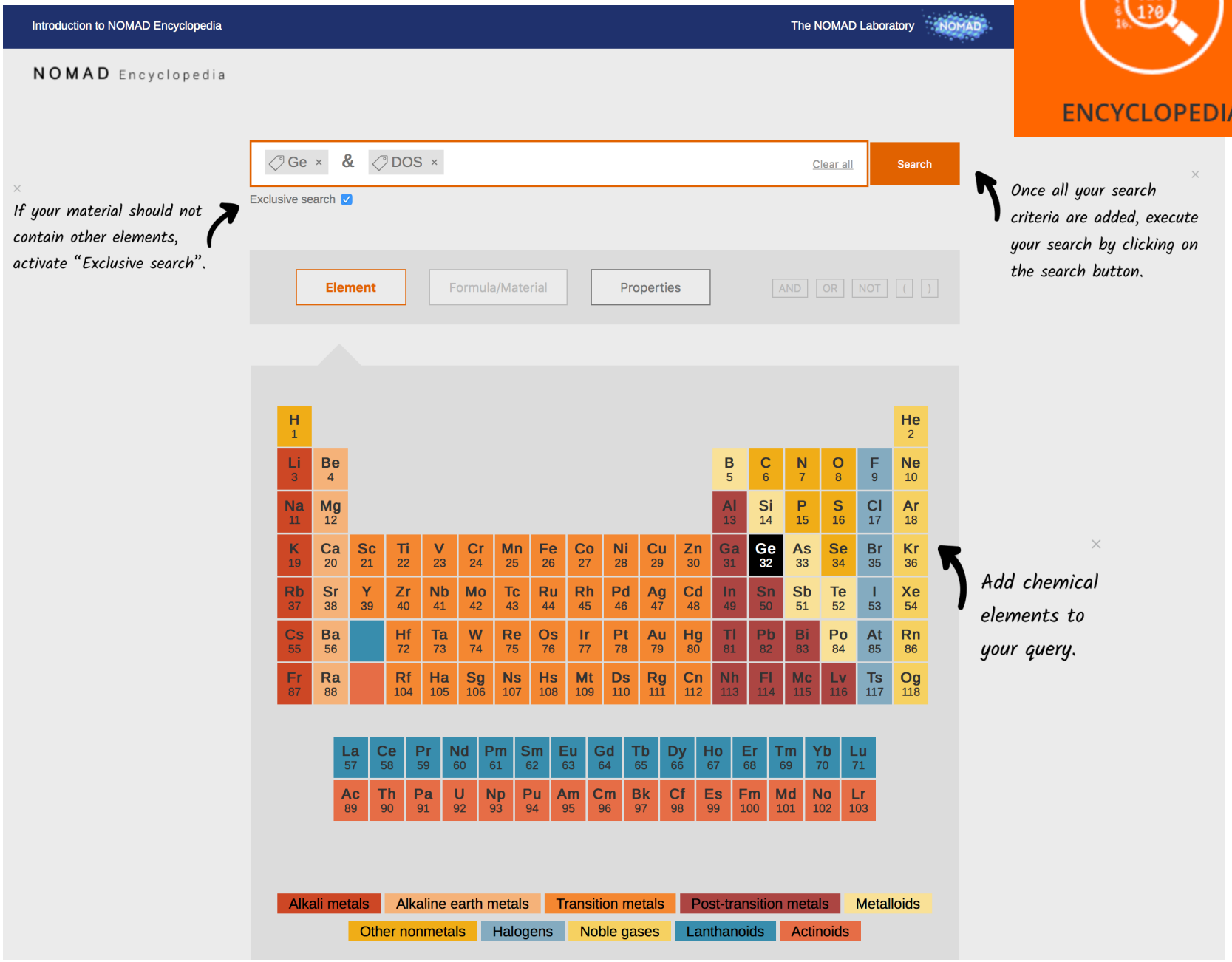
Amber
CHARMM
Gromacs
GROMOS
NAMD
Tinker



Supports ***128*** Topology/Trajectory : Formats

ASE, Mdtraj, MdAnalysis, **ParmEd**, GROMOSTopo, CHARMM_Reader, Pymolfile (VMD plugins)

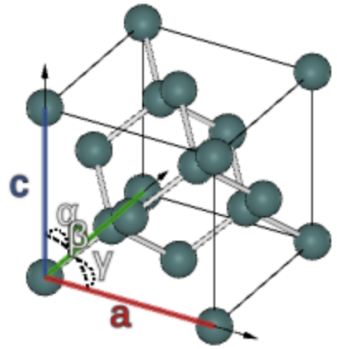
NOMAD Encyclopedia



NOMAD Encyclopedia

Ge - space group 227

Structure



Ge

Show axis Show bonds Virtual Reality files

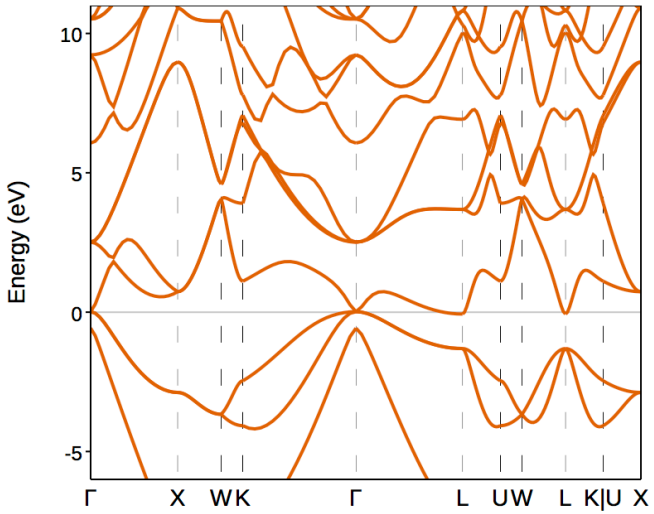
System type: bulk

Space group: 227 (Fd-3m)

Structure type: diamond

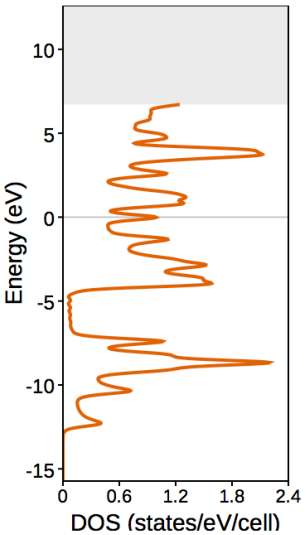
Electronic structure

Band structure



From calculation **26048**
(GGA - VASP)

DOS

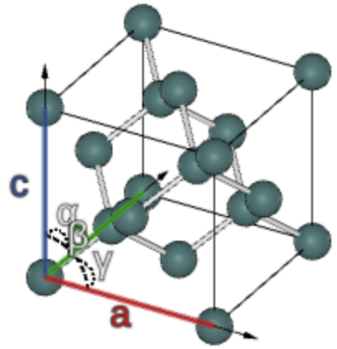


From calculation **26048**
(GGA - VASP)

NOMAD Encyclopedia

Ge - space group 227

Structure



Ge

Show axis Show bonds Virtual Reality files

System type: bulk

Space group: 227 (Fd-3m)

Structure type: diamond

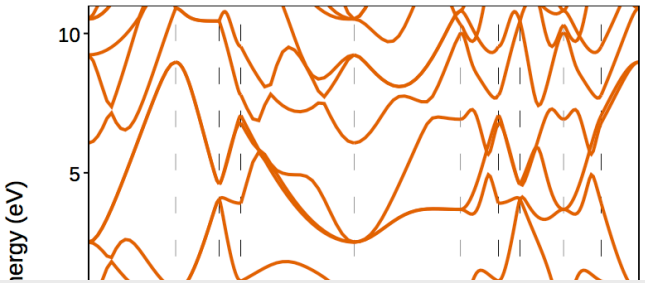
Methodology

Available calculations

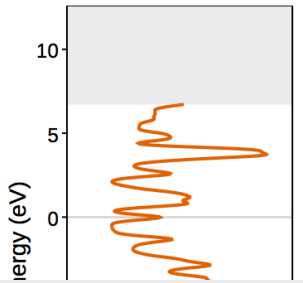
Functional	Code
431 LDA	620 FHI-aims
518 GGA	230 VASP
	78 GPAW
	21 exciting

Electronic structure

Band structure

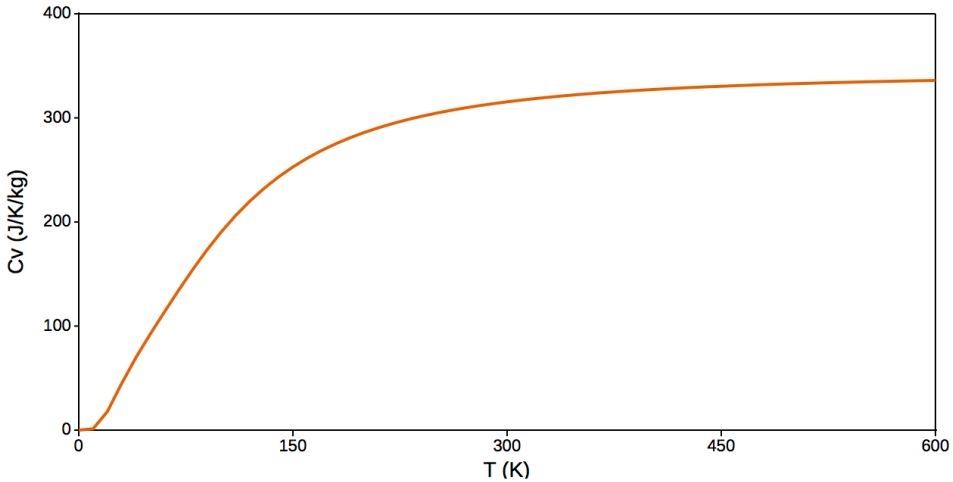


DOS



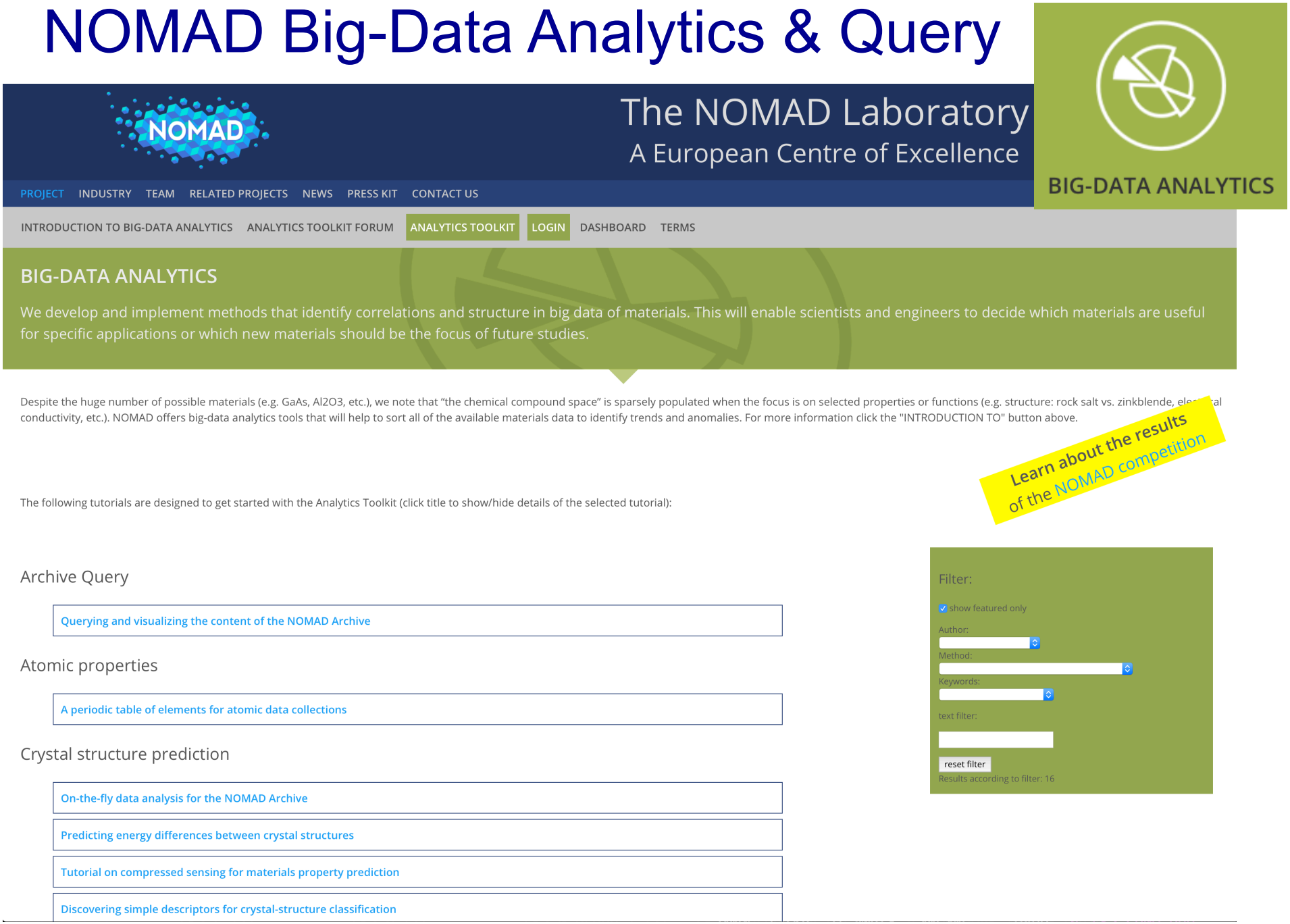
Vibrational and thermal properties

Specific heat

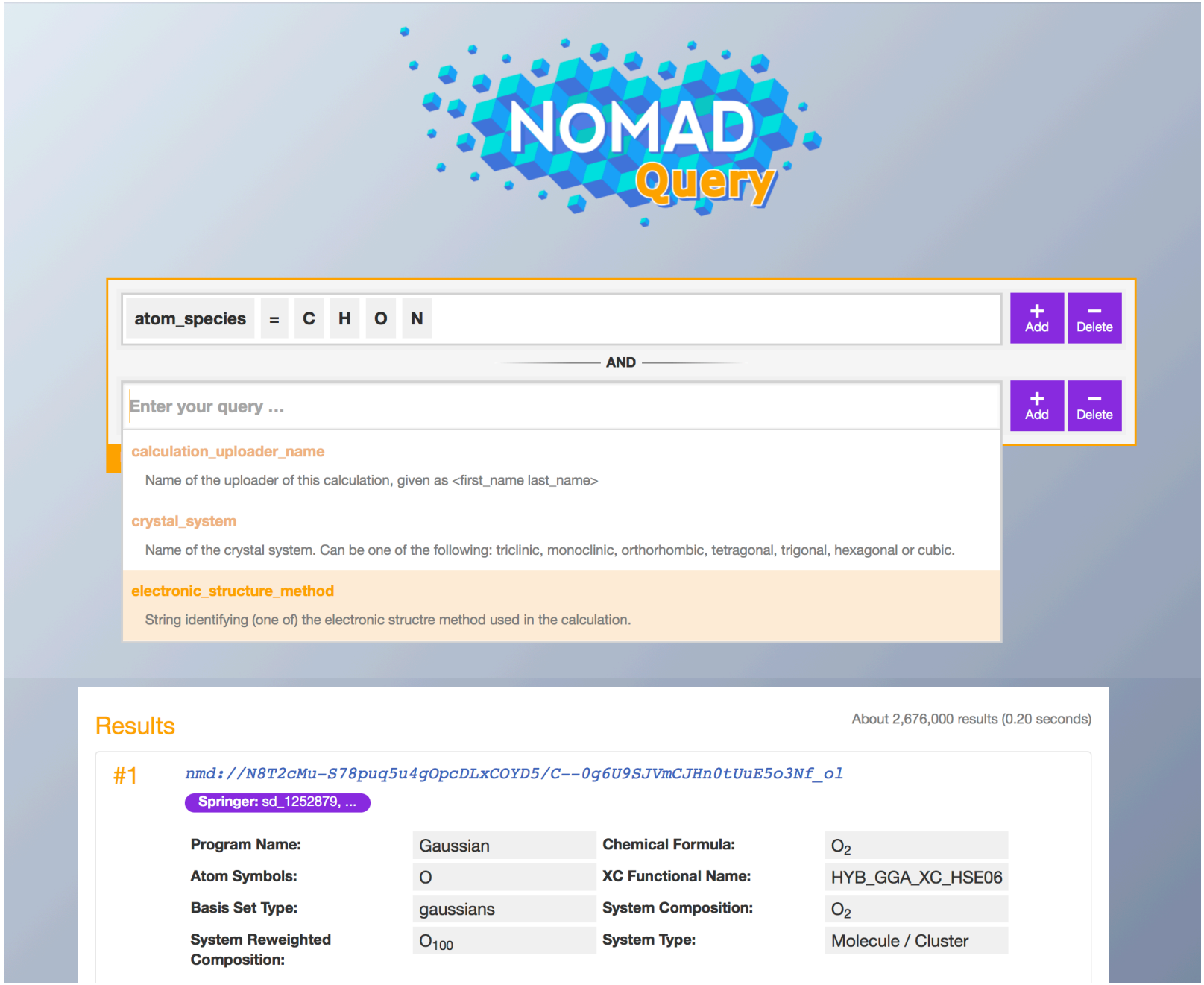


From calculation **1478973** (LDA - FHI-aims)

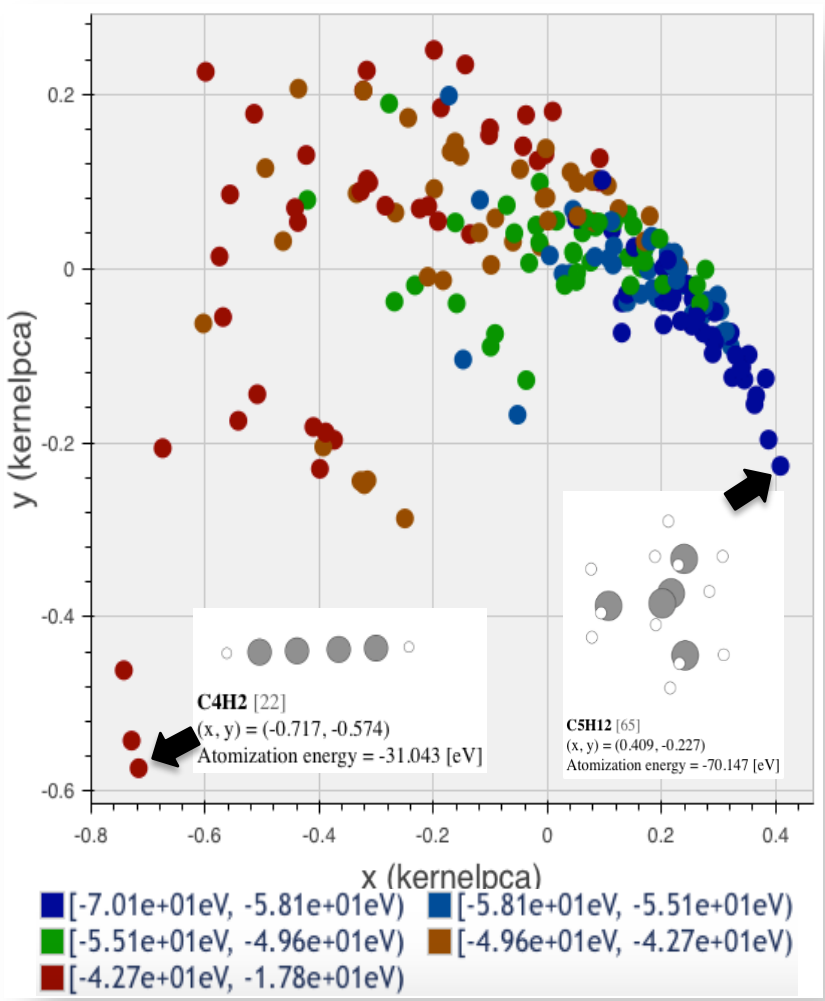
NOMAD Big-Data Analytics & Query



NOMAD Big-Data Archive and Query

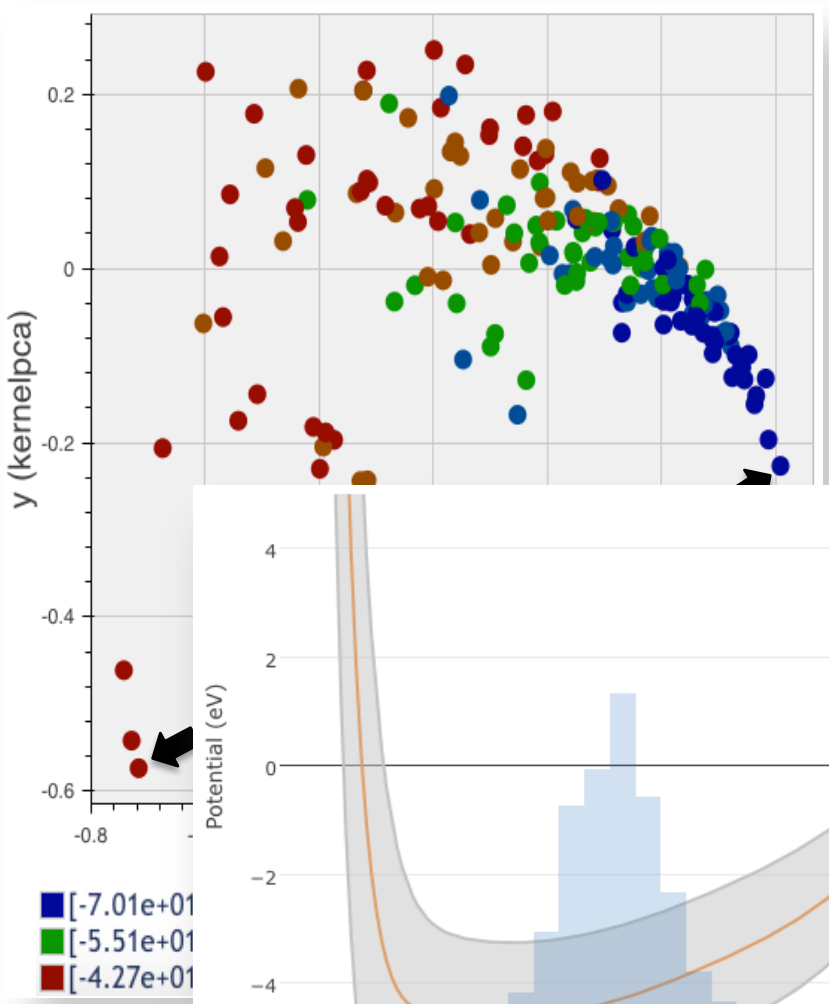


Similarity Map with SOAP Representation



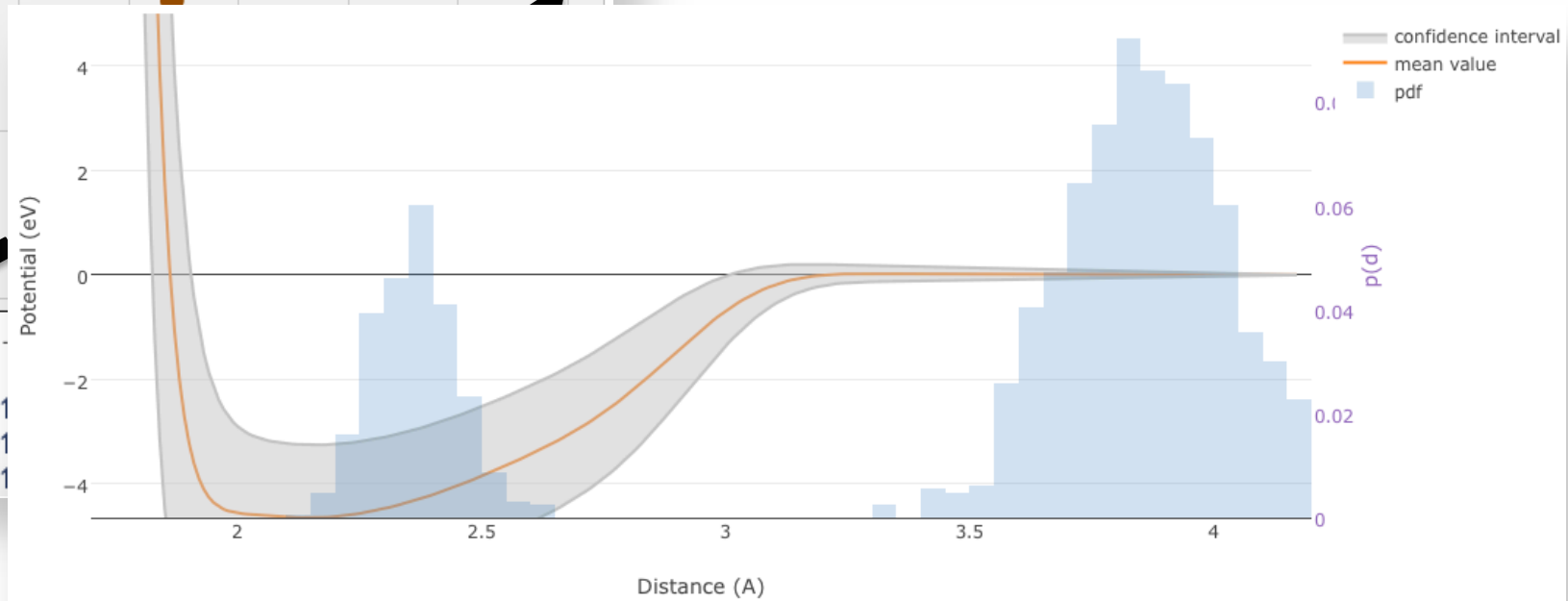
[1] C. Poelking, A. Ziletti, L. Ghiringhelli, and G. Csányi, NOMAD. S. De, A. Bartók, G. Csányi, and M. Ceriotti, Phys. Chem. Chem. Phys. (2016)

Similarity Map with SOAP Representation



[1] C. Poelking, A. Ziletti, L. Ghiringhelli, and G. Csányi, NOMAD.
S. De, A. Bartók, G. Csányi, and M. Ceriotti, Phys. Chem. Chem. Phys. (2016)
[2] Ádám Fekete, Aldo Glielmo, Martina Stella, and Alessandro De Vita, NOMAD Big-Data Analytics

Pair-Potential Predictor for Si



Classification of Representations

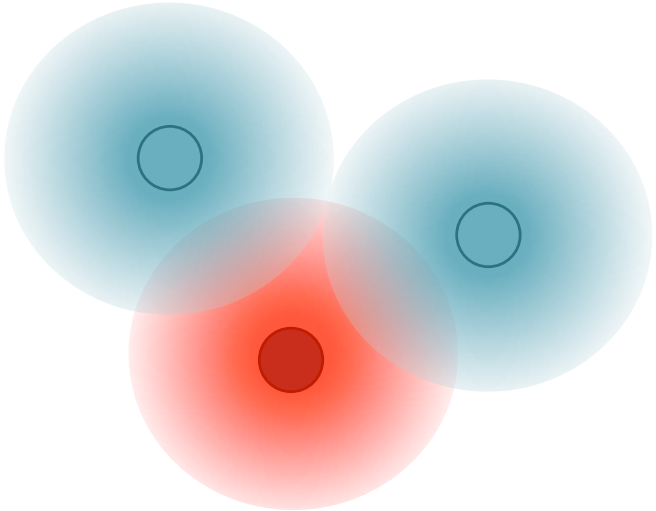
Atomic neighbor density			Histogram		Connectivity (Graphs)		Physical Property
Symmetry Adapted		Direct	Direct		Direct		Direct
Kernel/ Power expens ion	Functions/ Filters	Expensio n/Tensor	Structure	Electronic	Static Builds	Hierarchical Builds	Combinati on of any property with any math. operation
SOAP	Sym. Funcs, Chebyshev expansion, AGNI	MBTR	k-bags, Bag of Bonds/ Angles …	Electroni c Band Structure , DOS	n-gram, Graphs, CGCNN ,Coulom b Matrix	Building blocks or Ligand/ Residue based Graphs	SISSO

Ref: Berk Onat, James Kermode (2018) ***under preparation***

Smooth Overlap of Atomic Positions (SOAP)

$$\rho_{\mathscr{X}}(\mathbf{r}) = \sum_{i \in \mathscr{X}} \exp\left(-\frac{(\mathbf{x}_i - \mathbf{r})^2}{2\sigma^2}\right)$$

$$\tilde{k}(\mathscr{X}, \mathscr{X}') = \int \mathrm{d}\hat{R} \left| \int \rho_{\mathscr{X}}(\mathbf{r}) \rho_{\mathscr{X}'}(\hat{R}\mathbf{r}) \mathrm{d}\mathbf{r} \right|^n$$



Power Expansion:

$$\rho_{\mathscr{X}}(\mathbf{r}) = \sum_{blm} c_{blm} g_b(|\mathbf{r}|) Y_{lm}(\hat{\mathbf{r}})$$

$$p(\mathscr{X})_{b_1 b_2 l} = \pi \sqrt{\frac{8}{2l+1}} \sum_m \left(c_{b_1 lm}\right)^\dagger c_{b_2 lm}$$

SOAP Kernel:

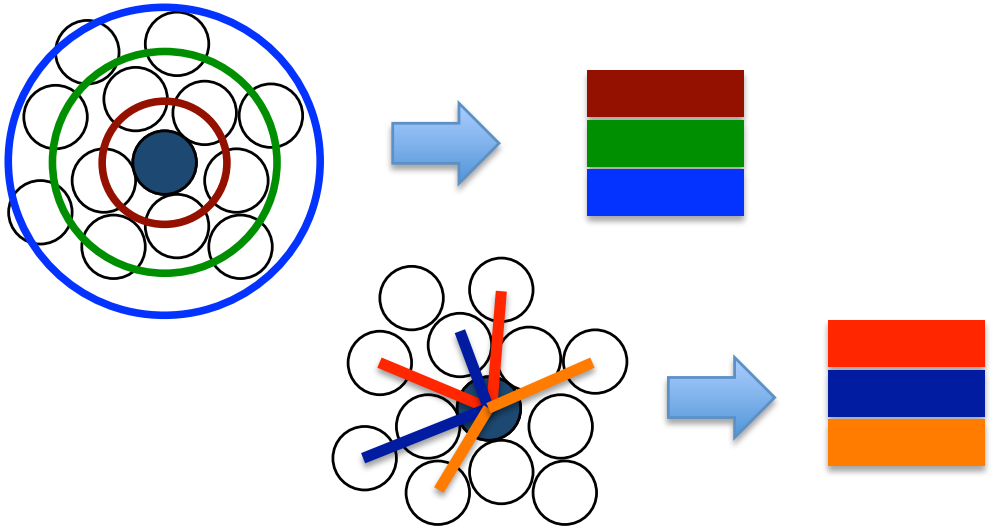
$$k(\mathscr{X}, \mathscr{X}') = \hat{\mathbf{p}}(\mathscr{X}) \cdot \hat{\mathbf{p}}(\mathscr{X}')$$

Ref: **A. P. Bartok, R. Kondor and G. Csanyi, PRB 87, 184115, (2013)**
A. P. Bartok, G. Csanyi, Int. J. Quantum Chemistry 115, 1051–1057, (2015)

Symmetry Functions

Radial Symmetry Functions:

$$G_2^i = \sum_j e^{-\eta(R_{ij}-R_s)^2} \cdot f_c(R_{ij}),$$

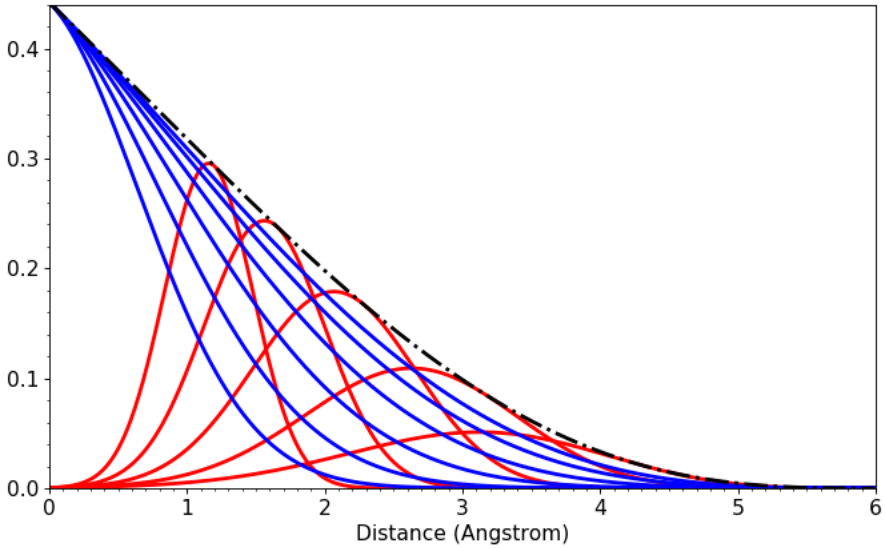


Angular Symmetry Functions:

$$G_3^i = 2^{1-\zeta} \sum_j \sum_{k \neq j} (1 + \lambda \cdot \cos\theta_{ijk})^\zeta$$
$$\cdot e^{-\eta(R_{ij}^2+R_{ik}^2+R_{jk}^2)} \cdot f_c(R_{ij}) f_c(R_{ik}) f_c(R_{jk}),$$

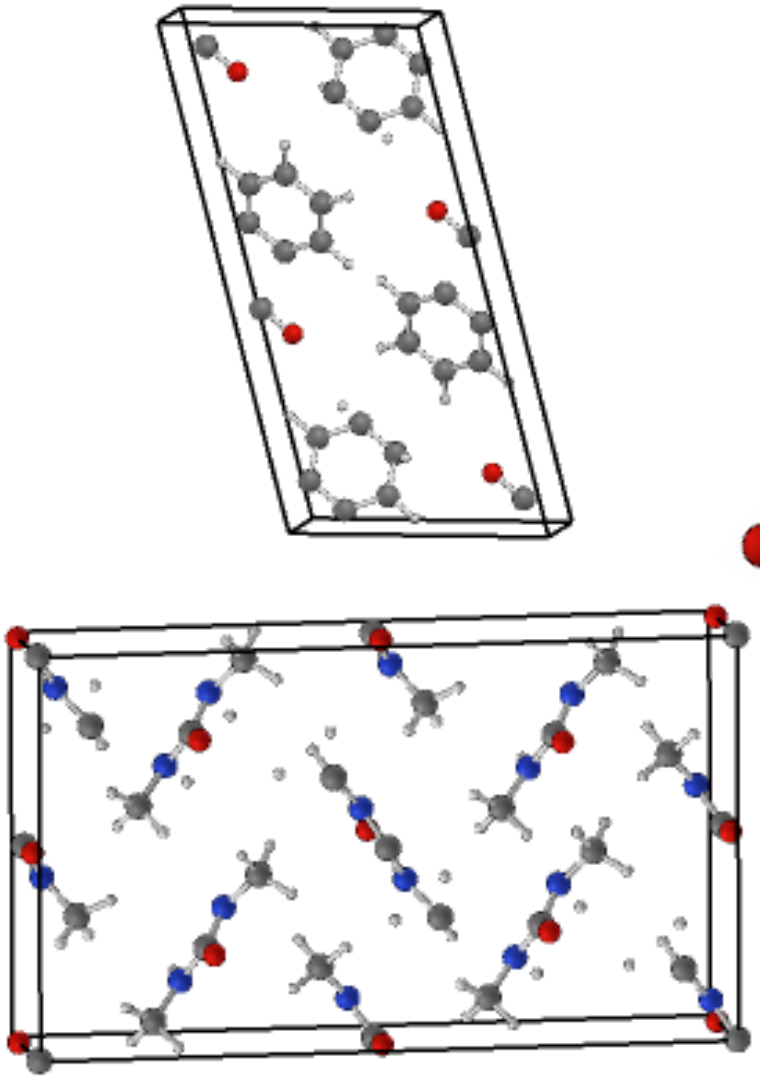
Cutoff function:

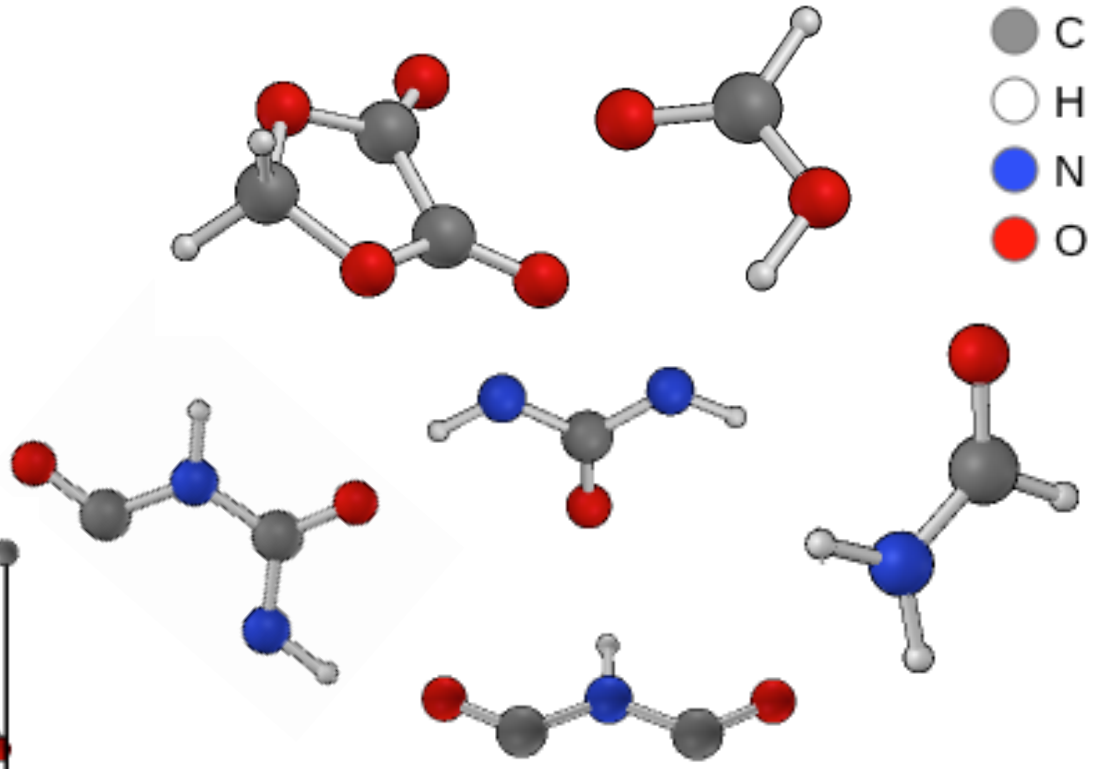
$$f_c(R_{ij}) = \begin{cases} \tanh^3\left[1 - \frac{R_{ij}}{r_c}\right] & \text{for } R_{ij} \leq r_c \\ 0.0 & \text{for } R_{ij} > r_c \end{cases}$$



Ref: **N. Artrith, B. Hiller and J. Behler, Physica Status Solidi B, 250, 1191 (2013)**
G. Imbalzano, A. Anelli, D. Giofré, S. Klees, J. Behler, M. Ceriotti, J Chem. Phys 148, 241730 (2018)

Compressibility Tests with CUR and FPS Methods on C,H,N,O Structures





2963 Molecular Structures
(Single Molecules, Bulk Molecular Structures)

CUR Decomposition

$$\mathbf{X} \approx \tilde{\mathbf{X}} = \mathbf{C}\,\mathbf{U}\,\mathbf{R},$$

Selecting Columns of X:

1) **SVD Decomposition**
2) **Column scoring with right singular vector *v***

$$\pi_c = \sum_{j=1}^{k} (v_c^{(j)})^2,$$

3) ***Select c from k columns (Here we apply CUR[k=1])***
4) **Orthogonalize all other columns of X to *c***

$$\mathbf{R} = \mathbf{X},$$
$$\mathbf{U} = \mathbf{C}^{+}\mathbf{X}\mathbf{X}^{+},$$

Error estimation:

$$\epsilon = \|\mathbf{X} - \mathbf{C}\mathbf{U}\mathbf{R}\|_F \,/\, \|\mathbf{X}\|_F$$

Ref: G. Imbalzano, A. Anelli, D. Giofré, S. Klees, J. Behler, M. Ceriotti, J Chem. Phys 148, 241730 (2018)

Farthest Point Sampling (FPS)

Selecting Columns of X:

1) **Select first column randomly**
2) **Select *N* columns according to**

$$k = \text{argmax}(\min_j |X_k - X_j|),$$

3) **Build C matrix using the selected columns**

$$\mathbf{R} = \mathbf{X},$$
$$\mathbf{U} = \mathbf{C}^{+}\mathbf{X}\mathbf{X}^{+},$$

Error estimation:

$$\epsilon = \|\mathbf{X} - \mathbf{CUR}\|_F \,/\, \|\mathbf{X}\|_F$$

Ref: G. Imbalzano, A. Anelli, D. Giofré, S. Klees, J. Behler, M. Ceriotti, J Chem. Phys 148, 241730 (2018)

Horizon 2020

NOMAD: Novel Materials Discovery

http://www.nomad-coe.eu

WARWICK

Dr. Berk Onat

Research Fellow

Dr. James R. Kermode

Associate Professor

WCPM

Warwick Centre of Predictive Modelling

WARWICK

NOMAD Collaborators

Acknowledgement

This work is supported in part by **NOMAD Project** and **University of Warwick**.

NOMAD project has received funding from the **European Union's Horizon 2020** research and innovation programme under grant agreement No. 676580.

Horizon 2020