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# Solving Beautiful Puzzles

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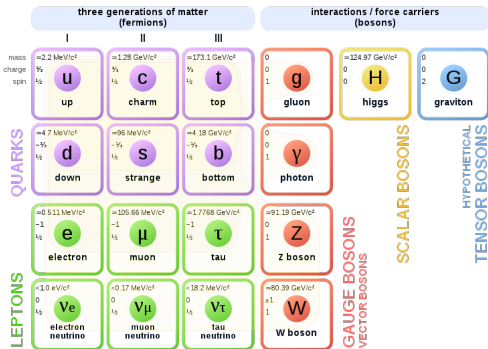
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K. Keri Vos

Maastricht University & Nikhef

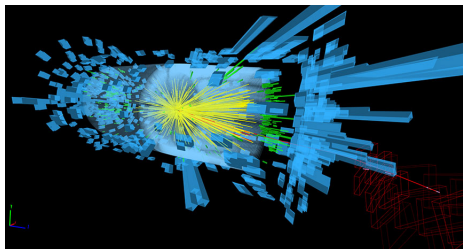
# Testing the Standard Model

## Standard Model of Elementary Particles and Gravity

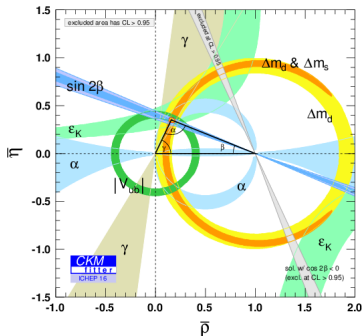


Passed all tests up to 100 GeV

# Testing the Standard Model



Energy/Direct



Precision/Indirect

## Precision frontier

Tiny deviations from SM predictions constrain effects of New Physics

# The Flavour Puzzle

- Flavour symmetry broken by Yukawa couplings to the Higgs field
- Origin of mixing between families described by unitary CKM matrix
- Visualized by unitary triangles
- Dominant source of CP violation (antiparticle-particle asymmetry)

$$\begin{pmatrix} \mathbf{V}_{ud} & V_{us} & V_{ub} \\ V_{cd} & \mathbf{V}_{cs} & V_{cb} \\ V_{td} & V_{ts} & \mathbf{V}_{tb} \end{pmatrix}$$

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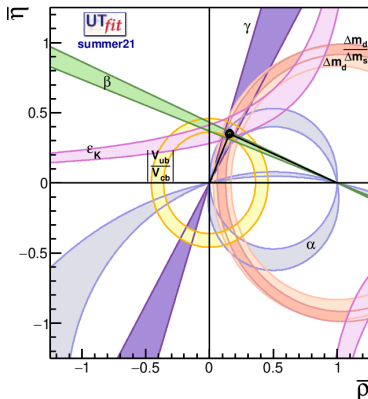
$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

Our understanding of Flavour is unsatisfactory

# The Flavour Puzzle

Thanks to Marcella Bona for providing the 2021 plots

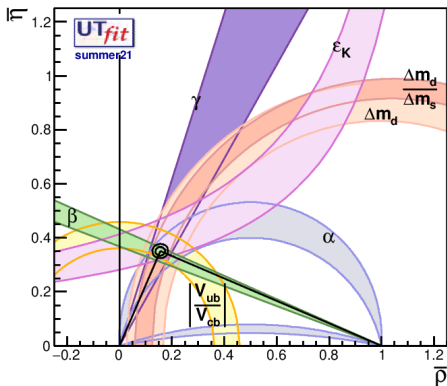
$$\bar{\rho} + i\bar{\eta} = -\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*}$$



# The Flavour Puzzle

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$$\bar{\rho} + i\bar{\eta} = -\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*}$$



Huge amounts of data + theory advances = Precision frontier

Tiny deviations from SM predictions constrain effects of New Physics

# SM or beyond?

## Challenge:

Disentangle SM long-distances effects from the effects of new interactions



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# SM or beyond?

## Challenge:

Disentangle SM long-distances effects from the effects of new interactions

- Some anomalies already spotted
- Revise previous assumptions: reliable theory uncertainties
- Look for the cleanest observables/methods

# Puzzles in Flavour Physics

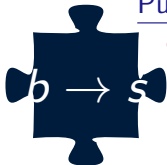
## Challenge:

Disentangle SM long-distance effects from the effects of new physics contributions



## Puzzles in semileptonic decays

- Inclusive versus Exclusive
- $V_{cb}$  and  $V_{ub}$
- LFUV in  $R_D$  and  $R_{D^*}$



## Puzzles in rare decays

- Anomalies in  $b \rightarrow sll$

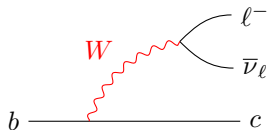


# Puzzles in semileptonic decays: $V_{ub}$ and $V_{cb}$

Inclusive versus Exclusive decays



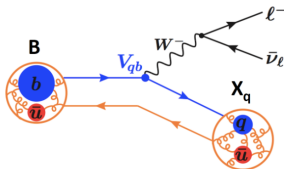
# Exclusive versus Inclusive Theory



- Theory (Weak interaction): Transitions between **quarks/partons**

# Exclusive versus Inclusive Theory

Figure from Marzia Bordone



- Theory (Weak interaction): Transitions between **quarks/partons**
- Observation: Transitions between **hadrons**

## Challenge:

- Dealing with QCD at large distances/small scales
- Parametrize fundamental mismatch in non-perturbative objects
  - Calculable: Lattice or Light-cone sumrules
  - Measurable: from data

## Inclusive $B \rightarrow X_c \ell \nu$ : Heavy Quark Expansion (HQE)

- $b$  quark mass is large compared to  $\Lambda_{\text{QCD}}$
- Setting up the HQE: momentum of  $b$  quark:  $p_b = m_b v + k$ , expand in  $k \sim iD$
- Optical Theorem  $\rightarrow$  (local) Operator Product Expansion (OPE)

$$d\Gamma = d\Gamma_0 + \frac{d\Gamma_1}{m_b} + \frac{d\Gamma_2}{m_b^2} + \dots \quad d\Gamma_i = \sum_k C_i^{(k)} \langle B | \mathcal{O}_i^{(k)} | B \rangle$$

- $C_i^{(k)}$  perturbative Wilson coefficients
- $\langle B | \dots | B \rangle$  non-perturbative matrix elements  $\rightarrow$  string of  $iD$
- operators contain chains of covariant derivatives

$$\langle B | \mathcal{O}_i^{(n)} | B \rangle = \langle B | \bar{b}_v (iD_\mu) \dots (iD_{\mu_n}) b_v | B \rangle$$

- HQE parameters extracted from **lepton energy** and **hadronic mass** moments

$\Gamma_i$  are power series in  $\mathcal{O}(\alpha_s)$

$$\Gamma = \Gamma_0 + \frac{1}{m_b} \Gamma_1 + \frac{1}{m_b^2} \Gamma_2 + \frac{1}{m_b^3} \Gamma_3 \dots$$

- $\Gamma_0$ : decay of the free quark (partonic contributions),  $\Gamma_1 = 0$
- $\Gamma_2$ :  $\mu_\pi^2$  kinetic term and the  $\mu_G^2$  chromomagnetic moment

$$2M_B \mu_\pi^2 = - \langle B | \bar{b}_\nu iD_\mu iD^\mu b_\nu | B \rangle$$

$$2M_B \mu_G^2 = \langle B | \bar{b}_\nu (-i\sigma^{\mu\nu}) iD_\mu iD_\nu b_\nu | B \rangle$$

- $\Gamma_3$ :  $\rho_D^3$  Darwin term and  $\rho_{LS}^3$  spin-orbit term

$$2M_B \rho_D^3 = \frac{1}{2} \langle B | \bar{b}_\nu [iD_\mu, [ivD, iD^\mu]] b_\nu | B \rangle$$

$$2M_B \rho_{LS}^3 = \frac{1}{2} \langle B | \bar{b}_\nu \{ iD_\mu, [ivD, iD_\nu] \} (-i\sigma^{\mu\nu}) b_\nu | B \rangle$$

- $\Gamma_4$ : 9 parameters Mannel, Turczyk, Uraltsev, JHEP 1010 (2011) 109
- $\Gamma_5$ : 18 parameters Mannel, Turczyk, Uraltsev, JHEP 1010 (2011) 109



# Moments of the spectrum

BABAR, PRD 68 (2004) 111104; BABAR, PRD 81 (2010) 032003; Belle, PRD 75 (2007) 032005

Non-perturbative matrix elements obtained from moments of differential rate

## Charged lepton energy

$$\langle E^n \rangle_{\text{cut}} = \frac{\int_{E_\ell > E_{\text{cut}}} dE_\ell E_\ell^n \frac{d\Gamma}{dE_\ell}}{\int_{E_\ell > E_{\text{cut}}} dE_\ell \frac{d\Gamma}{dE_\ell}}$$

## Hadronic invariant mass

$$\langle (M_X^2)^n \rangle_{\text{cut}} = \frac{\int_{E_\ell > E_{\text{cut}}} dM_X^2 (M_X^2)^n \frac{d\Gamma}{dM_X^2}}{\int_{E_\ell > E_{\text{cut}}} dM_X^2 \frac{d\Gamma}{dM_X^2}}$$

$$R^*(E_{\text{cut}}) = \frac{\int_{E_\ell > E_{\text{cut}}} dE_\ell \frac{d\Gamma}{dE_\ell}}{\int_0 dE_\ell \frac{d\Gamma}{dE_\ell}}$$

- Moments up to  $n = 3, 4$  and with several energy cuts available
- Experimentally necessary to use lepton energy cut

# State-of-the-art in inclusive $b \rightarrow c$

Ježabek, Kuhn, NPB 314 (1989) 1; Melnikov, PLB 666 (2008) 336; Pak, Czarnecki, PRD 78 (2008) 114015; Becher, Boos, Lunghi, JHEP 0712 (2007) 062; Alberti, Gambino, Nandi, JHEP 1401 (2014) 147; Mannel, Pivovarov, Rosenthal, PLB 741 (2015) 290; Fael, Schonwald, Steinhauser, Phys Rev. D 104 (2021) 016003; Fael, Schonwald, Steinhauser, Phys Rev. Lett. 125 (2020) 052003; Fael, Schonwald, Steinhauser, Phys Rev. D 103 (2021) 014005,

$$\Gamma \propto |V_{cb}|^2 m_b^5 \left[ \Gamma_0 + \Gamma_0^{(1)} \frac{\alpha_s}{\pi} + \Gamma_0^{(2)} \left( \frac{\alpha_s}{\pi} \right)^2 + \Gamma_0^{(3)} \left( \frac{\alpha_s}{\pi} \right)^3 + \frac{\mu_\pi^2}{m_b^2} \left( \Gamma^{(\pi,0)} + \frac{\alpha_s}{\pi} \Gamma^{(\pi,1)} \right) + \frac{\mu_G^2}{m_b^2} \left( \Gamma^{(G,0)} + \frac{\alpha_s}{\pi} \Gamma^{(G,1)} \right) + \frac{\rho_D^3}{m_b^3} \left( \Gamma^{(D,0)} + \Gamma_0^{(1)} \left( \frac{\alpha_s}{\pi} \right) \right) + \mathcal{O} \left( \frac{1}{m_b^4} \right) + \dots \right]$$

- Include terms up to  $1/m_b^3$ \* see also Gambino, Healey, Turczyk [2016]
- **Recent progress:**  $\alpha_s^3$  to total rate and kinetic mass Fael, Schonwald, Steinhauser [2020, 2021]
- **Recent progress:**  $\alpha_s \rho_D^3$  for total rate Mannel, Pivovarov [2020]
- Includes all known  $\alpha_s$ ,  $\alpha_s^2$  and  $\alpha_s^3$  corrections!

**Recent update:**

$$|V_{cb}|_{\text{incl}} = (42.16 \pm 0.51) \times 10^{-3}$$

Gambino, Schwanda, PRD 89 (2014) 014022;  
Alberti, Gambino et al, PRL 114 (2015) 061802;  
Bordone, Capdevila, Gambino, Phys.Lett.B 822 (2021) 136679

$$\Gamma \propto |V_{cb}|^2 m_b^5 \left[ \Gamma_0 + \Gamma_0^{(1)} \frac{\alpha_s}{\pi} + \Gamma_0^{(2)} \left( \frac{\alpha_s}{\pi} \right)^2 + \Gamma_0^{(3)} \left( \frac{\alpha_s}{\pi} \right)^3 + \frac{\mu_\pi^2}{m_b^2} \left( \Gamma(\pi,0) + \frac{\alpha_s}{\pi} \Gamma(\pi,1) \right) \right. \\ \left. + \frac{\mu_G^2}{m_b^2} \left( \Gamma(G,0) + \frac{\alpha_s}{\pi} \Gamma(G,1) \right) + \frac{\rho_D^3}{m_b^3} \left( \Gamma(D,0) + \Gamma_0^{(1)} \left( \frac{\alpha_s}{\pi} \right) \right) + \mathcal{O} \left( \frac{1}{m_b^4} \right) + \dots \right]$$

## Challenge:

- Include higher-order  $1/m_b$  and  $\alpha_s$  corrections
- Proliferation of non-perturbative matrix elements
  - 4 up to  $1/m_b^3$
  - 13 up to  $1/m_b^4$  Dassinger, Mannel, Turczyk, JHEP 0703 (2007) 087
  - 31 up to  $1/m_b^5$  Mannel, Turczyk, Uraltsev, JHEP 1011 (2010) 109

# Alternative $V_{cb}$ determination

Mannel, KKV, JHEP 1806 (2018) 115; Fael, Mannel, KKV, JHEP 02 (2019) 177

- Setting up the HQE: momentum of  $b$  quark:  $p_b = m_b v + k$ , expand in  $k \sim iD$
- Choice of  $v$  not unique: Reparametrization invariance (RPI)
  - links different orders in  $1/m_b \rightarrow$  reduction of parameters
  - up to  $1/m_b^4$ : 8 parameters (previous 13)

$$\delta_{RP} v_\mu = \delta v_\mu \quad \text{and} \quad \delta_{RP} iD_\mu = -m_b \delta v_\mu$$

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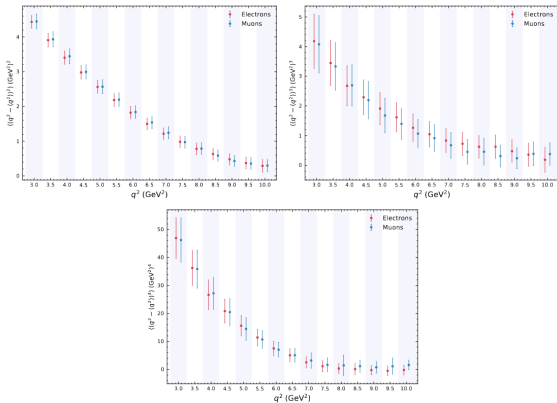
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- Caveat: standard lepton energy and hadronic mass moments are not RPI quantities
- Alternative determination using only RPI  $q^2$  moments including  $1/m_b^4$
- Recent progress: First measurement of  $q^2$  moments Belle [2109.01685], Belle II [2205.06372]

Belle Collaboration [2109.01685, 2105.08001]



Centralized moments as function of  $q_{\text{cut}}^2$

# New $V_{cb}$ Determination

$$\begin{aligned} & R^*(q_{\text{cut}}^2) \quad \langle (q^2)^n \rangle_{\text{cut}} \\ & \downarrow \\ & \mu_3, \mu_G, \tilde{\rho}_D, r_E, r_G, s_E, s_B, s_{qB}, m_b, m_c \\ & \downarrow \\ & \text{Br}(\bar{B} \rightarrow X_c \ell \bar{\nu}) \propto \frac{|V_{cb}|^2}{\tau_B} \left[ \Gamma_{\mu_3} \mu_3 + \Gamma_{\mu_G} \frac{\mu_G^2}{m_b^2} + \Gamma_{\tilde{\rho}_D} \frac{\tilde{\rho}_D^3}{m_b^3} \right. \\ & \quad \left. + \Gamma_{r_E} \frac{r_E^4}{m_b^4} + \Gamma_{r_G} \frac{r_G^4}{m_b^4} + \Gamma_{s_B} \frac{s_B^4}{m_b^4} + \Gamma_{s_E} \frac{s_E^4}{m_b^4} + \Gamma_{s_{qB}} \frac{s_{qB}^4}{m_b^4} \right] \\ & \downarrow \\ & V_{cb} = (41.69 \pm 0.63) \cdot 10^{-3} \end{aligned}$$

Bernlochner, Welsch, Fael, Olschewsky, Persson, van Tonder, KKV [2205.10274]



# New $V_{cb}$ determination

Bernlochner, Welsch, Fael, Olschewsky, Persson, van Tonder, KKV [2205.10274]

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- Independent cross check of previous determinations
  - Agreement at  $1 - 2\sigma$  level
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- First pure data extraction of  $1/m_b^4$  terms
- Important to check convergence of the HQE

$$r_E^4 = (0.02 \pm 0.34) \cdot 10^{-1} \text{GeV}^4 \quad r_G^4 = (-0.21 \pm 0.69) \text{GeV}^4$$

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- Inputs for calculations of  $B \rightarrow X_u \ell \nu$ ,  $B$  lifetimes and  $B \rightarrow X_s \ell \ell$

## $B \rightarrow D$ and $B \rightarrow D^*$

- Form factors extracted from lattice, LC sumrules (+data)
- Knowledge on the  $q^2$  dependence crucial
- BGL Boyd, Grinstein, Lebed or CLN/HQE Caprini, Lellouch, Neubert parametrization
  - Start of many discussions Gambino, Jung, Schacht, Bordone, van Dyck, Gubernari, ...
  - BGL: model independent parametrization using analyticity
  - CLN\*: uses HQE at  $1/m_b$  + assumptions \*justified at time of introduction
- Improved HQE treatment including  $1/m_c^2$  corrections Bordone, van Dyk, Jung [1908.09398]

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- **Recent progress:**  $B \rightarrow D^*$  form factors at nonzero recoil Fermilab/MILC [2105.14019]
  - tension between the slope of the lattice and experimental data
- Same form factors determine SM predictions for  $R_{D^{(*)}}$
- **New experimental and lattice data needed!**

# The challenge of $V_{ub}$

## Exclusive $B \rightarrow \pi \nu$

- Only one form factor
- Combining Lattice QCD [FNAL/MILC, RBC/UKQCD] and QCD sum rules

Recent update:

Lejnak, Melic, van Dyk [2102.07233]

$$|V_{ub}|_{\text{excl}} = (3.77 \pm 0.15) \cdot 10^{-3}$$

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Recent update:

Leljak, Melic, van Dyk [2102.07233]

$$|V_{ub}|_{\text{excl}} = (3.77 \pm 0.15) \cdot 10^{-3}$$

## Inclusive $B \rightarrow X_u \ell \nu$

- Experimental cuts necessary to remove charm background
- Local OPE as in  $b \rightarrow c$  cannot work
- Switch to different set-up using light-cone OPE
- Introduce non-perturbative shape functions ( $\sim$  parton DAs in DIS)
- Different frameworks: **BLNP**, **GGOU**, **DGE**, **ADFR**

Recent update:

Belle [2102.00020]

$$|V_{ub}|_{\text{incl}} = (4.10 \pm 0.28) \cdot 10^{-3}$$

## Update of BLNP approach

- Systematic framework: Soft Collinear Effective Theory (SCET)
- Separates the different scales in the problem
- **In progress:** include known  $\alpha_s^2$  corrections
- Moments of shape functions can be linked to HQE parameters in  $b \rightarrow c$ 
  - **In progress:** include higher-moments
  - kinetic mass scheme as in  $b \rightarrow c$
- Shape function is non-perturbative and cannot be computed
  - **In progress:** new flexible parametrization



## Update of BLNP approach

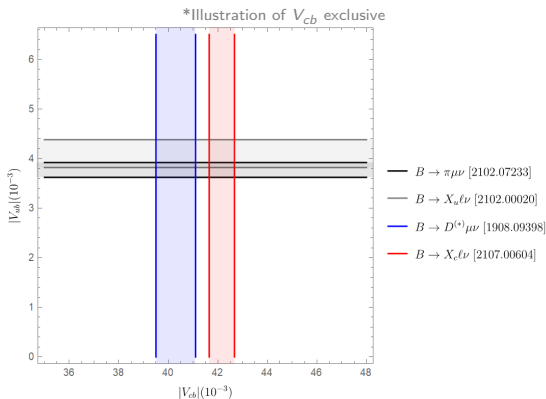
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**In progress:**

Gunawardana, Lange, Mannel, Paz, Olschewsky, KKV [in progress]

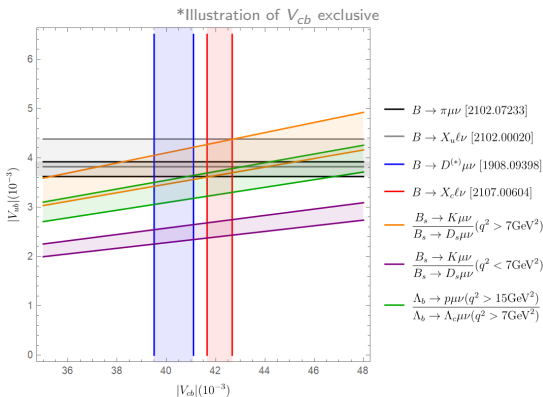
$$|V_{ub}|_{\text{incl}} = \text{Stay Tuned!}$$

# Inclusive versus Exclusive semileptonic decays



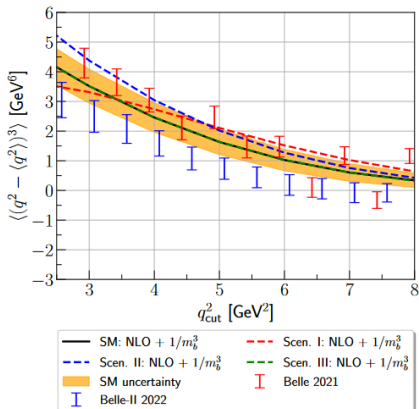
- Recently a lot of attention for the  $V_{cb}$  puzzle! [Bigi, Schacht, Gambino, Jung, Straub, Bernlochner, Bordone, van Dyk, Gubernari]

# Inclusive versus Exclusive semileptonic decays



- Recently a lot of attention for the  $V_{cb}$  puzzle! [Bigi, Schacht, Gambino, Jung, Straub, Bernlochner, Bordone, van Dyk, Gubernari]
- **Recent progress:**  $B_s \rightarrow K \mu \nu$  [LHCb [2012.05143], Khodjamirian, Rusov [2017]]
- Unlikely to be due to NP Jung, Straub [2018]
- **New data necessary: stay tuned!**

Rahimi, Fael, Vos [2208.04282]



- NP would also influence the moments of the spectrum
- Requires a simultaneous fit of hadronic parameters and NP **In progress..**

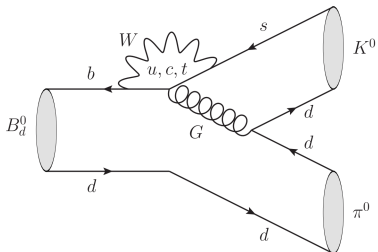
# Puzzles in nonleptonic decays

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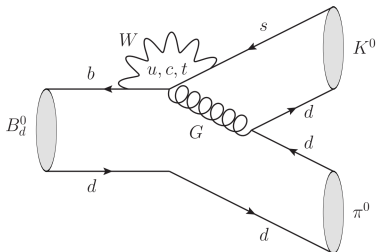
# The challenge of nonleptonic $B$ decays

- Nonleptonic decays are important probes of CP violation
  - Direct CP violation due to different strong and weak phases
  - Mixing-induced CP violation in neutral decays probe mixing phase  $\phi_{d,s}$
  - Sensitivity to NP in loops (penguins)
- CP violation in the SM is too small and peculiar!
  - CKM CP violating effects only from flavour changing currents
  - Flavour diagonal CP violation tiny in SM (EDMs)
  - Large CP asymmetries with processes with tiny BRs and vice versa



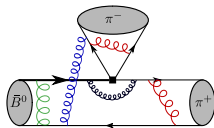
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Challenge: Calculation of Hadronic matrix elements

# How to handle nonleptonic B decays?



## QCD Factorization Beneke, Buchalla, Neubert, Sachrajda

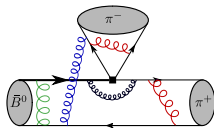
- Disentangle perturbative (calculable) and non-perturbative dynamics using HQE
- Systematic expansion in  $\alpha_s$  and  $1/m_b$  (studied up to  $\alpha_s^2$ ) Bell, Beneke, Huber, Li

$$\langle \pi^+ \pi^- | Q_i | B \rangle = T_i^I \otimes F^{B \rightarrow \pi^+} \otimes \Phi_{\pi^-} + T_i^{II} \otimes \Phi_{\pi^-} \otimes \Phi_{\pi^+} \otimes \Phi_B$$

- Non-perturbative **form factors** and **LCDAs**
  - from data, lattice or Light-Cone Sum Rules
- No systematic framework to compute power corrections (yet?)
- Strong phases suffer from large uncertainties
- Theoretical challenge: reliable computations of observables
- **Include QED corrections** Beneke, Boer, Toelstede, KKV [2020]



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- Disentangle perturbative (calculable) and non-perturbative dynamics using HQE
- **Include QED corrections** Beneke, Boer, Toelstede, KKV [2020]

## Flavour symmetries (Isospin or $SU(3)$ )

- Many studies e.g. Fleischer, Jaarsma, KKV, Malami [2017,2018]
- **Recent progress:** Global  $SU(3)$  fit to  $B \rightarrow PP$  decays Huber, Tetlalmatzi-Xolocotzi [2111.06418]

$B \rightarrow \pi K$  puzzle



# The $B \rightarrow K\pi$ Puzzle

e.g. Buras, Fleischer, Recksiegel, Schwab [2004, 2007]; Fleischer, Jaeger, Pirjol, Zupan [2008]

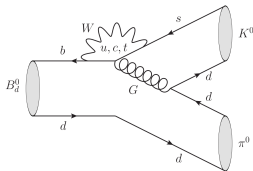
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- Penguin dominated; Electroweak penguins contribute at same level as tree!

$$\delta(\pi K) \equiv A_{CP}(\pi^0 K^-) - A_{CP}(\pi^+ K^-)$$

- Recent LHCb measurement for  $A_{CP}(K^- \pi^0)$   
LHCb Collaboration, PRL 126, 091802 [2021]
- Confirms and enhances the observed difference
  - $\delta(\pi K)^{\text{exp}} = (11.5 \pm 1.4)\%$
  - $8\sigma$  from 0



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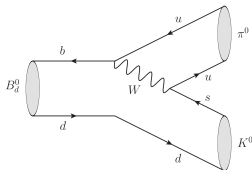
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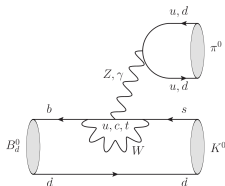
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- Hint for NP in the EWP sector?



e.g. Gronau [2005]; Gronau, Rosner [2006]

$$\begin{aligned}\Delta(\pi K) \equiv & A_{\text{CP}}(\pi^+ K^-) + \frac{\Gamma(\pi^- \bar{K}^0)}{\Gamma(\pi^+ K^-)} A_{\text{CP}}(\pi^- \bar{K}^0) - \frac{2\Gamma(\pi^0 K^-)}{\Gamma(\pi^+ K^-)} A_{\text{CP}}(\pi^0 K^-) \\ & - \frac{2\Gamma(\pi^0 \bar{K}^0)}{\Gamma(\pi^+ K^-)} A_{\text{CP}}(\pi^0 \bar{K}^0) \equiv \Delta(\pi K)^{\text{QCD}} + \delta\Delta(\pi K)\end{aligned}$$

- Sensitive to new physics effects:  $\Delta(\pi K)^{\text{QCD}} = (0.5 \pm 1.1)\%$  [Bell, Beneke, Huber, Li]
- QED effects:  $\delta\Delta(\pi K) = -0.42\%$  [Beneke, Boer, Toelstede, KKV [2020]]
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- Mixing-induced CP asymmetry in  $B \rightarrow \pi^0 K^0$  provides additional test [Fleischer, Jaarsma, Malami, KKV [2016,2018]]



$B \rightarrow D\pi$  puzzle



# $B_s^0 \rightarrow D_s^+ \pi$ and $B_d^0 \rightarrow D^+ K^-$ puzzle

see also Cai, Deng, Li, Yang [2103.04138], Endo, Iguro, Mishima [2109.10811], Gershon, Lenz, Rusov, Skidmore [2111.04478]

## Discrepancies between data and theory for $B_s \rightarrow D_s^{+(*)} \pi^-$ and $B \rightarrow D^{+(*)} K^-$

- pure tree decays (no color-suppressed nor penguin contributions)
- NNLO predictions in QCDF Huber, Kraenkl [1606.02888]
- Same form factors as for exclusive  $V_{cb}$
- Updated and extended calculations give  $\sim 4\sigma$  deviation Bordone, Gubernari, Huber, Jung and van Dyk, [2007.10338]

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- QED corrections cannot explain the tension\* Beneke, Boer, Finauri, KKV [2107.03819]
- Possible NP explanations have been studied Iguro, Kitahara [2008.01086], Bordone, Greljo, Marzocca [2103.10332]
- Also puzzling patterns in  $B_s \rightarrow D_s K$  are revealed Fleischer, Malami [2110.04240]

Interesting puzzle that requires both experimental and theoretical attention!

# The Challenge of QED Corrections

---

$$\Gamma[\bar{B} \rightarrow M_1 M_2](\Delta E) \equiv \Gamma[\bar{B} \rightarrow M_1 M_2 + X_s] \Big|_{E_{X_s} \leq \Delta E},$$

- IR finite observable (width) must include **ultra-soft photon** radiation
- $X_s$  are soft photons with total energy less than **ultrasoft scale**  $\Delta E$
- Factorizes in **non-radiative** amplitude and **ultrasoft** function

$$\Gamma[\bar{B} \rightarrow M_1 M_2](\Delta E) = |\mathcal{A}(\bar{B} \rightarrow M_1 M_2)|^2 \sum_{X_s} |\langle X_s | (\bar{S}_v^{(Q_B)} S_{v_1}^{\dagger(Q_{M_1})} S_{v_2}^{\dagger(Q_{M_2})}) | 0 \rangle|^2 \theta(\Delta E - E_{X_s})$$

## Simple classification:

- Ultra-soft photons: eikonal approximation, well understood

$$\Delta E \ll \Lambda_{\text{QCD}}$$

- **NEW: Non-universal, structure dependent corrections** Beneke, Boer, Toelstede, KKV [2020]
- Both effects important: virtual photons can resolve the structure of the meson!

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- Often done: Assume pointlike approximation up to the scale  $m_B$  [Baracchini, Isidori]
  - fails to account for all large logarithms (and scales)!
  - photons with energy  $\gtrsim \Lambda_{\text{QCD}}$  probe the partonic structure of the mesons

- Ultrasoft effects dress braching ratio

$$U(M_1 M_2) = \left( \frac{2\Delta E}{m_B} \right)^{-\frac{\alpha_{em}}{\pi}} \left( Q_B^2 + Q_{M_1}^2 \left[ 1 + \ln \frac{m_{M_1}^2}{m_{Bq}^2} \right] + Q_{M_2}^2 \left[ 1 + \ln \frac{m_{M_2}^2}{m_B^2} \right] \right)$$

- Recover the standard eikonal/QED factor Beneke, Boer, Toelstede, KKV [2020]
- $\Delta E$  is the window of the  $\pi K$  invariant mass around  $m_B$
- Theory requires  $\Delta E \ll \Lambda_{\text{QCD}} = 60 \text{ MeV}$

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$$\rightarrow U(\pi^+ K^-) = 0.914, U(\pi^0 K^-) = U(K^- \pi^0) = 0.976 \text{ and } U(\pi^- \bar{K}^0) = 0.954$$



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- Experimentally usoft effects included using PHOTOS
- Challenging to compare theory with experiment! **In progress...**

# Solving Beautiful Puzzles

---

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Close collaboration between theory and experiment necessary!

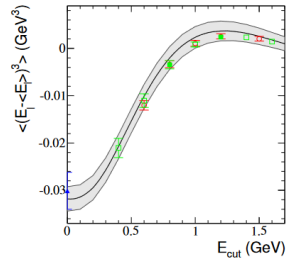
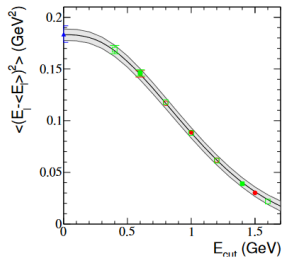
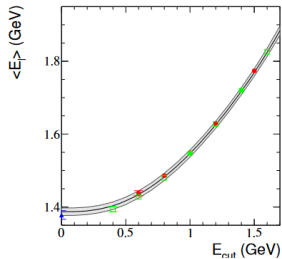
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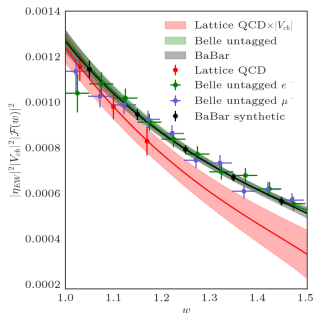
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# Moments of the spectrum

Gambino, Schwanda Phys. Rev. D 89, 014022 (2014)





- Tension between the slope of the lattice and experimental data
- Same form factors determine SM predictions for  $R_{D^{(*)}}$
- **New experimental and lattice data needed!**

Beneke, Boer, Toelstede, KKV, JHEP 11 (2020) 081 [2008.10615]

- QED gives sub-percent corrections to Branching ratios

- Beneficial to consider ratios in which QCD is suppressed

$$R_L = \frac{2\text{Br}(\pi^0 K^0) + 2\text{Br}(\pi^0 K^-)}{\text{Br}(\pi^- K^0) + \text{Br}(\pi^+ K^-)} = R_L^{\text{QCD}} + \cos \gamma \text{Re } \delta_E + \delta_U$$

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- **Combined QED effect larger than QCD uncertainty!**

# The $V_{cb}$ puzzle: Inclusive versus Exclusive decays

## Exclusive $B \rightarrow D^{(*)} l \bar{\nu}$

- Form factor required (only for  $B \rightarrow D$  available at different kinematic points)
- Different parametrizations for form factors: CLN Caprini, Lellouch, Neubert [1997] and BGL Boyd, Grinstein, Lebed [1995]
  - BGL: model independent based on unitarity and analyticity
  - CLN: Simple parametrization using HQE relations
- Some inconsistencies in the Belle data were pointed out see e.g. van Dyk, Jung, Bordone, Gubernari [2104.02094]

## Inclusive $B \rightarrow X_c l \nu$

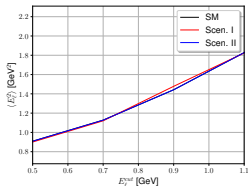
- Determined fully data driven including  $1/m_b$  power corrections

Recently a lot of attention for the  $V_{cb}$  puzzle! Bigi, Schacht, Gambino, Jung, Straub, Bernlochner, Bordone, van Dyk, Gubernari

Stay tuned!

## NP in the $\tau$ sector

- Affects also inclusive  $B \rightarrow X_c \tau \nu$  Rusov, Mannel, Shahriaran [2017]
- Lepton and hadronic moments challenging to measure
- Recently moments of the five-body decay  $B \rightarrow X_c \tau (\rightarrow \mu \nu \nu) \nu$  investigated Mannel, Rahimi, KKV [2105.02163]
- Would also be influenced by NP [in progress]
- Specific NP scenarios from global fit Mandal, Murgui, Penuela, Pich [2004.06726]



Preliminary!



Contribution from five-body charm decay to  $b \rightarrow c \ell \nu$  via

$$B(p_B) \rightarrow X_c(p_{X_c})(\tau(q_{[\tau]} \rightarrow \mu(q_{[\mu]})\nu_\mu(q_{[\bar{\nu}_\mu]})\nu_\tau(q_{[\nu_\tau]}))\bar{\nu}_\tau(q_{[\bar{\nu}_\tau]}))$$

- Phase space suppressed:

$$\frac{\Gamma_{\text{tot}}(b \rightarrow c\tau(\rightarrow \ell\bar{\nu}_\ell\nu_\tau)\bar{\nu}_\tau)}{\Gamma_{\text{tot}}(b \rightarrow c\ell\bar{\nu})} \sim 4.0\%$$

- Experimentally effects diminished by cutting on the invariant mass of the  $B$
- Can be calculated exactly in the HQE

$$\frac{d^8\Gamma}{dq^2 dq_{\nu\bar{\nu}}^2 dp_{X_c}^2 d^2\Omega d\Omega^* d^2\Omega^{**}} = - \frac{3G_F^2 |V_{cb}|^2 \sqrt{\lambda}(q^2 - m_\tau^2)(m_\tau^2 - q_{\nu\bar{\nu}}^2) \mathcal{B}(\tau \rightarrow \mu\nu\nu)}{2^{17} \pi^5 m_\tau^8 m_b^3 q^2} W_{\mu\nu} L^{\mu\nu}$$

- $L_{\mu\nu}$  five-body leptonic tensor (narrow-width limit for  $\tau$ )
- $W_{\mu\nu}$  standard hadronic tensor including HQE parameters

- Interesting to search for new physics! Mannel, Rusov, Shahriaran (2017); Mannel, Rahimi, KKV [in progress]

- Leading order shape functions

$$2m_B f(\omega) = \langle B(v) | \bar{b}_v \delta(\omega + i(n \cdot D)) b_v | B(v) \rangle$$

- Charged Lepton Energy Spectrum (at leading order)

$$\frac{d\Gamma}{dy} \sim \int d\omega \theta(m_b(1-y) - \omega) f(\omega)$$

- Moments of the shapefunction are related to HQE ( $b \rightarrow c$ ) parameters:

$$f(\omega) = \delta(\omega) + \frac{\mu_\pi^2}{6m_b^2} \delta''(\omega) - \frac{\rho_D^3}{m_b^3} \delta'''(\omega) + \dots$$

- Shape function is non-perturbative and cannot be computed

- Systematic framework: Soft Collinear Effective Theory (SCET)
- Separates the different scales in the problem

$$d\Gamma = H \otimes J \otimes S$$

- H: Hard scattering kernel at  $\mathcal{O}(m_b)$
- J: universal Jet function at  $\mathcal{O}(\sqrt{m_b\Lambda_{\text{QCD}}})$
- S: Shape function at  $\mathcal{O}(\Lambda_{\text{QCD}})$
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- Other approach: OPE with hard-cutoff  $\mu$  Gambino, Giordano, Ossola, Uraltsev
  - Use pert. theory above cutoff and parametrize the infrared
  - Different definition of the shape functions
- Shape functions have to be parametrized and obtained from data

# New Physics explanation?

- Too many to count: exclusive  $B \rightarrow D^{(*)}$  in combination with

$$R_{D^{(*)}} = \frac{B \rightarrow D^{(*)} \tau \nu}{B \rightarrow D^{(*)} \mu \nu}$$

- For inclusive  $b \rightarrow c$  less analyses
  - RH-current, scalar and tensor NP contributions to rate Jung, Straub [2018]
  - RH-current to moments Feger, Mannel, et. al. [2010]
  - NP for moments KKV, Fael, Rahimi [in progress]

