$B \to D\bar{D}h$ decays: a new (virtual) laboratory for exotic particle searches

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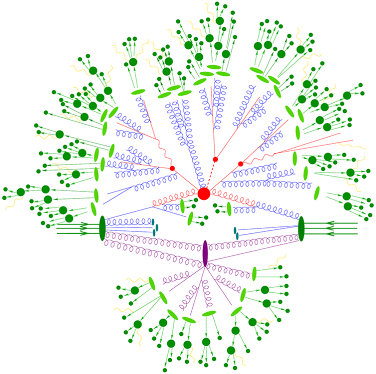
Outline

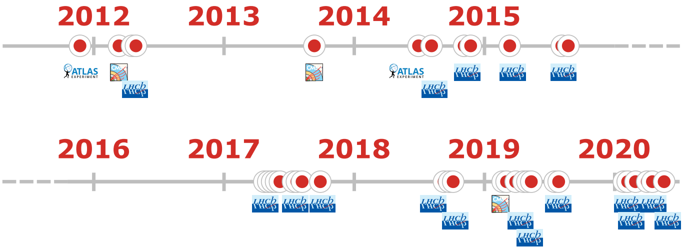
1. Introduction
2. Datasets
3. Model-independent analysis [arXiv:2009.00025], PRL accepted
4. Amplitude analysis [arXiv:2009.00026], PRD accepted
5. Reaction
6. Conclusion

The mystery of hadronisation



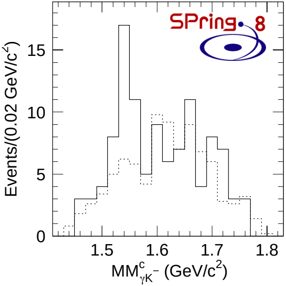
- QCD: successful and predictive. Perturbative at hard scales
- Hadronisation models in lieu of analytical solutions
- Least-well understood aspect of the SM. How to improve?

The allure of spectroscopy



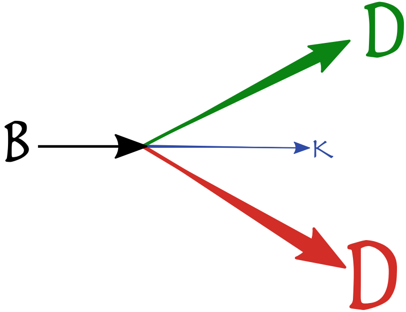
- The LHC brought a wealth of new particles: 37 new hadrons
- Great deal of attention: 1,398 citations
- Crucial inputs for hadronisation model-builders

Beware the pentaquark...

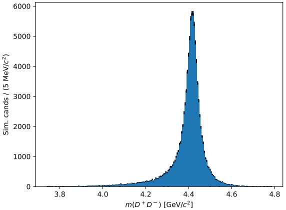


- *uudds̄* state predicted in 1997 arXiv:hep-ph/9703373
- Excess seen in 2003 arXiv:hep-ex/0301020
- Bumps 'confirmed' by 9 other experiments
- Un-discovered by CLAS, Belle, . . .

The power of exclusive reconstruction



- Fully reconstructed decay
- Much more than a bump-hunt
- Toy $B^+ \to [\psi(4415) \to D^+ D^-] K^+$

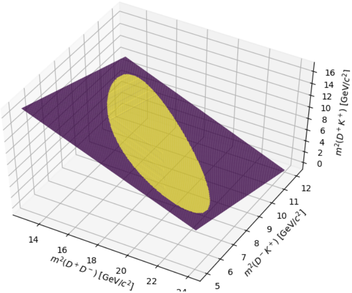


The power of exclusive reconstruction

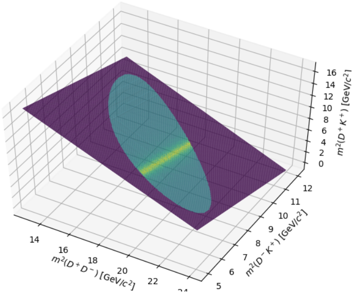
- Conservation of four-momentum in the decay:

$$m_B^2 + 2m_D^2 + m_K^2 = m_{D^+D^-}^2 + m_{D^-K^+}^2 + m_{D^+K^+}^2$$

Toy: phase-space



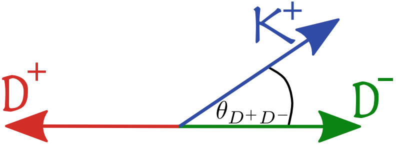
Toy: spin-0



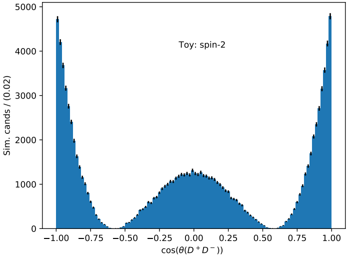
- Two degrees of freedom, within kinematic limits
- Intermediate resonances produce non-uniform structure

The power of exclusive reconstruction

- Strong $P \longrightarrow 3P$ decay: resonances have $J^P = 0^+, 1^-, 2^+, \ldots$
- Resonance spin dictates angular structure



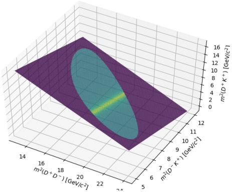
- Resonance (e.g. 2^+) decaying to D^+D^-: intuitive $\theta_{D^+D^-}$ shape



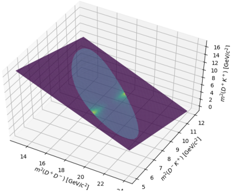
The power of exclusive reconstruction

- Spin-dependent helicity-angle maps onto phase-space plane

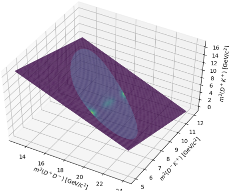
Toy: spin-0



Toy: spin-1



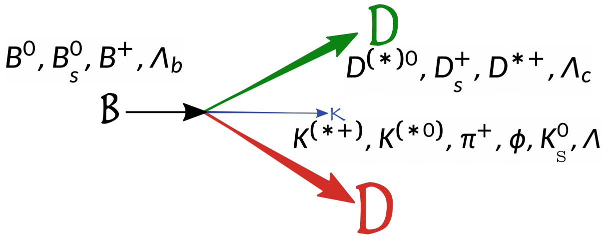
Toy: spin-2



- We'll always project onto one pair of these axes: 'Dalitz plot'

Why $B \to D\bar{D}h$ decays?

- Huge family of topologically similar decays

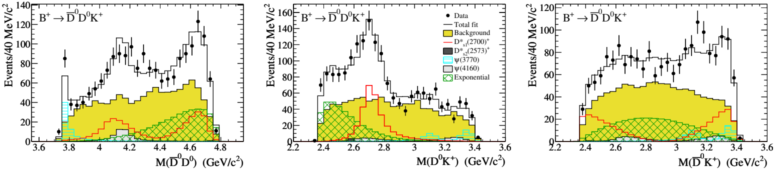


- Wide range of spectroscopy studies
  - Charmonia (e.g. D^+D^-)
  - D_{sJ} spectroscopy (e.g. D^0K^+)
  - Manifestly exotic channels (e.g. D^0D^- $[c\bar{c}?]$; D^+K^- $[c\bar{d}\bar{u}s]$)
- Resonances little-studied
- LHCb data of unprecedented size/purity

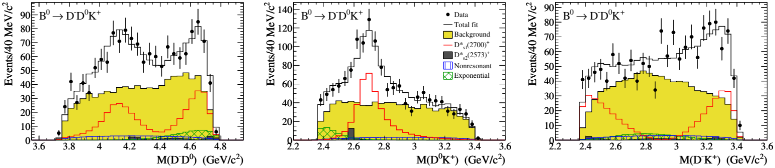
A new laboratory for spectroscopy

- $B \to D^{(*)} D^{(*)} X$ branching fractions well-studied 2005.10264,2007.04280
- Amplitude analysis exists for only two decays 0707.3491, 1412.6751
  - 400-2000 candidates, but purity 40% at best

BaBar: $B^{\pm} \to D^0 \bar{D}^0 K^{\pm}$ 1412.6751



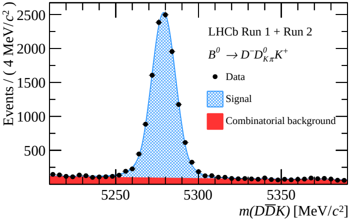
BaBar: $B^0 \to D^- D^0 K^+$ 1412.6751



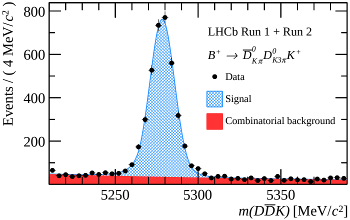
An unprecedented dataset

- LHCb has:
  - high-statistics: order of magnitude improvement
  - high-purity: order of magnitude reduction in background
- (see recent LHCb branching fraction measurement: 2005.10264)

$B^0 \longrightarrow D^- D^0 K^+$



$B^+ \longrightarrow \bar{D}^0 D^0_{K3\pi} K^+$



A simple study?

- $B^\pm \to D^+ D^- K^\pm$ interesting for charmonia; conventional resonances only expected in the $D^+ D^-$ channel
- (even illuminating $c\bar{c}$ in $B^\pm \to \mu^+ \mu^- K^\pm$ decays 1006.4945,1406.0566?)
- Amplitude analysis should be an 'easy' study of charmonia...

Surprising phase-space structure!

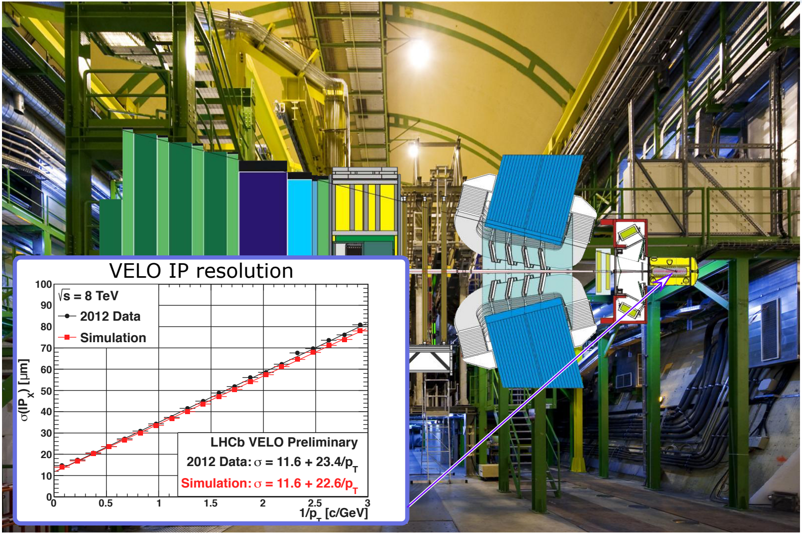
- LHCb-PAPER-2020-024: model-independent study of resonant structure in $B^+ \to D^+ D^- K^+$ decays
- LHCb-PAPER-2020-025: amplitude analysis of the $B^+ \to D^+ D^- K^+$ decay

Outline

LHCb detector

1412.6352

LHCb detector



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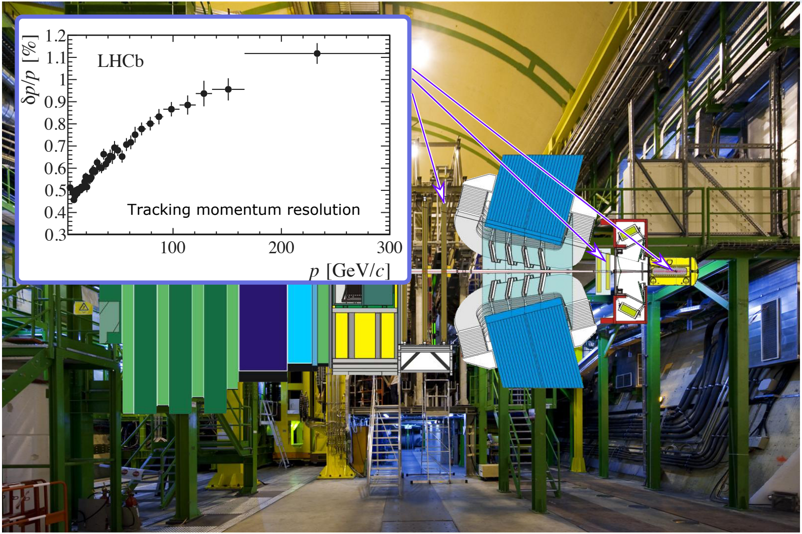
LHCb detector



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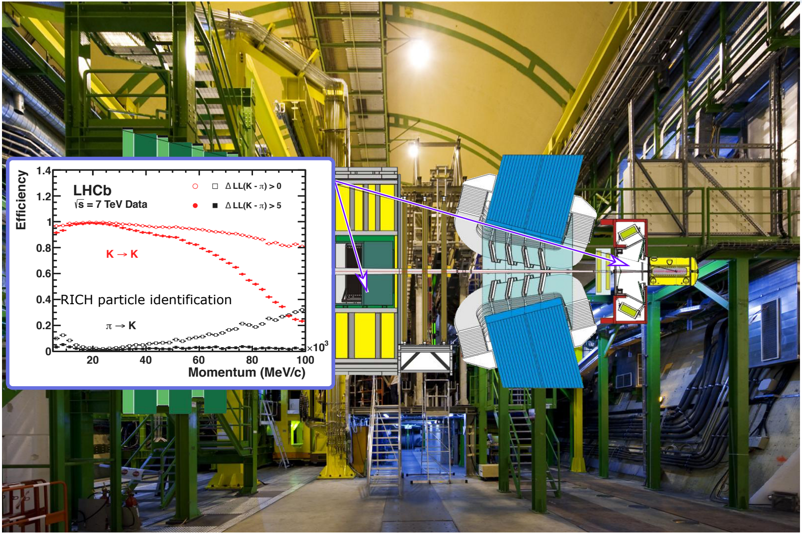
LHCb detector



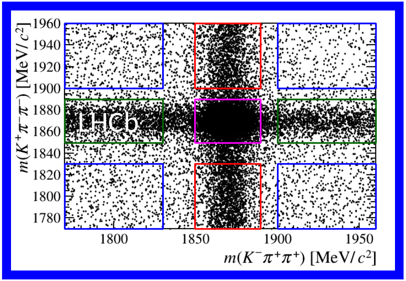
1412.6352

Sample preparation

- Full Run 1 + Run 2 pp datasets ($9\ \text{fb}^{-1}$)
- Reconstruct $B^+ \to [K^-\pi^+\pi^+]_{D^+}[K^+\pi^-\pi^-]_{D^-}K^+$
- Trigger for candidates:
  - $\frac{2}{3}$ satisfy hadron trigger requirements directly
  - $\frac{1}{3}$ from events where something else fires the h, μ, e, γ trigger
- UniformBDT 1305.7248 with topological and PID variables
- Optimise `significance × purity`

Specific backgrounds

- Suppress peaking backgrounds producing the same final state:
  - Veto sharp inv. mass peaks for disconnected pairs of f.s. particles
  - Inspect $B^{\pm}$ peak in D^{+} and D^{-} sidebands, and cut on $D^{\pm}$ FD



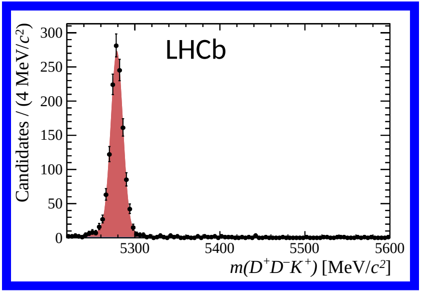
Charmless

Single charm

- Negligible residual peaking background
- No dangerous partially-reconstructed backgrounds

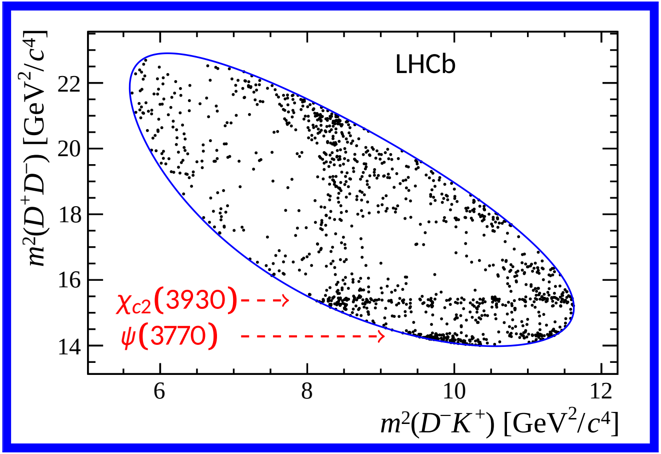
Determining signal yield

- Simultaneous, extended, max-$\mathscr{L}$ fit; Sig. shape guided by MC
- Combine all years:

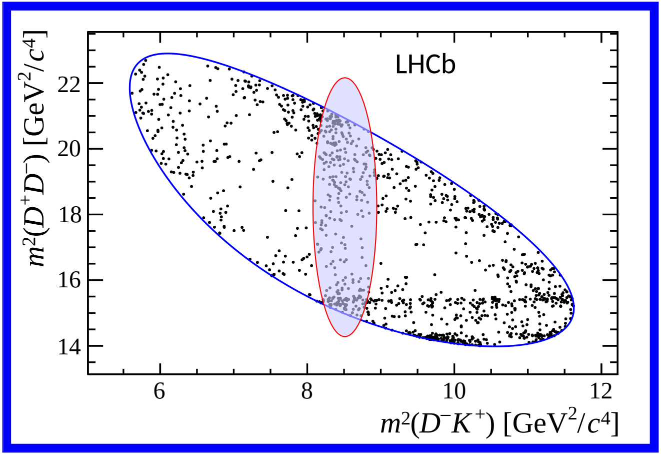


- 1,374 candidates enter the fit; 1,260 within 20 MeV/c^2 of $m(B^\pm)$
- Purity $> 99.5\%$

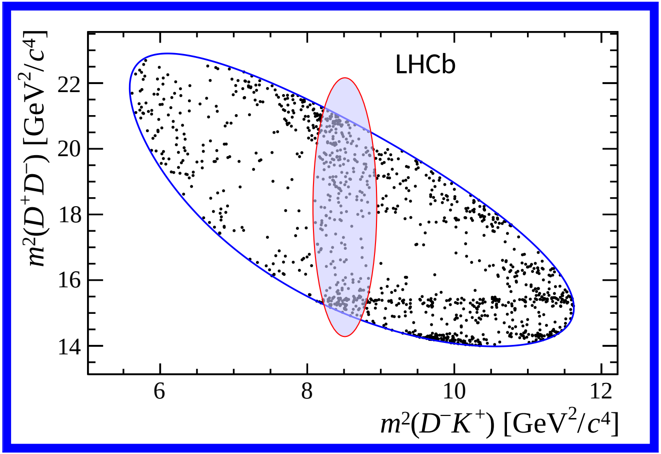
Sneak-peak: the phasespace structure



Sneak-peak: the phasespace structure



Sneak-peak: the phasespace structure



What is that???

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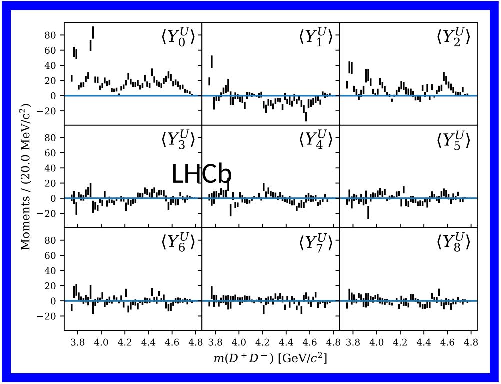
Model-independent analysis approach

- Can $D^+D^-K^+$ phsp be described by D^+D^- partial-waves only?
- Resonances only expected in a single channel: 'simple'
- Method used in $B^0 \to \psi(2S)K^+\pi^-$ 1510.01951, $B^0 \to J/\psi K^+\pi^-$ 1901.05745, $\Lambda_b \to J/\psi pK^-$ 1604.05708, CERN-THESIS-2016-086.

Procedure

1. Capture D^+D^- angular structure using orthonormal basis of Legendre polynomials in $h(D^+D^-) = \cos(\theta(D^+D^-))$:

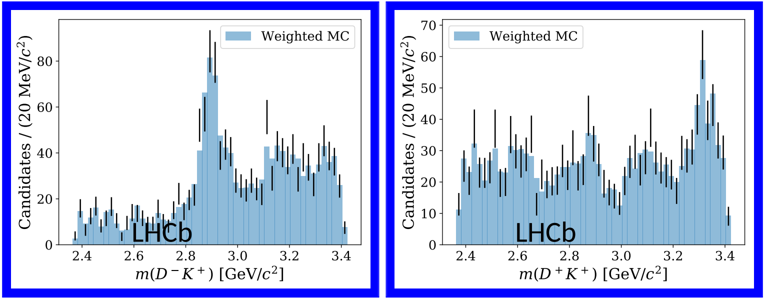
$$\langle Y_k^{U,j} \rangle = \sum_{l=1}^{N_j^{\mathrm{Data}}} w_l P_k \left(h_l(D^+D^-) \right) \tag{1}$$



Procedure

2. Apply weights to MC to visualise resulting $m(D^+K^-)$ shape:

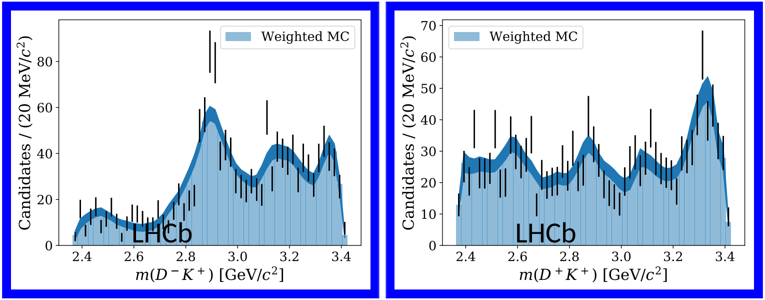
$$\eta_i = \frac{2}{N_j^{\mathrm{Sim}}} \times \sum_{k=0}^{k_{\max}} \langle Y_k^{U,j} \rangle P_k\left(h(D^+D^-)\right) \qquad (2)$$



- Obviously high $k_{\max}$ allows to describe nearly everything

Procedure

3. Truncate the expansion: up to spin-2 $\longrightarrow$ up to $k_{\mathrm{max}} = 4$:

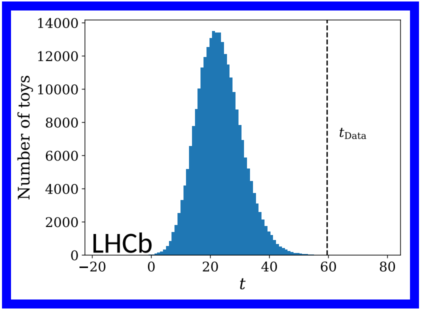


- Bootstrap to propagate uncertainty on moments $\langle Y_k^{U,j} \rangle$
- Clear problem describing the D^+K^- spectrum

Procedure

4. Construct PDF in $m(D^+K^-)$ to build a test-statistic:

$$t = -2 \sum_{l=1}^{N^{\mathrm{Data}}} s_l \log \left(\frac{\mathscr{P}\left(m_l(D^-K^+)|H_0\right)/I_{H_0}}{\mathscr{P}\left(m_l(D^-K^+)|H_1\right)/I_{H_1}} \right) \quad (3)$$



- Ensemble of toys using $k_{\mathrm{max}} = 4$; bootstrap efficiency models
- Evaluate t. t_{Data} discrepant at level of 3.9σ

Outline

Formalism

Used the Laura++ Dalitz plot fitter 1711.09854 to maximise

$$\mathscr{L} = \exp\left[-\sum_{c}\left(\frac{(p_c-\mu_c)^2}{2\sigma_c^2}\right)\right]\prod_{j=1}^{N_c}\left(N_{\rm sig}\mathscr{P}_{\rm sig}(\vec{x}_j)+N_{\rm bg}\mathscr{P}_{\rm bg}(\vec{x}_j)\right)$$

with signal PDF,

$$\mathscr{P}_{\rm sig}(\vec{x}) = \frac{1}{\mathscr{N}}\times\epsilon_{\rm total}(\vec{x})\times|\mathscr{A}_{\rm sig}(\vec{x})|^2$$

and isobar construction for signal amplitude:

$$\mathscr{A}_{\rm sig}(\vec{x}) = \sum_{j=1}^{N} c_j F_j(\vec{x})$$

Formalism

For a resonance in the $D^+ D^-$ channel, the amplitude is

$$F(\vec{x}) = R\left(m(D^+ D^-)\right) \times T(\vec{p}, \vec{q}) \times X(|\vec{p}|) \times X(|\vec{q}|)\,, \tag{4}$$

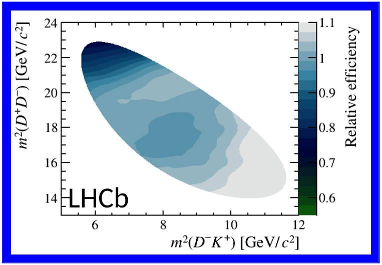
- R: relativistic Breit-Wigner for all resonances
- T: angular factor - non-relativistic Zemach tensor formalism
- X: Blatt-Weisskopf barrier factors

Efficiency variations

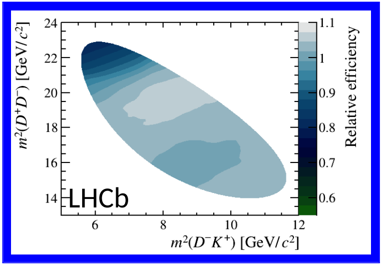
$$\epsilon_{\text{total}}(\vec{x}) = \epsilon_{\text{offline|reco}}(\vec{x}) \times \epsilon_{\text{reco|trig}}(\vec{x}) \times \epsilon_{\text{trig|geom}}(\vec{x}) \times \epsilon_{\text{geom}}(\vec{x})\,.$$

- Main variations at trigger, reconstruction, and stripping stages
- Uniform BDT achieves flat acceptance, as expected

Run 1



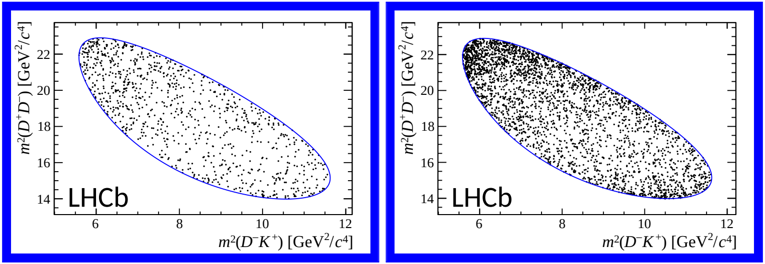
Run 2



Tiny background component

- Use $5.35\,\mathrm{GeV}/c^2 < m(D^+D^-K^+) < 5.69\,\mathrm{GeV}/c^2$, relaxing BDT
- Dalitz plots in the sidebands:

Run 1 Run 2



Signal model ingredients (1/2)

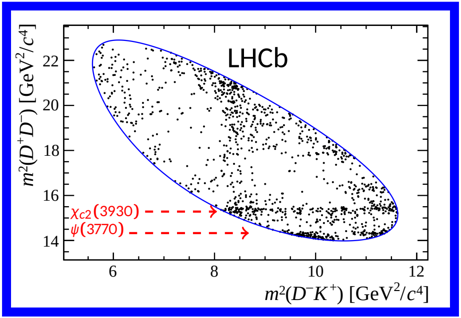
Expect natural J^P (→pseudoscalars) and suppressed high-spin

Partial wave (J^{PC})	Resonance	Mass (MeV/c^2)	Width (MeV/c^2)
S wave (0^{++})	$\chi_{c0}(3860)$	3862 ± 39	201 ± 139
	$X(3915)$	3918.4 ± 1.9	20 ± 5
	Possible nonresonant contributions		
P wave (1^{--})	$\psi(3770)$	3778.1 ± 0.9	27.2 ± 1.0
	$\psi(4040)$	4039 ± 1	80 ± 10
	$\psi(4160)$	4191 ± 5	70 ± 10
	$\psi(4260)$	4230 ± 8	55 ± 19
	$\psi(4415)$	4421 ± 4	62 ± 20
D wave (2^{++})	$\chi_{c2}(3930)$	3921.9 ± 0.6	36.6 ± 2.1
F wave (3^{--})	$X(3842)$	$3842.71 \pm 0.16 \pm 0.12$	$2.79 \pm 0.51 \pm 0.35$

- Most values taken from PDG
- $m(\psi(3770))$ and $\{m, \sigma\}(\chi_{c2}(3930), X(3842))$ from 1903.12240

Fit procedure

- Refit decay, constraining $B^{\pm}$ & $D^{\pm}$ masses: $\sigma(D^+D^-)$ improves from $\mathcal{O}(10\,\mathrm{MeV}/c^2)$ to $\mathcal{O}(2\,\mathrm{MeV}/c^2)$: neglect resolution
- Fit Run 1 and Run 2 data simultaneously, with separate efficiency, bg models and purity
- Minimisation repeated 100 times, randomising coefficients
- $\chi^2/ndof_{\mathrm{effective}}$ computed with adaptive binning scheme

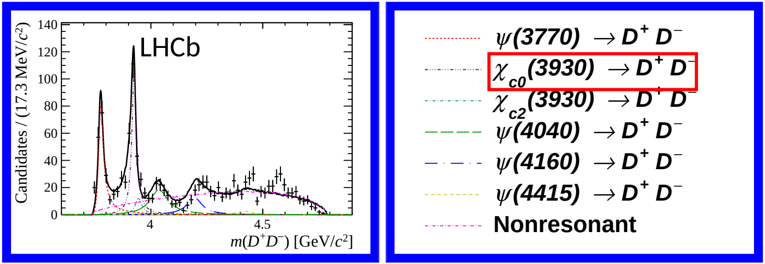


Fit procedure

- Always include $\psi(3770)$ and $\chi_{c2}(3930)$: clearly visible
- Further components included if significantly reduce NLL
- Complex coefficients vary for all except $\psi(3770)$
- Vary m & σ; constrain $\psi(3770)/\psi(4040)/\psi(4160)/\psi(4415)$
- Better fit adding '$\chi_{c0}(3930)$'; no constraint on $\chi_{cJ}(3930)$ m, σ
- Tried various nonresonant lineshapes (uniform, exponential, polynomial, cubic spline) with spin-0,1

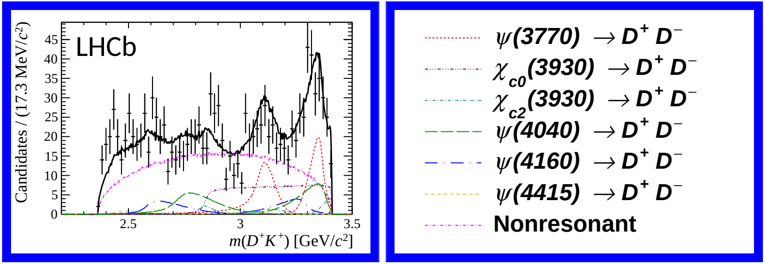
Model excluding D^-K^+ resonances

- $\psi(3770)$, $\chi_{c0}(3930)$, $\chi_{c2}(3930)$, $\psi(4040)$, $\psi(4160)$, and $\psi(4415)$ resonances
- Nonresonant best described by an exponential S-wave lineshape in the D^-K^+ spectrum



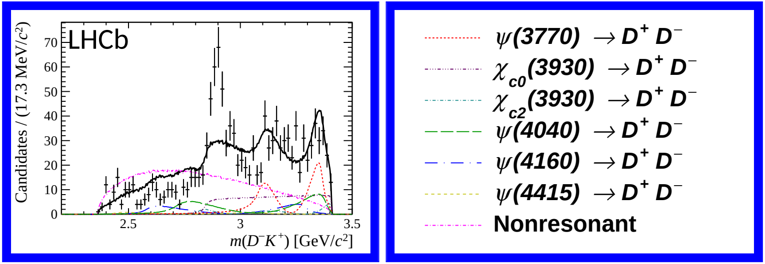
Model excluding $D^{-}K^{+}$ resonances

- $\psi(3770)$, $\chi_{c0}(3930)$, $\chi_{c2}(3930)$, $\psi(4040)$, $\psi(4160)$, and $\psi(4415)$ resonances
- Reflections model the $D^{+}K^{+}$ spectrum satisfactorily:



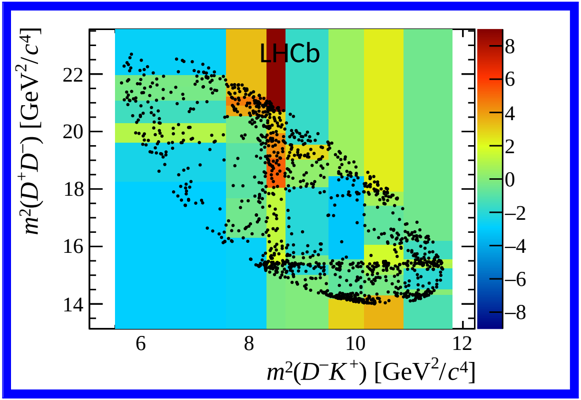
Model excluding D^-K^+ resonances

- $\psi(3770)$, $\chi_{c0}(3930)$, $\chi_{c2}(3930)$, $\psi(4040)$, $\psi(4160)$, and $\psi(4415)$ resonances
- But the description of the D^-K^+ spectrum is severely deficient!



Model excluding D^-K^+ resonances

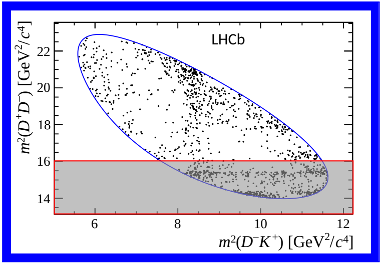
Goodness of fit:

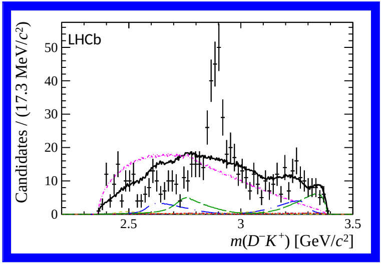


- Largest deviations seen near $m(D^-K^+) \approx 2.9\,\mathrm{GeV}/c^2$

Model excluding $D^- K^+$ resonances

- Clearer: $m(D^+ D^-) > 4\,\mathrm{GeV}/c^2$: cut away low-mass charmonia





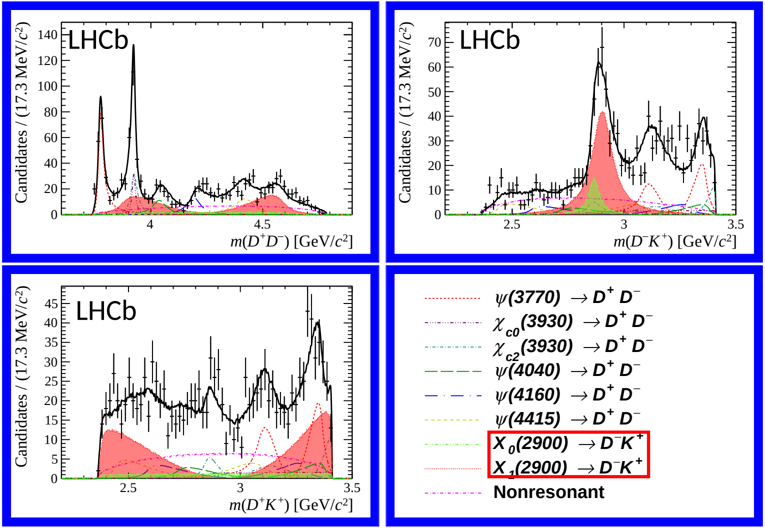
- Bit of a show-stopper

Model including $D^- K^+$ resonances

We had to do something about the $D^- K^+$ channel

- May well need more intricate theoretical study e.g. rescattering effects since suspiciously close to $D^* K^*$ threshold
- Simple approach: new Breit-Wigners (spin-0 **and** spin-1 needed)

Model including $D^{-}K^{+}$ resonances



Model including D^-K^+ resonances

Fit results: coefficients

Resonance	Magnitude	Phase (rad)	Fit fraction (%)
D^+D^- resonances			
$\psi(3770)$	1 (fixed)	0 (fixed)	$14.5 \pm 1.2 \pm 0.8$
$\chi_{c0}(3930)$	$0.506 \pm 0.064 \pm 0.017$	$2.162 \pm 0.184 \pm 0.034$	$3.7 \pm 0.9 \pm 0.2$
$\chi_{c2}(3930)$	$0.703 \pm 0.064 \pm 0.012$	$0.827 \pm 0.170 \pm 0.133$	$7.2 \pm 1.2 \pm 0.3$
$\psi(4040)$	$0.585 \pm 0.078 \pm 0.035$	$1.416 \pm 0.176 \pm 0.084$	$5.0 \pm 1.3 \pm 0.4$
$\psi(4160)$	$0.668 \pm 0.084 \pm 0.052$	$0.898 \pm 0.225 \pm 0.092$	$6.6 \pm 1.5 \pm 1.2$
$\psi(4415)$	$0.797 \pm 0.080 \pm 0.061$	$-1.458 \pm 0.197 \pm 0.091$	$9.2 \pm 1.4 \pm 1.5$
D^-K^+ resonances			
$X_0(2900)$	$0.619 \pm 0.079 \pm 0.025$	$1.091 \pm 0.193 \pm 0.095$	$5.6 \pm 1.4 \pm 0.5$
$X_1(2900)$	$1.449 \pm 0.086 \pm 0.032$	$0.367 \pm 0.102 \pm 0.049$	$30.6 \pm 2.4 \pm 2.1$
Nonresonant	$1.293 \pm 0.088 \pm 0.043$	$-2.410 \pm 0.119 \pm 0.508$	$24.2 \pm 2.2 \pm 0.5$

- Total fit fraction: 107%

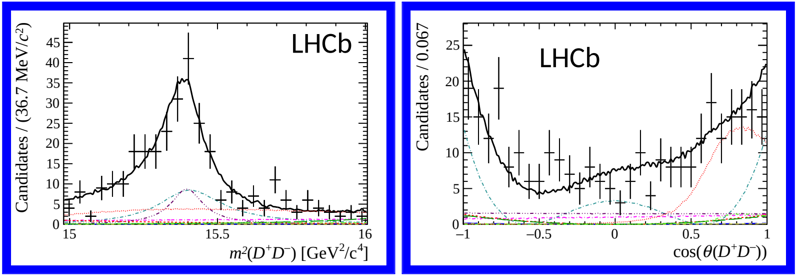
Model including D^-K^+ resonances

Fit results: lineshapes

Resonance	Mass (GeV/c^2)	Width (MeV/c^2)
$\chi_{c0}(3930)$	$3.9238 \pm 0.0015 \pm 0.0004$	$17.4 \pm 5.1 \pm 0.8$
$\chi_{c2}(3930)$	$3.9268 \pm 0.0024 \pm 0.0008$	$34.2 \pm 6.6 \pm 1.1$
$X_0(2900)$	$2.8663 \pm 0.0065 \pm 0.0020$	$57.2 \pm 12.2 \pm 4.1$
$X_1(2900)$	$2.9041 \pm 0.0048 \pm 0.0013$	$110.3 \pm 10.7 \pm 4.3$

Model including $D^- K^+$ resonances

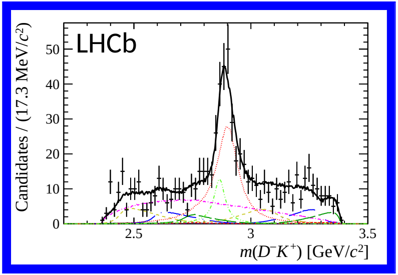
Zoom in on the $\chi_{cJ}(3930)$ ($15\,\mathrm{GeV}/c^2 < m^2(D^+D^-) < 16\,\mathrm{GeV}/c^2$):

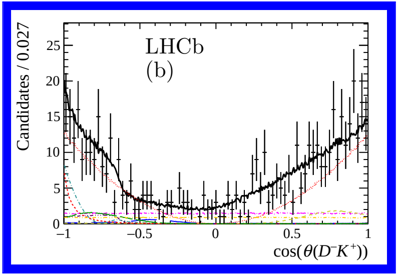


- Both a spin-0 and spin-2 component are needed in this region
- Masses are consistent and spin-0 slightly narrower 2002.03311

Model including D^-K^+ resonances

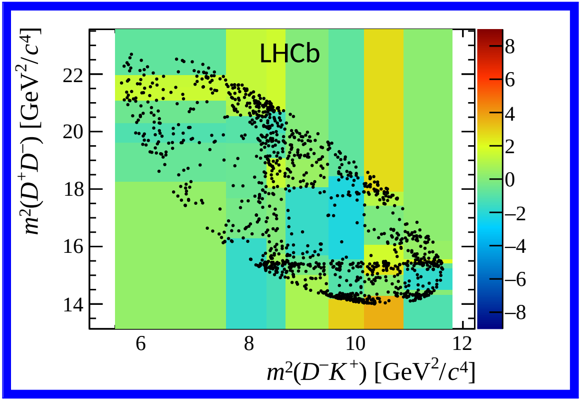
Focus on the new D^-K^+ states ($m(D^+D^-) > 4\,\mathrm{GeV}/c^2$):





Model including $D^{-}K^{+}$ resonances

Goodness of fit:



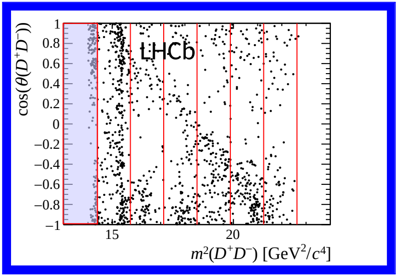
- The χ^2/ndf is 86.1/38.3 = 2.25

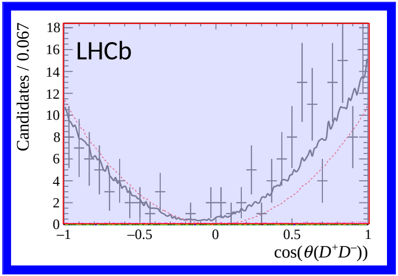
Model including D^-K^+ resonances

Main areas of disagreement (1):

$\left(m^2(D^-K^+), m^2(D^+D^-)\right) \sim \left(10.5\,\mathrm{GeV}^2/c^4, 13.5\,\mathrm{GeV}^2/c^4\right)$

- Data exhibit large interference between S and P wave at low $m(D^+D^-)$, but fit does not introduce any S wave here:





Model including D^-K^+ resonances

Main areas of disagreement (2):

$\left(m^2(D^-K^+), m^2(D^+D^-)\right) \sim (10.5\,\mathrm{GeV}^2/c^4, 18.5\,\mathrm{GeV}^2/c^4)$

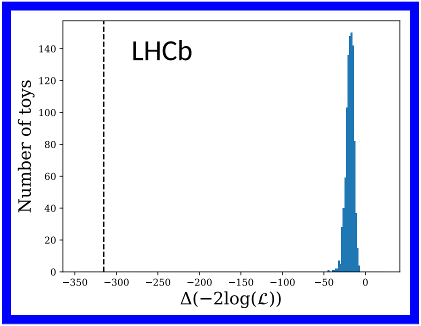
- Seems to originate at low values of $m^2(D^+K^+)$. No particular disagreement is seen in other projections of this region, and therefore it is not considered a source of concern.

Conclusion

The fit is not perfect but the new features are too narrow or too prominent to be ignored

Significance of new $D^- K^+$ state

- Generate $\sim$ 1000 toys from data fit with no $D^- K^+$ components
- Fit with model with and without the new components
- Find difference in NLL for the toy ensemble, and for the data:

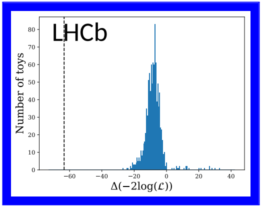


- Overwhelmingly significant, $\gg 5\sigma$

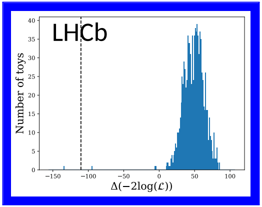
Significance of $\chi_{cJ}(3930)$ spin conclusions

- Generate $\sim$ 1000 toys from data fit with single $\chi_{c0,1,2}$ resonance
- Fit with model with that resonance or with both spin-0 and 2
- Find difference in NLL for the toy ensemble, and for the data:

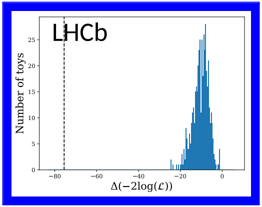
χ_{c0}-only



χ_{c1}-only



χ_{c2}-only



- Strong preference for the spin-0 and spin-2 combination

Systematic uncertainties

Major sources:

- Blatt-Weisskopf radii conventionally set to $4\,\mathrm{GeV}^{-1}$. Vary parent, charmonia, charm-strange radii separately. Dominant effect from the latter two ($\sim 50\%\,\sigma_{\rm stat}$)
- S wave modelling: introduce 5% uniform NR component in toy ensemble and fit with standard model ($10 \longrightarrow 80\%\,\sigma_{\rm stat}$)
- P wave modelling: add $\psi(4320)$ with fixed parameters ($10 \longrightarrow 100\%\,\sigma_{\rm stat}$)
- Limited MC statistics: bootstrap efficiency models and repeat fit to data ($\sim 10\%\,\sigma_{\rm stat}$)
- Hardware trigger modelling in MC: build alternative efficiency map using calibration samples ($\sim 10\%\,\sigma_{\rm stat}$)

Systematic uncertainties

Minor sources - percent-level:

- Signal yield uncertainty
- Signal PDF used in mass-fit
- Limited sideband statistics for background model
- Uncertainty in PID modelling in MC (PIDGen)

Outline

1. Introduction
2. Datasets
3. Model-independent analysis [arXiv:2009.00025], PRL accepted
4. Amplitude analysis [arXiv:2009.00026], PRD accepted
5. Reaction
6. Conclusion

$cs\bar{u}\bar{d}$ tetraquark

- 0^+ state an isosinglet compact tetraquark
- Analogy to $bb\bar{u}\bar{d}$ predicted by lattice QCD
- Discussed in 2008.05993, 2008.07145, 2008.07295, 2008.07340

Pro

Successfully explain the 0^+ state

Con

- *(Most) struggle with 1^-*
- *Analogy to $bb\bar{u}\bar{d}$ doubtful (far from threshold)*
- *Accompanied by plethora of additional states (pro?)*

Molecular bound state

- Genuine prediction (2010) for an isoscalar $D^*\overline{K}^*$ 0^+ state
- Prediction in 1005.0335 refined (to get the right mass!) in 2008.11171
- More discussion in 2008.07389, 2008.07782, 2008.06894, 2008.07516, 2008.09516.

Pro

- *Successfully explain the 0^+ state*
- *Diquark-diantiquark picture gives 1^-*

Con

- *(Most) struggle with 1^-*
- *More 1^+, 2^+ states expected*

Rescattering structure from nearby threshold

- Triangle diagram coupling B to DDK final state
- Assume single-pion exchange dominates: only possible between $D^*\overline{K}^*$ (not $D^*\overline{K}$, $D\overline{K}^*$, $D\overline{K}$)
- $D_1(2420)\overline{K} \to D^*\overline{K}^*$ scattering OK. Thresholds at $2.9\,\mathrm{GeV}/c^2$.

Pro

- *Nice connection to suspicious thresholds*
- *Natural explanation of 1^- with $D_1(2420)\overline{K}$ in S wave*
- *Discussed in 2008.07190 and 2008.12838*

Con

- *Only (so far) tested in fit to 1D mass projection*

What next?

Confirmation:

- Does the state reappear in $B^0 \to D^0 D^- K^+$ and $B^+ \to D^- K^+ \pi^+$?

Composition:

- Is the structure also present in $B^+ \to D^+ \bar{D}^0 K^0_S$ (also $cs\bar{u}\bar{d}$)?

Extension:

- Is it an isosinglet/triplet? Do additional states appear in $B^+ \to D^0 \bar{D}^0 K^+$ $(\bar{c}uu\bar{s})$?
- Is there a 1^+ partner in $B^+ \to D^+ D^{-*} K^+$?

... and all with a dataset that should increase in size by a factor of 5 by the end of 2024!

Outline

Conclusions

- **First** analysis of $D^+D^-K^+$ resonant structure
- **First** model-independent evidence for $D^+D^-K^+$ structure that cannot be accounted for by charmonium resonances
- **First** amplitude model of $D^+D^-K^+$
- Model-dependent **discovery** of exotic structure in D^-K^+
- **Discovery** of contributions from spin-0 and spin-2 components in the region of the existing '$\chi_{c2}(3930)$'

Resonance	Mass (GeV/c^2)	Width (MeV/c^2)	Fit fraction (%)
$\chi_{c0}(3930)$	3.924 ± 0.002	17.4 ± 5.2	3.7 ± 0.9
$\chi_{c2}(3930)$	3.927 ± 0.003	34.2 ± 6.7	7.2 ± 1.2
$X_0(2900)$	2.866 ± 0.007	57.2 ± 12.9	5.6 ± 1.5
$X_1(2900)$	2.904 ± 0.005	110.3 ± 11.5	30.6 ± 3.2

Backup: constraints compared to PDG

Expect natural J^P (→pseudoscalars) and suppressed high-spin

Partial wave (J^{PC})	Resonance	Mass (MeV/c^2)	Width (MeV/c^2)
P wave (1^{--})	$\psi(3770)$ (PDG)	3773.4 ± 0.4	27.2 ± 1.0
	$\psi(3770)$ (1903.12240)	3778.1 ± 0.9	27.2 ± 1.0
D wave (2^{++})	$\chi_{c2}(3930)$ (PDG)	3922.2 ± 1.0	35.3 ± 2.8
	$\chi_{c2}(3930)$ (1903.12240)	3921.9 ± 0.6	36.6 ± 2.1

- Most values taken from PDG
- $m(\psi(3770))$ and $\{m, \sigma\}(\chi_{c2}(3930), X(3842))$ from 1903.12240