



Science & Technology
Facilities Council

CKM measurements and the scope for New Physics therein

Matthew Kenzie

Warwick EPP Seminar

3rd October 2019

Who's this bloke then?

Started at Warwick on Tuesday

From Cambridge

- ▶ Grew up in the house that was built by my great-grandfather
- ▶ He founded “Kenzie’s Coaches”
- ▶ My father was a cinematographer

Education

- ▶ Undergraduate at Durham (BSc Physics)
- ▶ Masters at Imperial (MSc Theoretical Physics)
- ▶ PhD at Imperial / CERN (CMS $H \rightarrow \gamma\gamma$)

Research Career

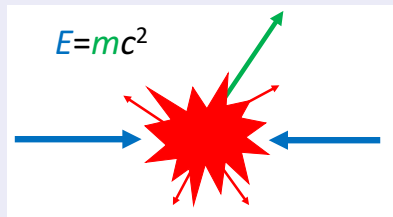
- ▶ CERN Fellow (LHCb)
- ▶ Junior Research Fellow (Cambridge, LHCb)
- ▶ STFC Ernest Rutherford Fellow (Cambridge, LHCb)
- ▶ Now at Warwick



How to find New Physics at the LHC?

High energy frontier

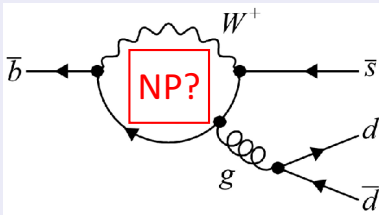
Direct observation



Require $E > mc^2$ for direct production

Precision frontier

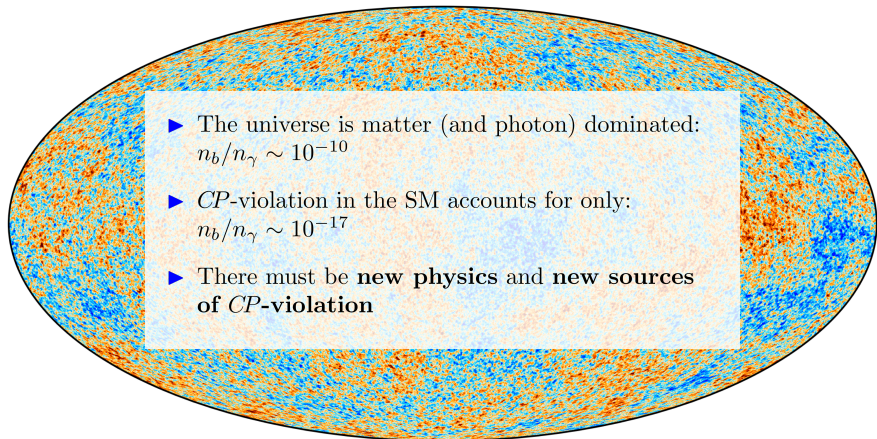
Indirect effects



New particles effect loop processes

- ▶ Most HEP direct discoveries have been preceded by **indirect evidence first!**
 - ▶ Think **charm**, **bottom** and **top** quarks, even the **Higgs**
- ▶ If we don't see New Physics directly at the LHC, indirect evidence can guide us where to look (or what to build) next

Why is the universe matter dominated?

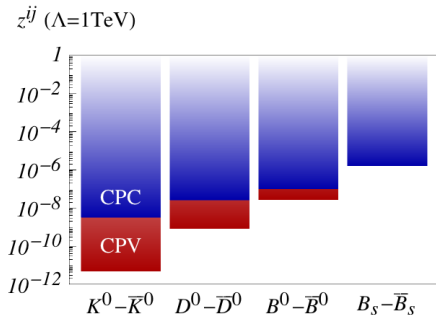
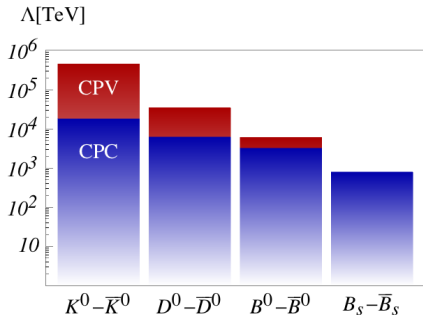


- ▶ *CP*-violation in the SM is generated by **quark flavour transitions**
- ▶ These contain the **only** source of *CP*-violation in the SM ($\theta_{\text{QCD}} = m_\nu = 0$)

New Physics from Flavour sector

- ▶ Direct NP discovery by ATLAS/CMS is still possible
- ▶ **The flavour sector provides another window of opportunity**
 - ▶ High Energy scales, Λ
 - ▶ Low coupling scales, z

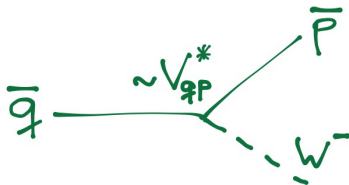
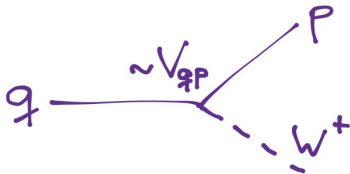
$$Q_{AB}^{(6)} \sim z_{ij} [\bar{q}_i \Gamma^A q_j] \otimes [\bar{q}_i \Gamma^B q_j]$$



Isidori, Nir and Perez, [*Ann. Rev. Nucl. Part. Sci* (2010) 60:355]

The CKM quark mixing matrix

- ▶ In the SM quarks can **change flavour** by emission of a W^\pm boson
 - ▶ So must also change charge (i.e. from up-type to down-type or vice-versa)



- ▶ The probability for such a transition is governed by the elements of the 3×3 **unitary CKM matrix**

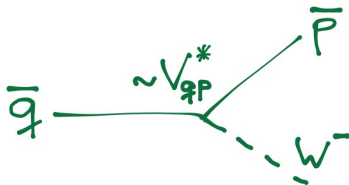
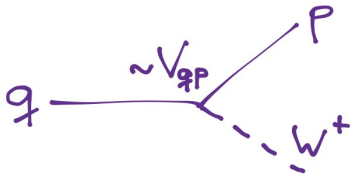
CKM matrix

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \cdot \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

flavour eigenstates mass eigenstates

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 - ▶ It exhibits a **clear hierarchy** (which sets strong constraints on NP)

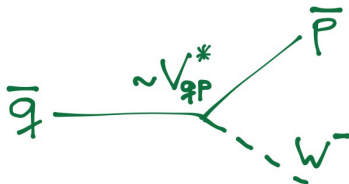
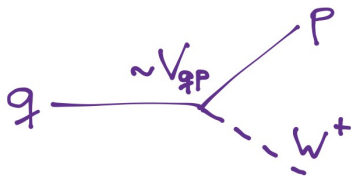
CKM hierarchy

$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \sim \begin{pmatrix} 1 & 0.2 & 0.004 \\ 0.2 & 1 & 0.04 \\ 0.008 & 0.04 & 1 \end{pmatrix}$$

experimentally
determined values

The CKM quark mixing matrix

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- ▶ The probability for such a transition is governed by the elements of the 3×3 **unitary CKM matrix**
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 - ▶ Contains the **only source of CP-violation in the SM** (if $\theta_{\text{QCD}} = m_\nu = 0$)

Wolfenstein parametrisation

$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$

4 $\mathcal{O}(1)$ real parameters (A, λ, ρ, η)

The B^0 unitarity triangle

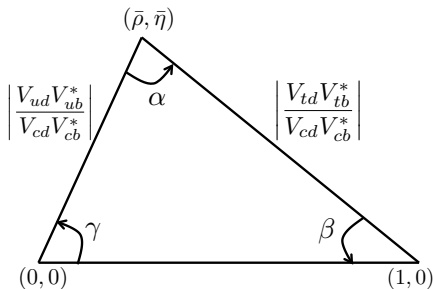
- ▶ Unitarity imposes several conditions ($V^\dagger V = \mathbb{1}$)
 - ▶ Gives rise to “unitarity” triangles
 - ▶ Internal area dictates the **total amount of CPV** in the quark sector

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“The B^0 unitarity triangle”

$$\underbrace{V_{ud}V_{ub}^*}_{\sim \lambda^3} + \underbrace{V_{cd}V_{cb}^*}_{\sim \lambda^3} + \underbrace{V_{td}V_{tb}^*}_{\sim \lambda^3} = 0$$

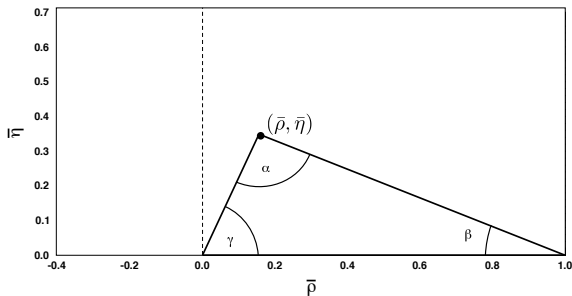


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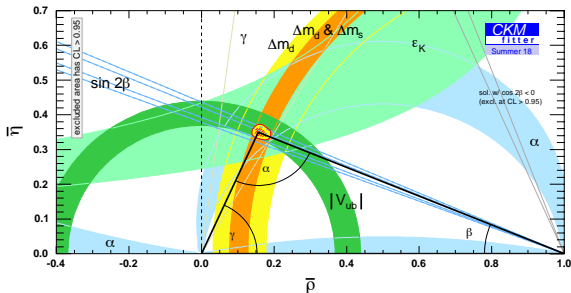


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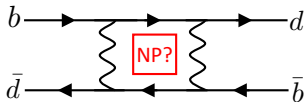
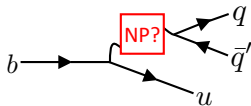


New Physics effects in the flavour sector

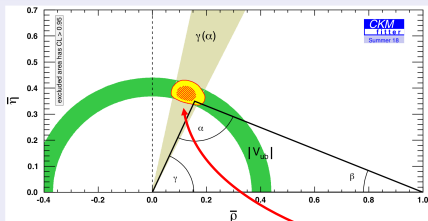
- ▶ Discrepancy between “tree” and “loop” constraints \Rightarrow clear sign of New Physics
- ▶ Sensitive to NP effects at extremely **high energy scales** $\sim \mathcal{O}(10^2 - 10^3)$ TeV

Direct: $\gamma = (72.1^{+5.4}_{-5.7})^\circ$
Indirect: $\gamma = (65.6^{+1.0}_{-3.4})^\circ$

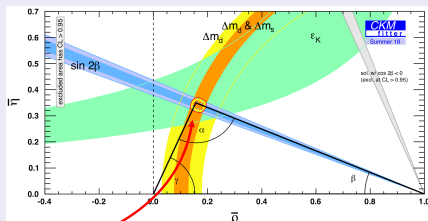
} Currently a $\sim 2\sigma$ tension



Tree-level constraints



Loop-level constraints



NP?

The B_s^0 unitarity triangle

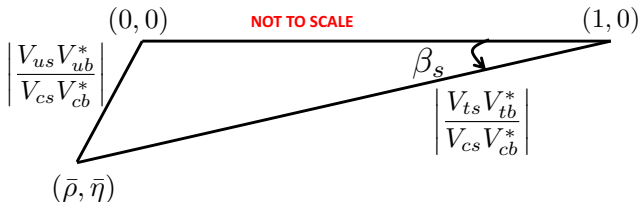
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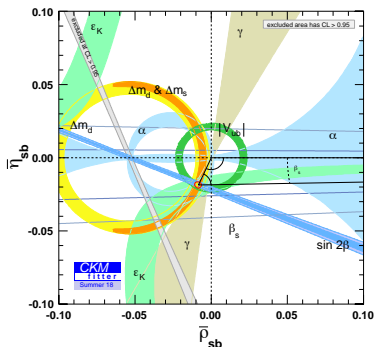


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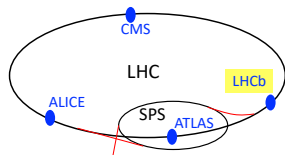
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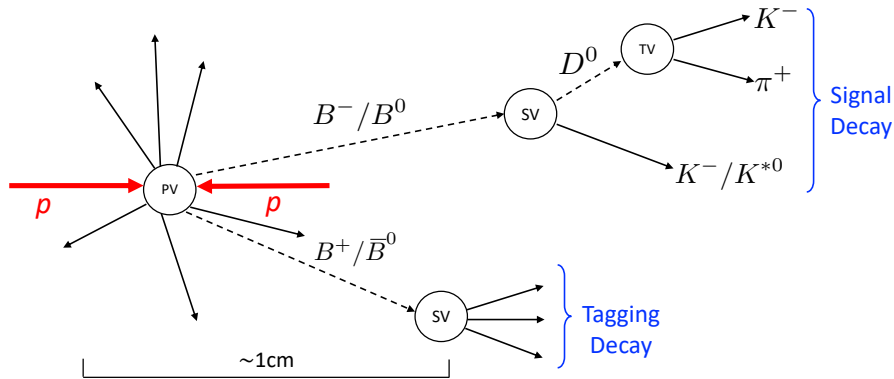
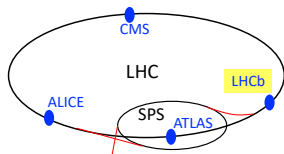
Why LHCb?

- ▶ Copious production of B^+ , B^0 , B_s^0 , Λ_b^0 ($100\text{K } b\bar{b}/\text{s}$)
- ▶ **LHCb detector** is specifically designed to study them



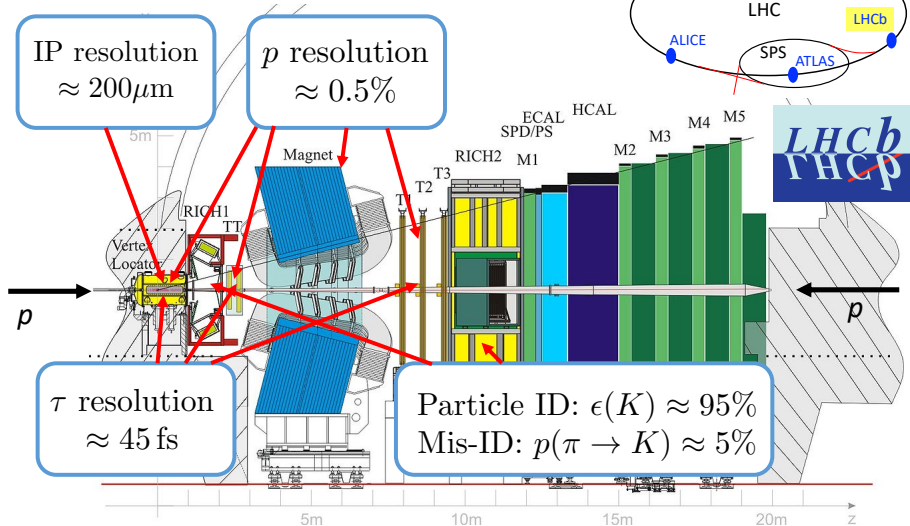
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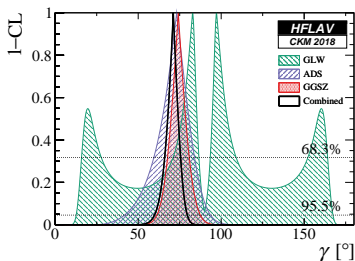
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1. Measurements of γ

- ▶ Theoretically clean, $\sigma_\gamma/\gamma \sim \mathcal{O}(10^{-7})$
- ▶ Experimentally challenging, $BR \sim \mathcal{O}(10^{-7})$
- ▶ Historically poorly known
- ▶ In 10 years will become *the* precision benchmark for SM CKM measurements

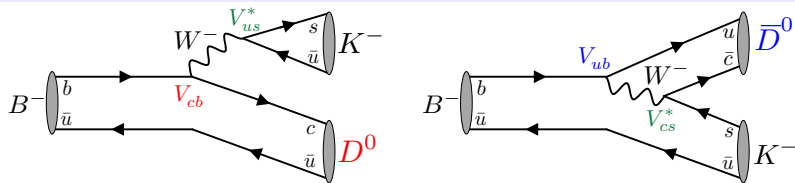
World average for γ



- ▶ Total of 136 input observables
- ▶ From 40 different measurements
- ▶ Across 6 different experiments

- ▶ γ is the phase between $V_{ub}^* V_{ud}$ and $V_{cb}^* V_{cd}$
 - ▶ Require interference between $b \rightarrow cW$ and $b \rightarrow uW$ to access it
 - ▶ No dependence on CKM elements involving the top
 - ▶ Can be measured using tree level B decays
- ▶ The “textbook” case is $B^\pm \rightarrow \bar{D}^0 K^\pm$:
 - ▶ Transitions themselves have different final states (D^0 and \bar{D}^0)
 - ▶ Interference occurs when D^0 and \bar{D}^0 decay to the same final state f

Reconstruct the D^0/\bar{D}^0 in a final state accessible to both to achieve interference



- ▶ The crucial feature of these (and similar) decays is that the D^0 can be reconstructed in several different final states [all have same weak phase γ]

Categorise decays sensitive to γ depending on the $\bar{D}^0 \rightarrow f$ final state

Optimal sensitivity is only achieved when combining them all together

▶ GLW

▶ CP eigenstates e.g. $D \rightarrow KK$, $D \rightarrow \pi\pi$

▶ [Phys. Lett. B253 (1991) 483]

▶ [Phys. Lett. B265 (1991) 172]

▶ ADS

▶ CF or DCS decays e.g. $D \rightarrow K\pi$

▶ [Phys. Rev. D63 (2001) 036005]

▶ [Phys. Rev. Lett. 78 (1997) 3257]

▶ GGSZ

▶ 3-body final states e.g. $D \rightarrow K_S^0 \pi\pi$

▶ [Phys. Rev. D68 (2003) 054018]

▶ TD (Time-dependent)

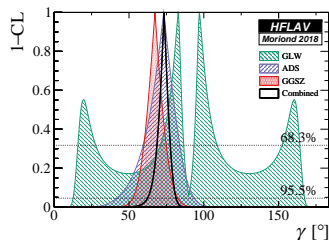
▶ Interference between mixing and decay e.g. $B_s^0 \rightarrow D_s^- K^+$ [phase is $(\gamma - 2\beta_s)$]

▶ Penguin free measurement of $\phi_s?$

▶ Dalitz

▶ Look at 3-body B decays with D^0 or \bar{D}^0 in the final state, e.g. $B^0 \rightarrow \bar{D}^0 K^+ \pi^-$

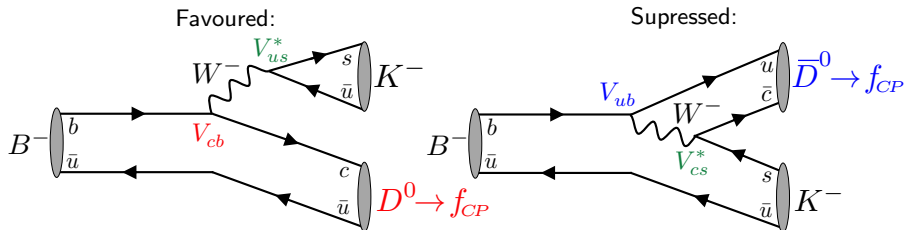
▶ [Phys. Rev. D79 (2009) 051301]



1.1 The GLW Method

γ with CP eigenstates (GLW)

- ▶ Use the $B^\pm \rightarrow \bar{D}^0 K^\pm$ case as an example:
 - ▶ Consider only D decays to CP eigenstates, f_{CP}
 - ▶ Favoured: $b \rightarrow c$ with strong phase δ_F and weak phase ϕ_F
 - ▶ Supressed: $b \rightarrow u$ with strong phase δ_S and weak phase ϕ_S



Subsequent amplitude to final state f_{CP} is:

$$B^- : A_f = |F|e^{i(\delta_F - \phi_F)} + |S|e^{i(\delta_S - \phi_S)} \quad (1)$$

$$B^+ : \bar{A}_f = |F|e^{i(\delta_F + \phi_F)} + |S|e^{i(\delta_S + \phi_S)} \quad (2)$$

because strong phases (δ) don't change sign under CP while weak phases (ϕ) do

γ with CP eigenstates (GLW)

- ▶ Can define the sum and difference of rates with B^+ and B^-

Rate difference and sum

$$|\bar{A}_f|^2 - |A_f|^2 = 2|F||S| \sin(\delta_F - \delta_S) \sin(\phi_F - \phi_S) \quad (3)$$

$$|\bar{A}_f|^2 + |A_f|^2 = |F|^2 + |S|^2 + 2|F||S| \cos(\delta_F - \delta_S) \cos(\phi_F - \phi_S) \quad (4)$$

- ▶ Choose $r_B = \frac{|S|}{|F|}$ (so that $r < 1$) and use strong phase difference $\delta_B = \delta_F - \delta_S$
- ▶ γ is the weak phase difference $\phi_F - \phi_S$
- ▶ Subsequently have two **experimental observables** which are

GLW CP asymmetry

$$A_{CP} = \frac{\pm 2r_B \sin(\delta_B) \sin(\gamma)}{1 + r_B^2 \pm 2r_B \cos(\delta_B) \cos(\gamma)}$$

GLW total rate

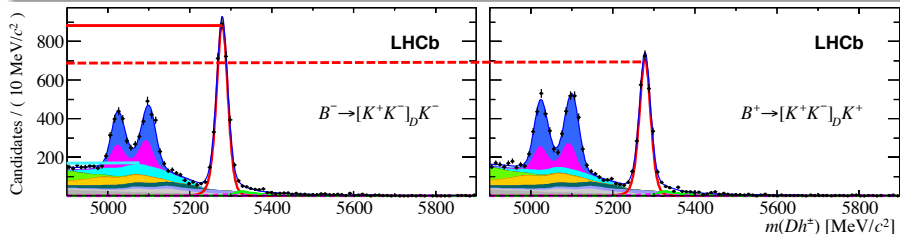
$$\mathcal{R}_{CP} = 1 + r_B^2 \pm 2r_B \cos(\delta_B) \cos(\gamma)$$

- ▶ The $+(-)$ sign corresponds to CP -even (-odd) final states
- ▶ Note that r_B and δ_B (ratio and strong phase difference of favoured and suppressed modes) are different for each B decay
- ▶ **The value of γ is shared by all such decays**

GLW observables

$$A_{CP} = \frac{\Gamma(B^- \rightarrow D_{CP}^0 K^-) - \Gamma(B^+ \rightarrow D_{CP}^0 K^+)}{\Gamma(B^- \rightarrow D_{CP}^0 K^-) + \Gamma(B^+ \rightarrow D_{CP}^0 K^+)} = \frac{\pm 2r_B \sin(\delta_B) \sin(\gamma)}{1 + r_B^2 \pm 2r_B \cos(\delta_B) \cos(\gamma)} \quad (1)$$

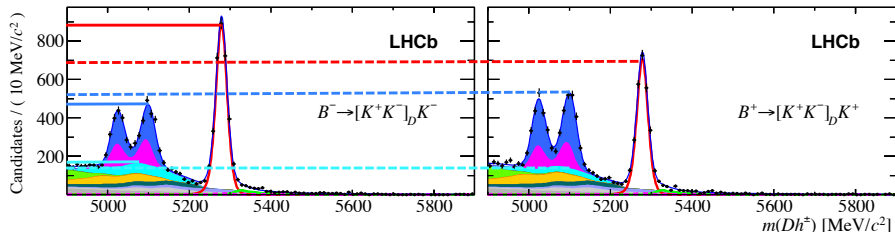
$$R_{CP} = \frac{\Gamma(B^- \rightarrow D_{CP}^0 K^-) + \Gamma(B^+ \rightarrow D_{CP}^0 K^+)}{\Gamma(B^- \rightarrow D^0 K^-) + \Gamma(B^+ \rightarrow D^0 K^+)} = 1 + r_B^2 \pm 2r_B \cos(\delta_B) \cos(\gamma) \quad (2)$$



GLW observables

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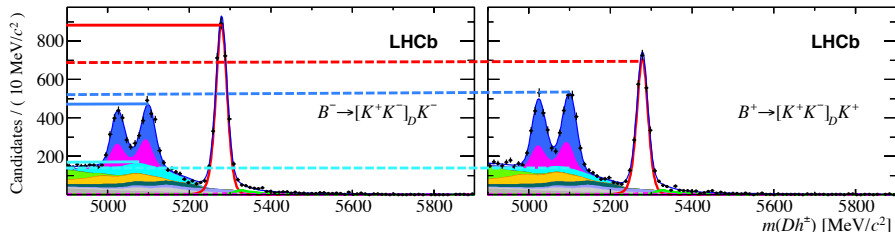


- ▶ LHCb has recently extracted GLW observables from partially reconstructed $B^- \rightarrow D^{*0} K^-$ in the same fit - [[arXiv:1708.06370](https://arxiv.org/abs/1708.06370)]

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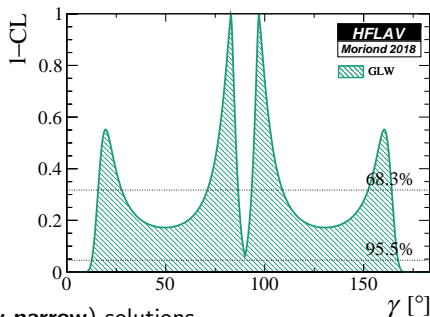


- ▶ LHCb has recently extracted GLW observables from partially reconstructed $B^- \rightarrow D^{*0} K^-$ in the same fit - [[arXiv:1708.06370](https://arxiv.org/abs/1708.06370)]
- ▶ Can extend to quasi-CP-eigenstates ($D^0 \rightarrow KK\pi^0$) if fraction of CP content, F^+ , is known

GLW observables

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- ▶ Multiple (**but very narrow**) solutions
- ▶ Require knowledge of F^+ from charm friends

1.2 The ADS Method

γ with CF and DCS decays (ADS)

- ▶ A 2-body D decay to final state f accessible to both D^0 and \bar{D}^0 can be
 - ▶ Cabibbo-favoured (CF) - $D^0 \rightarrow \pi^- K^+$
 - ▶ Doubly-Cabibbo-supressed (DCS) - $\bar{D}^0 \rightarrow \pi^- K^+$
- ▶ Introduces 2 new hadronic parameters:
 - ▶ r_D - ratio of magnitudes for D^0 and \bar{D}^0 decay to f
 - ▶ δ_D - relative phase for D^0 and \bar{D}^0 decay to f
- ▶ Gives a modified asymmetry and rate definition

ADS asymmetry

$$\mathcal{A}_{ADS} = \frac{2r_D r_B \sin(\delta_B + \delta_D) \sin(\gamma)}{r_D^2 + r_B^2 + 2r_D r_B \cos(\delta_B + \delta_D) \cos(\gamma)}$$

ADS ratio

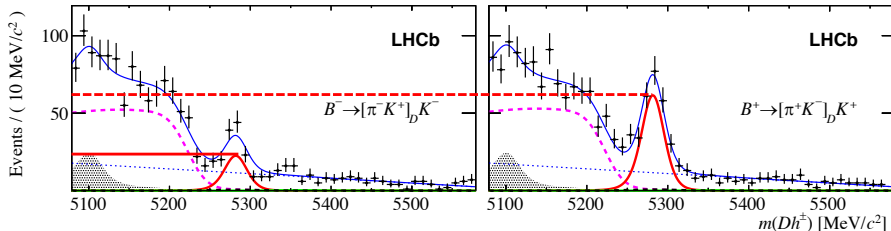
$$\mathcal{R}_{ADS} = \frac{|\bar{A}_f|^2 + |A_f|^2}{|\bar{A}_f|^2 + |A_f|^2} = r_B^2 + r_D^2 + 2r_D r_B \cos(\delta_B + \delta_D) \cos(\gamma)$$

- ▶ Hadronic parameters r_D and δ_D can be determined independently (using CLEO data and HFAG averages)

ADS observables

$$A_{ADS} = \frac{\Gamma(B^- \rightarrow [K^+\pi^-]_D K^-) - \Gamma(B^+ \rightarrow [K^-\pi^+]_D K^+)}{\Gamma(B^- \rightarrow [K^+\pi^-]_D K^-) + \Gamma(B^+ \rightarrow [K^-\pi^+]_D K^+)} = \frac{2r_B r_D \sin(\delta_B + \delta_D) \sin(\gamma)}{r_B^2 + r_D^2 + 2r_B r_D \cos(\delta_B + \delta_D) \cos(\gamma)}$$

$$R_{ADS} = \frac{\Gamma(B^- \rightarrow [K^+\pi^-]_D K^-) + \Gamma(B^+ \rightarrow [K^-\pi^+]_D K^+)}{\Gamma(B^- \rightarrow [K^-\pi^+]_D K^-) + \Gamma(B^+ \rightarrow [K^+\pi^-]_D K^+)} = r_B^2 + r_D^2 + 2r_B r_D \cos(\delta_B + \delta_D) \cos(\gamma)$$

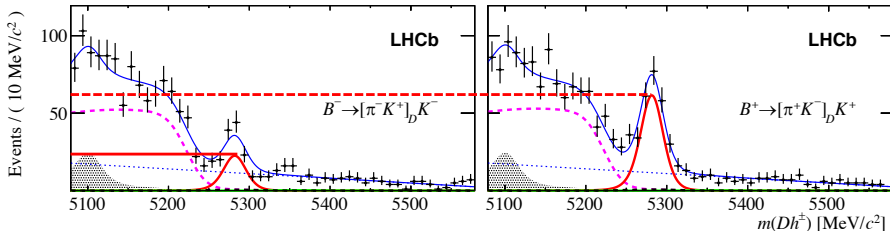


- ▶ Much harder to extract partially reconstructed observables because of $B_s^0 \rightarrow D^{(*)0} K^+ \pi^-$ backgrounds.

ADS observables

$$A_{ADS} = \frac{\Gamma(B^- \rightarrow [K^+\pi^-]_D K^-) - \Gamma(B^+ \rightarrow [K^-\pi^+]_D K^+)}{\Gamma(B^- \rightarrow [K^+\pi^-]_D K^-) + \Gamma(B^+ \rightarrow [K^-\pi^+]_D K^+)} = \frac{2r_B r_D \kappa_D \sin(\delta_B + \delta_D) \sin(\gamma)}{r_B^2 + r_D^2 + 2r_B r_D \kappa_D \cos(\delta_B + \delta_D) \cos(\gamma)}$$

$$R_{ADS} = \frac{\Gamma(B^- \rightarrow [K^+\pi^-]_D K^-) + \Gamma(B^+ \rightarrow [K^-\pi^+]_D K^+)}{\Gamma(B^- \rightarrow [K^-\pi^+]_D K^-) + \Gamma(B^+ \rightarrow [K^+\pi^-]_D K^+)} = \frac{r_B^2 + r_D^2 + 2r_B r_D \kappa_D \cos(\delta_B + \delta_D) \cos(\gamma)}{r_B^2 + r_D^2 + 2r_B r_D \kappa_D \cos(\delta_B + \delta_D) \cos(\gamma)}$$

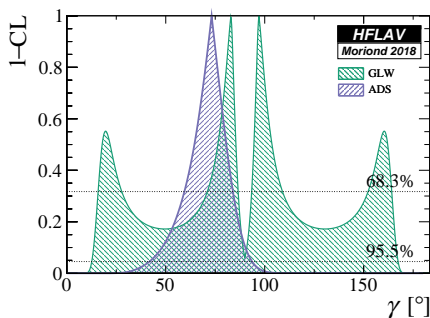


- ▶ Much harder to extract partially reconstructed observables because of $B_s^0 \rightarrow D^{(*)0} K^+ \pi^-$ backgrounds.
- ▶ Can extend to multibody-DCS-decays ($D^0 \rightarrow K \pi \pi^0$) if dilution from interference, κ_D , is known

ADS observables

$$A_{ADS} = \frac{\Gamma(B^- \rightarrow [K^+\pi^-]_D K^-) - \Gamma(B^+ \rightarrow [K^-\pi^+]_D K^+)}{\Gamma(B^- \rightarrow [K^+\pi^-]_D K^-) + \Gamma(B^+ \rightarrow [K^-\pi^+]_D K^+)} = \frac{2r_B r_D \kappa_D \sin(\delta_B + \delta_D) \sin(\gamma)}{r_B^2 + r_D^2 + 2r_B r_D \kappa_D \cos(\delta_B + \delta_D) \cos(\gamma)}$$

$$R_{ADS} = \frac{\Gamma(B^- \rightarrow [K^+\pi^-]_D K^-) + \Gamma(B^+ \rightarrow [K^-\pi^+]_D K^+)}{\Gamma(B^- \rightarrow [K^-\pi^+]_D K^-) + \Gamma(B^+ \rightarrow [K^+\pi^-]_D K^+)} = \frac{r_B^2 + r_D^2 + 2r_B r_D \kappa_D \cos(\delta_B + \delta_D) \cos(\gamma)}{r_B^2 + r_D^2 + 2r_B r_D \kappa_D \cos(\delta_B + \delta_D) \cos(\gamma)}$$



- ▶ A single (**yet broader**) solution
- ▶ Require knowledge of r_D , δ_D , κ_D from charm friends

1.3 The GGSZ Method

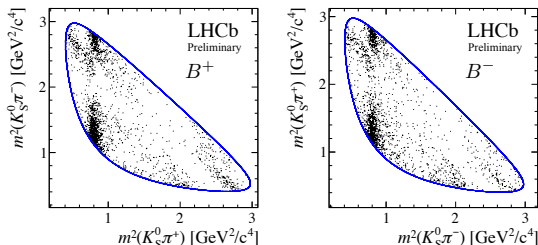
γ with 3-body self-conjugate states (GGSZ)

- ▶ Now get additional sensitivity over the 3-body phase space
- ▶ Idea is to perform a GLW/ADS type analysis across the D decay phase space
- ▶ For example $D^0 \rightarrow K_S^0 \pi^+ \pi^-$ has contributions from
 - ▶ Singly-Cabibbo-suppressed decay $D^0 \rightarrow K_S^0 \rho^0$
 - ▶ Doubly-Cabibbo-suppressed decay $D^0 \rightarrow K^{*+} \pi^-$
 - ▶ Interference between them enhances sensitivity and resolves ambiguities in γ

GGSZ observables (partial rate as function of Dalitz position)

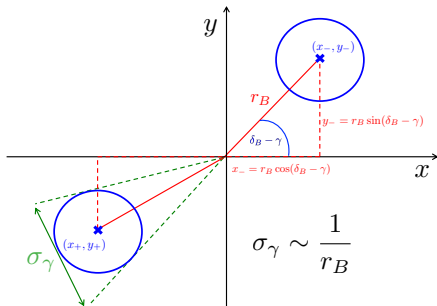
$$d\Gamma_{B^\pm(\mathbf{x})} = A_{(\pm, \mp)}^2 + r_B^2 A_{(\mp, \pm)}^2 + 2A_{(\pm, \mp)} A_{(\mp, \pm)} [r_B \cos(\delta_B \pm \gamma) \cos(\delta_{D(\pm, \mp)}) + r_B \sin(\delta_B \pm \gamma) \sin(\delta_{D(\pm, \mp)})] \quad (3)$$

From [LHCb-PAPER-2018-017]



GGSZ observables (partial rate as function of Dalitz position)

$$d\Gamma_{B^\pm(\mathbf{x})} = A_{(\pm, \mp)}^2 + r_B^2 A_{(\mp, \pm)}^2 + 2A_{(\pm, \mp)}A_{(\mp, \pm)} \left[\underbrace{r_B \cos(\delta_B \pm \gamma)}_{x_\pm} \underbrace{\cos(\delta_{D(\pm, \mp)})}_{c_j} + \underbrace{r_B \sin(\delta_B \pm \gamma)}_{y_\pm} \underbrace{\sin(\delta_{D(\pm, \mp)})}_{s_j} \right] \quad (4)$$

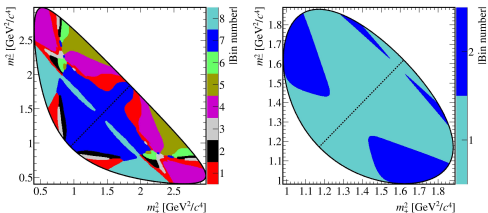


- ▶ $x_\pm + iy_\pm = r_B e^{i(\delta_B \pm \gamma)}$
- ▶ **Uncertainty on γ is inversely proportional to central value of hadronic unknown!!**
- ▶ Fluctuation in nuisance parameter = fluctuation in error on parameter of interest!

Model-independent GGSZ Analysis

- ▶ Consider both $D \rightarrow K_S^0 \pi \pi$ and $D \rightarrow K_S^0 K K$ decays
- ▶ Divide up the Dalitz space into $2N$ symmetric bins chosen to optimise sensitivity to γ

[LHCb-PAPER-2018-017]



Decay amplitude is a superposition of suppressed and favoured contributions

$$A_B(m_-^2, m_+^2) \propto A_D(m_-^2, m_+^2) + r_B e^{i(\delta_B - \gamma)} A_{\bar{D}}(m_-^2, m_+^2)$$

Expected number of B^+ (B^-) events in bin i

$$N_{\pm i}^+ = h_{B^+} \left[F_{\mp i} + (x_+^2 + y_+^2) F_{\pm i} + 2\sqrt{F_i F_{-i}} (x_+ c_{\pm i} - y_+ s_{\pm i}) \right]$$

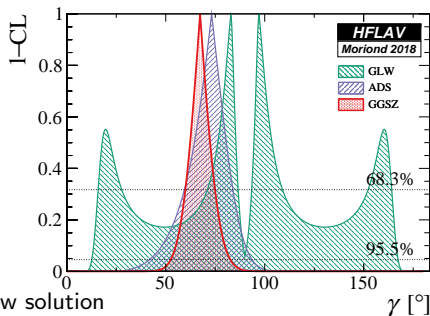
$$N_{\pm i}^- = h_{B^-} \left[F_{\pm i} + (x_-^2 + y_-^2) F_{\mp i} + 2\sqrt{F_i F_{-i}} (x_- c_{\pm i} - y_- s_{\pm i}) \right]$$

- ▶ $N_{\pm i}^{\pm}$ - events in each bin
- ▶ $F_{\pm i}$ - from $B \rightarrow D^{*\pm} \mu^{\mp} \nu_{\mu} X$
- ▶ c_i, s_i - from CLEO-c (QC $D^0 \bar{D}^0$) measurements
- ▶ $h_{B^{\pm}}$ - overall normalisation

Expected number of B^+ (B^-) events in bin i

$$N_{\pm i}^+ = h_{B^+} \left[F_{\mp i} + (x_+^2 + y_+^2) F_{\pm i} + 2\sqrt{F_i F_{-i}} (x_+ c_{\pm i} - y_+ s_{\pm i}) \right]$$

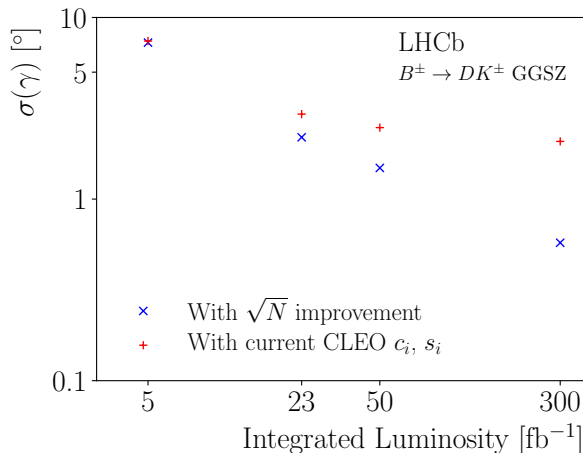
$$N_{\pm i}^- = h_{B^-} \left[F_{\pm i} + (x_-^2 + y_-^2) F_{\mp i} + 2\sqrt{F_i F_{-i}} (x_- c_{\pm i} - y_- s_{\pm i}) \right]$$



- ▶ A single and narrow solution
- ▶ Require knowledge of $c_{\pm i}$ and $s_{\pm i}$ from charm friends

A comment on GGSZ systematics

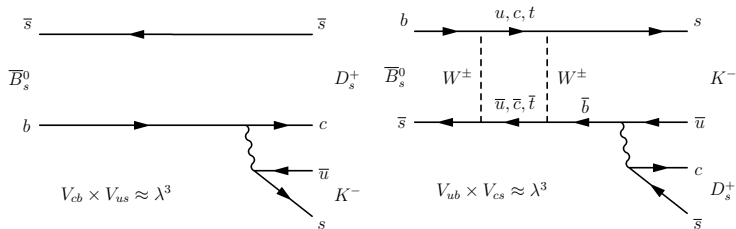
- ▶ Sensitivity to γ starts to degrade due to dependence on input from charm sector
- ▶ Measurements from BES-III (Beijing) will be vital to achieve ultimate precision on γ



1.4 The TD Method

The time-dependent method with $B_s^0 \rightarrow D_s^\mp K^\pm$

- ▶ B_s^0 and \bar{B}_s^0 can both decay to same final state $D_s^\mp K^\pm$ (one via $b \rightarrow cW$, the other via $b \rightarrow uW$)
- ▶ Interference achieved by neutral B_s^0 mixing (requires knowledge of $-2\beta_s \equiv \phi_s$)
 - ▶ Weak phase difference is $(\gamma - 2\beta_s)$



- ▶ Requires tagging the initial B_s^0 flavour
- ▶ Requires a time-dependent analysis to observe the meson oscillations
- ▶ Fit the decay-time-dependent decay rates
- ▶ Also requires knowledge of Γ_s , $\Delta\Gamma_s$, Δm_s

The time-dependent method with $B_s^0 \rightarrow D_s^\mp K^\pm$

Time-dependent decay rate for initial B_s^0 or \bar{B}_s^0 at $t = 0$

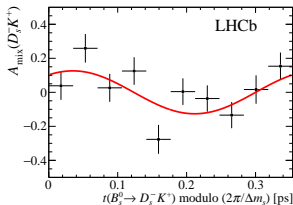
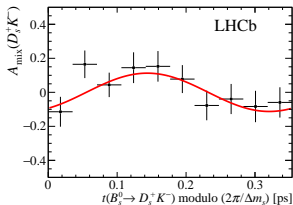
$$\begin{aligned}\frac{d\Gamma_{B_s^0 \rightarrow f}(t)}{dt} &\propto e^{-\Gamma_s t} \left[\cosh\left(\frac{\Delta\Gamma_s t}{2}\right) + A_f^{\Delta\Gamma_s} \sinh\left(\frac{\Delta\Gamma_s t}{2}\right) \right. \\ &\quad \left. + C_f \cos(\Delta m_s t) - S_f \sin(\Delta m_s t) \right] \\ \frac{d\Gamma_{\bar{B}_s^0 \rightarrow f}(t)}{dt} &\propto e^{-\Gamma_s t} \left[\cosh\left(\frac{\Delta\Gamma_s t}{2}\right) + A_f^{\Delta\Gamma_s} \sinh\left(\frac{\Delta\Gamma_s t}{2}\right) \right. \\ &\quad \left. - C_f \cos(\Delta m_s t) + S_f \sin(\Delta m_s t) \right]\end{aligned}$$

Time-dependent rate asymmetry

$$\mathcal{A}_{CP}(t) = \frac{\Gamma_{\bar{B}_s^0 \rightarrow f}(t) - \Gamma_{B_s^0 \rightarrow f}(t)}{\Gamma_{\bar{B}_s^0 \rightarrow f}(t) + \Gamma_{B_s^0 \rightarrow f}(t)} = \frac{S_f \sin(\Delta m_s t) - C_f \cos(\Delta m_s t)}{\cosh\left(\frac{\Delta\Gamma_s t}{2}\right) + A_f^{\Delta\Gamma_s} \sinh\left(\frac{\Delta\Gamma_s t}{2}\right)}$$

The time-dependent method with $B_s^0 \rightarrow D_s^\mp K^\pm$

► Fit for decay-time-dependent asymmetry

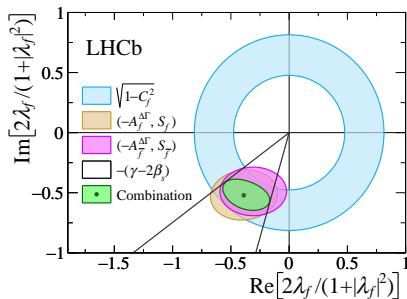


Variable definitions

$$C_f = -C_{\bar{f}} = \frac{1 - r_B^2}{1 + r_B^2}$$

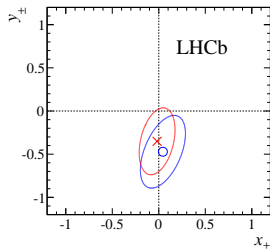
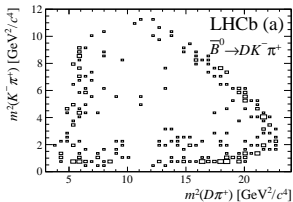
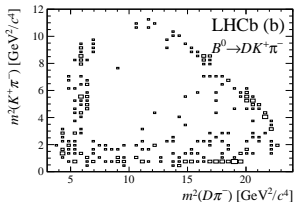
$$A_{f(\bar{f})}^{\Delta\Gamma_s} = \frac{-2r_B \cos(\gamma - 2\beta_s \mp \delta_B)}{1 + r_B^2}$$

$$S_{f(\bar{f})} = \frac{\pm 2r_B \sin(\gamma - 2\beta_s \mp \delta_B)}{1 + r_B^2}$$



Dalitz methods

- ▶ Study Dalitz structure of 3-body B decays with $B^0 \rightarrow DK^+ \pi^-$
 - ▶ In principle has excellent sensitivity to γ
 - ▶ “GW method”? (Gershon-Williams - [arXiv:0909.1495])
- ▶ Get multiple interfering resonances which increase sensitivity to γ
 - ▶ $D^{*0}(2400)^-$, $D^{*2}(2460)^-$, $K^*(892)^0$, $K^*(1410)^0$, $K^*_2(1430)^0$
- ▶ Fit B decay Dalitz Plot for cartesian parameters (similar to GGSZ except for the B not the D)
 - ▶ $D \rightarrow K^+ K^-$, $D \rightarrow \pi^+ \pi^-$ - GLW-Dalitz (done by LHCb - [arXiv:1602.03455])
 - ▶ $D \rightarrow K^\pm \pi^\mp$ - ADS-Dalitz (problematic backgrounds from $B_s^0 \rightarrow DK^\pm \pi^\mp$)
 - ▶ $D \rightarrow K_S^0 \pi^+ \pi^-$ - GGSZ-Dalitz (double Dalitz!)



Building up sensitivity

Different B decays

$$B^\pm \rightarrow DK^\pm$$

r_B^{DK}, δ_B^{DK}

$$B^\pm \rightarrow D^*K^\pm$$

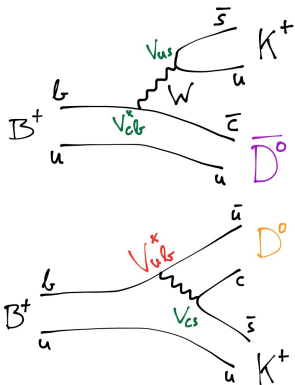
$r_B^{D^*K}, \delta_B^{D^*K}$

$$B^\pm \rightarrow DK^{*\pm}$$

$r_B^{DK^*}, \delta_B^{DK^*}$

$$B^0 \rightarrow DK^{*0}$$

$r_B^{DK^{*0}}, \delta_B^{DK^{*0}}$



Different B decays

$$B^\pm \rightarrow DK^\pm$$

r_B^{DK}, δ_B^{DK}

$$B^\pm \rightarrow D^*K^\pm$$

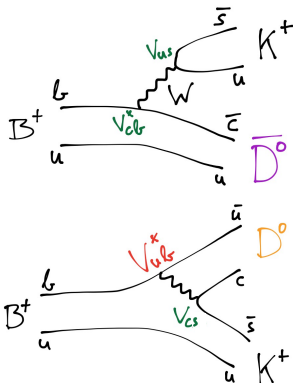
$r_B^{D^*K}, \delta_B^{D^*K}$

$$B^\pm \rightarrow DK^{*\pm}$$

$r_B^{DK^*}, \delta_B^{DK^*}$

$$B^0 \rightarrow DK^{*0}$$

$r_B^{DK^{*0}}, \delta_B^{DK^{*0}}$



$$D \rightarrow hh$$

$$D \rightarrow hh\pi^0 \quad F^+$$

$$D \rightarrow hhhh \quad F^+$$

$$D \rightarrow hh' \quad r_D, \delta_D$$

$$D \rightarrow hh'\pi^0 \quad r_D, \delta_D, \kappa_D$$

$$D \rightarrow hh'hh \quad r_D, \delta_D, \kappa_D$$

$$D \rightarrow K_S hh \quad c_i, s_i$$

Different D decays

MANY NUISANCE PARAMETERS

LHCb Input Status

Method		B Decay D Decay		Highest Statistics	Poorer sensitivity		High potential (Dalitz structure of B)		Low stats (multibody B)
				$B^- \rightarrow D^0 K^-$	$B^- \rightarrow D^0 K^{*-}$ [$K^{*-} \rightarrow K_s^0 \pi^-$]	$B^- \rightarrow D^{*0} K^-$ [$D^{*0} \rightarrow D^0 \pi^0$], [$D^{*0} \rightarrow D^0 \gamma$]		$B^0 \rightarrow D^0 K^+ \pi^-$	
					part-rec	full-rec	K^{*0} res	Dalitz	
GLW	(+) <ul style="list-style-type: none"> $D^0 \rightarrow K^+ K^-$ $D^0 \rightarrow \pi^+ \pi^-$ $D^0 \rightarrow K^+ K^- \pi^0$ $D^0 \rightarrow \pi^+ \pi^- \pi^0$ $D^0 \rightarrow K^+ K^- \pi^+ \pi^-$ $D^0 \rightarrow \pi^+ \pi^- \pi^+ \pi^-$ 	5 fb^{-1}	5 fb^{-1}	5 fb^{-1}	•	$3 \text{ fb}^{-1}(\bullet)$	3 fb^{-1}	3 fb^{-1}	
		5 fb^{-1}	5 fb^{-1}	5 fb^{-1}	•	$3 \text{ fb}^{-1}(\bullet)$	3 fb^{-1}	3 fb^{-1}	
		$3 \text{ fb}^{-1}(\bullet)$	-	-	-	-	-	-	-
		3 fb^{-1}	-	-	-	-	-	-	-
		•	-	-	-	-	-	-	-
		$3 \text{ fb}^{-1}(\bullet)$	5 fb^{-1}	•	•	•	-	-	-
ADS	(-) <ul style="list-style-type: none"> $D^0 \rightarrow K_s^0 \pi^0$ 	•	-	-	-	-	-	-	
		$3 \text{ fb}^{-1}(\bullet)$	5 fb^{-1}	•	•	$3 \text{ fb}^{-1}(\bullet)$	•	3 fb^{-1}	
		3 fb^{-1}	-	-	-	-	-	-	
GGSZ	<ul style="list-style-type: none"> $D^0 \rightarrow K^+ \pi^-$ $D^0 \rightarrow K^+ \pi^- \pi^0$ $D^0 \rightarrow K^+ \pi^- \pi^+ \pi^-$ 	$3 \text{ fb}^{-1}(\bullet)$	5 fb^{-1}	•	•	$3 \text{ fb}^{-1}(\bullet)$	•	3 fb^{-1}	
		3 fb^{-1}	-	-	-	-	-	-	
		$3 \text{ fb}^{-1}(\bullet)$	5 fb^{-1}	•	•	•	•	-	
		•	-	-	-	-	-	-	
GGSZ	<ul style="list-style-type: none"> $D^0 \rightarrow K_s^0 \pi^+ \pi^-$ $D^0 \rightarrow K_s^0 K^+ K^-$ $D^0 \rightarrow K_s^0 \pi^+ \pi^- \pi^0$ $D^0 \rightarrow K_s^0 K^+ K^- \pi^0$ 	5 fb^{-1}	•	-	•	$3 \text{ fb}^{-1}(\bullet)$	•	•	
		5 fb^{-1}	•	-	•	$3 \text{ fb}^{-1}(\bullet)$	•	•	
		•	-	-	-	-	-	-	
		•	-	-	-	-	-	-	

KEY: •: (update) in progress

•: requires input from Charm sector (r_D, δ_D, κ_D)

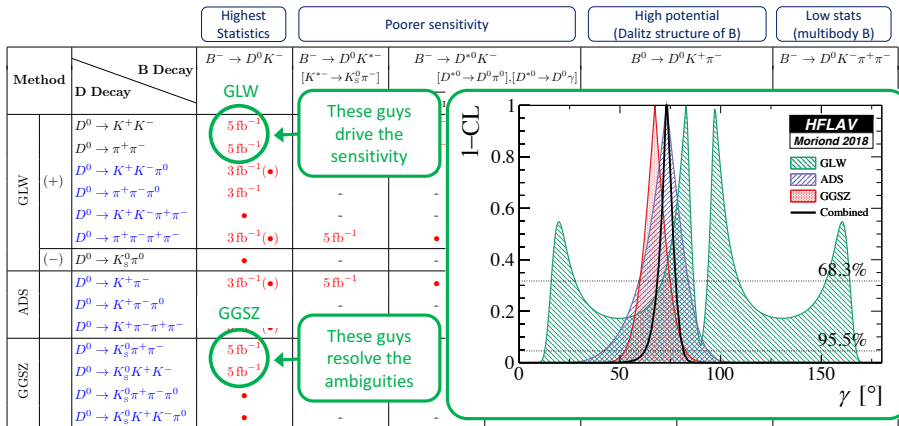
NOTE: TD result with $B_s^0 \rightarrow D_s^- K^+ 3 \text{ fb}^{-1}(\bullet)$

TD result with $B^0 \rightarrow D^- \pi^+ 3 \text{ fb}^{-1}$

GLS result from $B^- \rightarrow D^0 K^-$ with $D^0 \rightarrow K_s^0 K^\pm \pi^\mp 3 \text{ fb}^{-1}(\bullet)$

Working on $B^- \rightarrow D^0 K^{*-}$ with $K^{*-} \rightarrow K^- \pi^0$ •

LHCb Input Status



KEY: \bullet : (update) in progress

\bullet : requires input from Charm sector (r_D, δ_D, κ_D)

NOTE: TD result with $B_s^0 \rightarrow D_s^- K^+ 3 \text{ fb}^{-1} (\bullet)$

TD result with $B^0 \rightarrow D^- \pi^+ 3 \text{ fb}^{-1}$

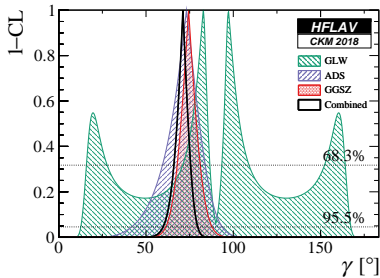
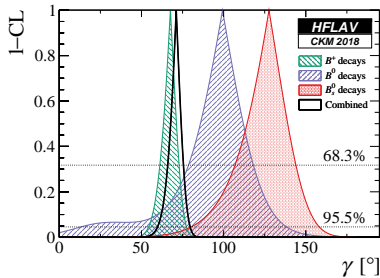
GLS result from $B^- \rightarrow D^0 K^-$ with $D^0 \rightarrow K_S^0 K^\pm \pi^\mp 3 \text{ fb}^{-1} (\bullet)$

Working on $B^- \rightarrow D^0 K^{*-}$ with $K^{*-} \rightarrow K^- \pi^0 \bullet$

Combined constraints on γ

World Average (HFLAV) - [Spring update]

$$\gamma = (71.1^{+4.6}_{-5.3})^\circ$$



Indirect constraints are: $\gamma = (65.3^{+1.0}_{-2.5})^\circ$ ($\sim 2\sigma$)

Comparison between B_s^0 and B^+ initial states $\sim 2\sigma$
($B_s^0 \rightarrow D_s^\mp K^\pm$ is hugely important for resolving this)

Sensitivity to tree-level Wilson coefficients

- ▶ We always say CKM angle γ is a SM benchmark with negligible theoretical uncertainty - $\mathcal{O}(10^{-7})^\circ$
- ▶ This is only true **if we assume no NP at tree-level**
- ▶ Brod, Lenz et. al [[Phys. Rev. D92 \(2015\) 033002](#)] show how much “wobble” room is in this assumption

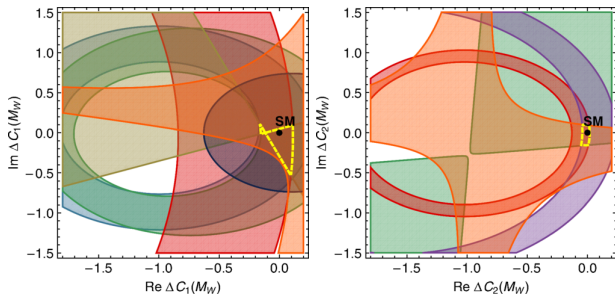
Effective Hamiltonian

$$\mathcal{H}_{\text{eff}} = \frac{G_F}{\sqrt{2}} V_{ub} V_{cs}^* [C_1 O_1 + C_2 O_2]$$

Interference terms require modification

$$\frac{\bar{\mathcal{A}}_f}{\mathcal{A}_f} \sim e^{-i\gamma} \rightarrow e^{-i\gamma} \left[1 + \mathcal{O} \left(\frac{\Delta C_1}{C_2} \right) \right]$$

$$C_1 = C_1^{SM} + \Delta C_1^{NP}$$
$$C_2 = C_2^{SM} + \Delta C_2^{NP}$$



- ▶ A NP contribution to C_1 or C_2 gives a modification to our amplitude ratio:

Modification of amplitude ratio

$$r_B e^{i(\delta_B \pm \gamma)} \rightarrow r_B e^{i(\delta_B \pm \gamma)} \left[1 + (r_{A'} - r_A) \frac{\Delta C_1^{NP}}{C_2} \right]$$

In particular note that:

$$\gamma \rightarrow \gamma \left[1 + (r_A - r_{A'}) \frac{\text{Im}(\Delta C_1^{NP})}{C_2} \right]$$

where r_A ($r_{A'}$) are hadronic unknowns representing the favoured (suppressed) colour singlet / rearranged amplitude ratio

- ▶ Can redefine all GLW/ADS/GGSZ relations shifting by a single complex NP contribution $A = (r_{A'} - r_A) \Delta C_1^{NP} / C_2$

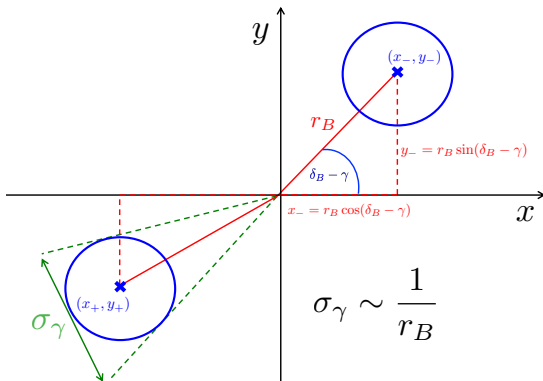
Modification of decay rate

$$\Gamma(B^\pm \rightarrow DK^\pm) \rightarrow \left| r_D e^{-i\delta_D} + r_B e^{i(\delta_B \pm \gamma)} (1 + A) \right|^2$$

Sensitivity to tree-level Wilson coefficients

Modification of decay rate

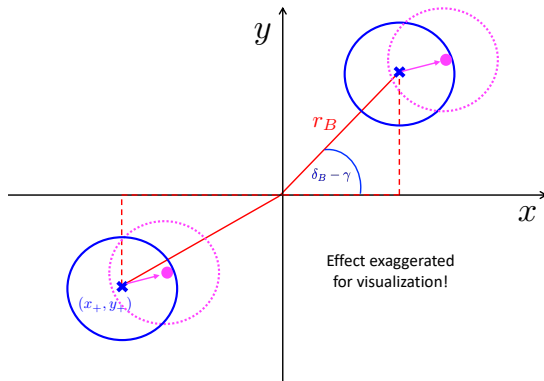
$$\Gamma(B^\pm \rightarrow DK^\pm) \rightarrow \left| r_D e^{-i\delta_D} + r_B e^{i(\delta_B \pm \gamma)} (1 + A) \right|^2$$



Sensitivity to tree-level Wilson coefficients

Modification of decay rate

$$\Gamma(B^\pm \rightarrow DK^\pm) \rightarrow \left| r_D e^{-i\delta_D} + r_B e^{i(\delta_B \pm \gamma)} (1 + A) \right|^2$$

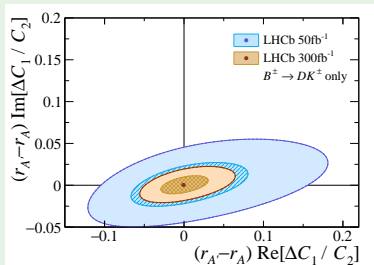


Sensitivity to tree-level Wilson coefficients

Sensitivity to generic NP contribution in complex number A

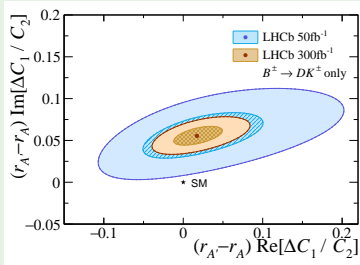
$$A = (r_{A'} - r_A) \frac{\Delta C_1^{NP}}{C_2}$$

Future exclusion profile for A



- What values of A can be excluded in the future

Using “still allowed” NP contribution



- Estimate $\Delta r = r_{A'} - r_A \approx 0.6$ and allow $\text{Im}(\Delta C_1^{NP}(m_b)) \sim \mathcal{O}(10\%)$

This includes only GLW, ADS and GGSZ modes for $B^{\pm} \rightarrow D^0 K^{\pm}$

Can do even more by including rates from other $b \rightarrow c/u$ processes:

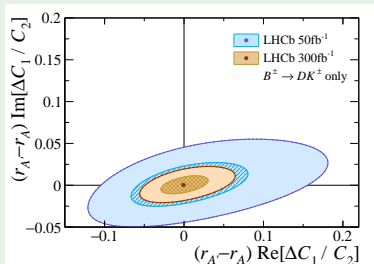
$$B \rightarrow D\pi, B \rightarrow D^{*0}h^0, B \rightarrow X_{d(s)}\gamma, a_{sl}^{d(s)}, B \rightarrow \pi\pi$$

Sensitivity to tree-level Wilson coefficients

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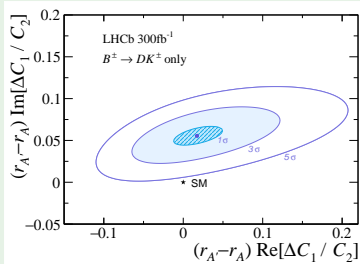
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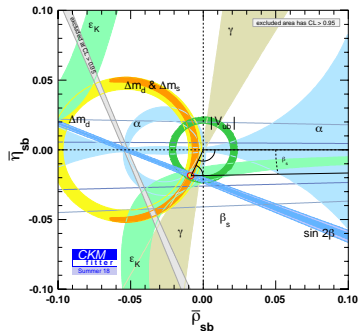
Can do even more by including rates from other $b \rightarrow c/u$ processes:

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2. Measurements of ϕ_s

“The B_s^0 unitarity triangle”

$$\underbrace{V_{us} V_{ub}^*}_{\sim \lambda^4} + \underbrace{V_{cs} V_{cb}^*}_{\sim \lambda^2} + \underbrace{V_{ts} V_{tb}^*}_{\sim \lambda^2} = 0$$



- CKM fits give a precise prediction for the **small** but **non-zero** value of β_s in the SM

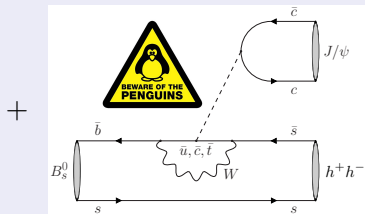
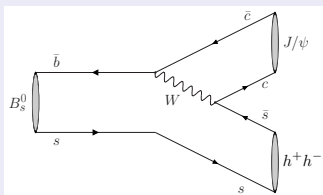
$$-2\beta_s = (-0.0370 \pm 0.0006) \text{ rad}$$

Sensitivity to ϕ_s

- ▶ The weak phase ϕ_s arises in the interference between decay and mixing of e.g. $B_s^0 \rightarrow f$ and $B_s^0 \rightarrow \bar{B}_s^0 \rightarrow f$

Golden mode: $B_s^0 \rightarrow J/\psi K^+ K^-$ - [Phys. Rev. Lett. 114 (2015) 041801]

$$\phi_s = \underbrace{\phi_{\text{SM}}}_{-2\beta_s} + \Delta\phi_{\text{peng}} + \Delta\phi_{\text{NP}}$$

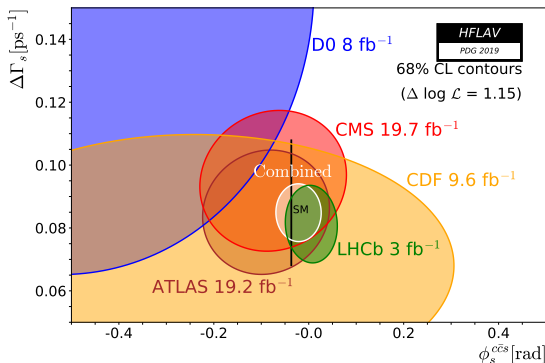


- ▶ Only for $b \rightarrow c\bar{c}s$ transitions ($\phi_s^{c\bar{c}}$)
- ▶ Estimate $\Delta\phi_{\text{peng}} \approx 0.003$ [JHEP 11 (2015) 082] ($B^0 \rightarrow J/\psi \rho$, $B_s^0 \rightarrow J/\psi K^{*0}$)

- ▶ World average for these modes currently dominated by LHCb
- ▶ Consistent with both the SM and zero - [[arXiv:1909.12524](https://arxiv.org/abs/1909.12524)]

$$\phi_s^{c\bar{c}}(\text{SM}) = (-0.0370 \pm 0.0006) \text{ rad}$$

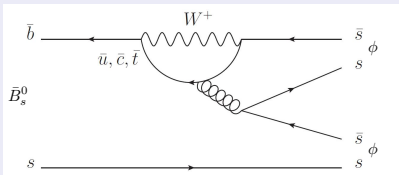
$$\phi_s^{c\bar{c}}(\text{WA}) = (-0.021 \pm 0.031) \text{ rad}$$



$B_s^0 \rightarrow \phi\phi$ decays

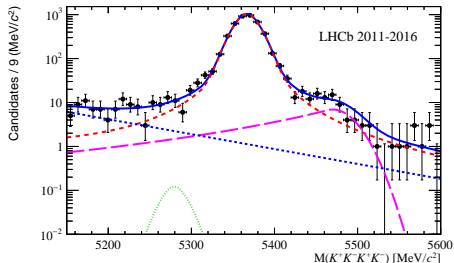
- ▶ **Pure penguin decay** - $b \rightarrow ss\bar{s}$ transition
- ▶ New Physics can be significantly enhanced
- ▶ Purely hadronic final state
- ▶ The ϕ resonance is very narrow

$B_s^0 \rightarrow \phi\phi$



$$\phi_s^{s\bar{s}} = (-0.073 \pm 0.115 \pm 0.027) \text{ rad}$$

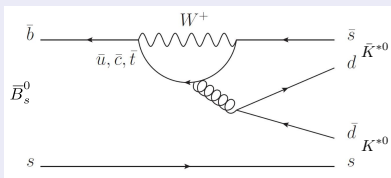
[arXiv:1907.10003]



$B_s^0 \rightarrow (K^+\pi^-)(K^-\pi^+)$ decays

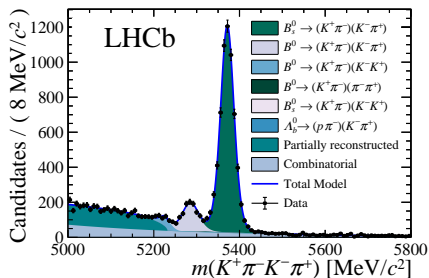
- ▶ **Pure penguin decay** - $b \rightarrow sd\bar{d}$ transition
- ▶ New Physics can be significantly enhanced and entirely different from $B_s^0 \rightarrow J/\psi\phi$ and $B_s^0 \rightarrow \phi\phi$
- ▶ Expect similar statistical precision to $B_s^0 \rightarrow \phi\phi$
- ▶ CPV in decay is also possible

$$B_s^0 \rightarrow K^{*0} \bar{K}^{*0}$$



$$\phi_s^{d\bar{d}} = (-0.10 \pm 0.13 \pm 0.14) \text{ rad}$$

[JHEP 03 (2018) 140]



$$\phi_s^{c\bar{c}} \neq \phi_s^{s\bar{s}} \neq \phi_s^{d\bar{d}}$$

Measurement of ϕ_s in $B_{(s)}^0 \rightarrow (K^+\pi^-)(K^-\pi^+)$ decays

- ▶ **A combined B^0 and $B_s^0 \rightarrow (K^+\pi^-)(K^-\pi^+)$ analysis** would be very powerful
- ▶ The SU(3) partner B^0 mode is a $\Delta S = 0$ transition and expected to have a much smaller NP contribution
- ▶ Allows for much easier theory interpretation as B^0 mode sets a SM benchmark for comparison with B_s^0 mode
- ▶ **Simplified time-dependent rate asymmetry for each polarization amplitude**

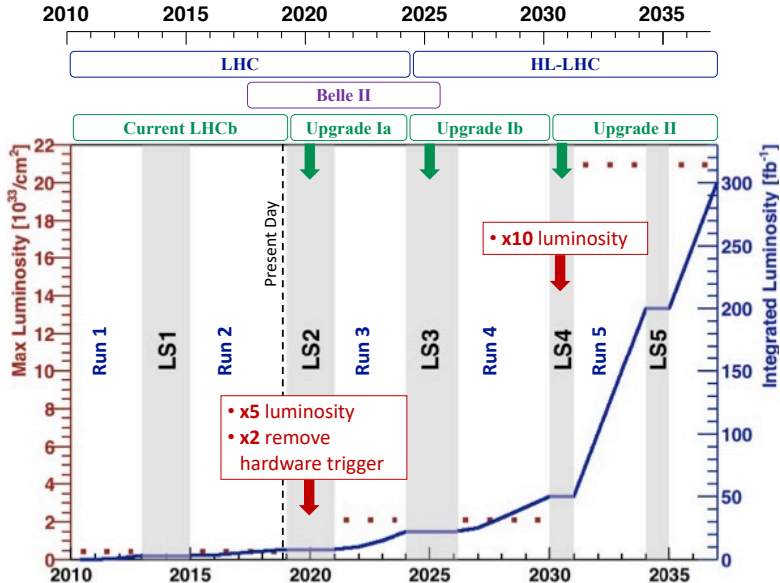
$$A_{CP}(t) \approx (1 - 2w)e^{-\frac{1}{2}\Delta m_s^2 \sigma_t^2} \eta_f \sin(\phi_s) \sin(\Delta m_s t)$$

Experimentally challenging and requires use of LHCb's full armoury

- ▶ Need to **tag** initial B flavour
- ▶ Decay-time dependence (**1 time dimension**)
- ▶ Separate various wide K^* contributions (**2 mass dimensions**)
- ▶ Separate different spin components (**3 angular dimensions**)
- ▶ Purely hadronic final state

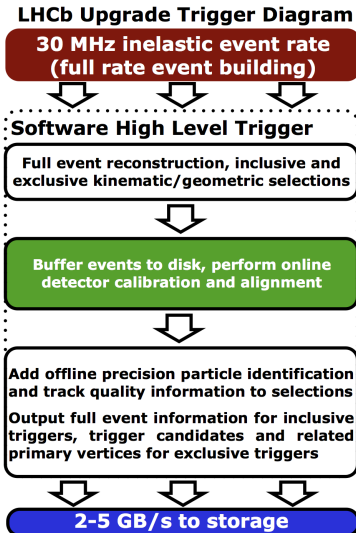
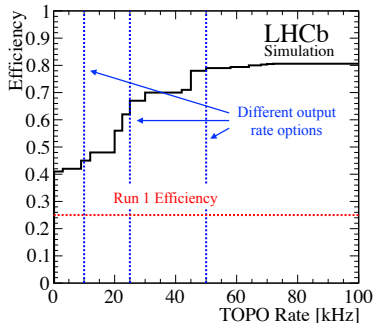
Summary and Outlook

Future prospects



Future prospects

- ▶ **LHCb Upgrade** will be installed in LS2
- ▶ Ready for operation in **Run 3**
- ▶ Completely redesigned tracking systems
- ▶ Redesigned readout for all subsystems



Summary

- ▶ Finding new sources of CP violation can lead us to New Physics
- ▶ Measurements of CKM elements are becoming increasingly precise

Measurements of γ

- ▶ Will eventually reach $\mathcal{O}(0.4^\circ)$ precision
- ▶ Will have $< 1^\circ$ precision independently in B^+ , B^0 and B_s^0 modes
- ▶ Will allow for penguin free measurement of ϕ_s with ~ 0.02 rad precision
- ▶ Can eventually set limits on / directly probe generic new physics contributions at tree-level
- ▶ Have the potential to be even more sophisticated than this when including additional inputs

Measurements of ϕ_s

- ▶ Will eventually reach $\mathcal{O}(0.003$ rad) precision for $b \rightarrow c\bar{c}s$
- ▶ Will eventually reach $\mathcal{O}(0.01$ rad) precision for penguin modes $b \rightarrow ss\bar{s}$ and $b \rightarrow sd\bar{d}$

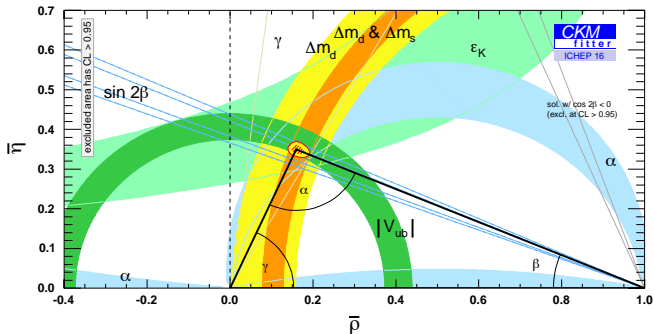
The SM is beautiful, now let's **BREAK IT!**



BACK UP

CKM matrix

$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$



How does CP -violation manifest itself?

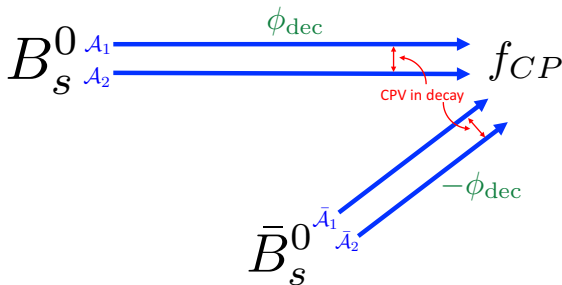
- ▶ Must have **two** interfering amplitudes with **different** strong (δ) and weak (ϕ) phases
- ▶ For a B_s^0 decay to a CP -eigenstate, f , CP -violation effects depend on $\lambda = \frac{q}{p} \frac{\bar{A}_f}{A_f}$

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- ▶ $P(B_s^0 \rightarrow f) \neq P(\bar{B}_s^0 \rightarrow f)$
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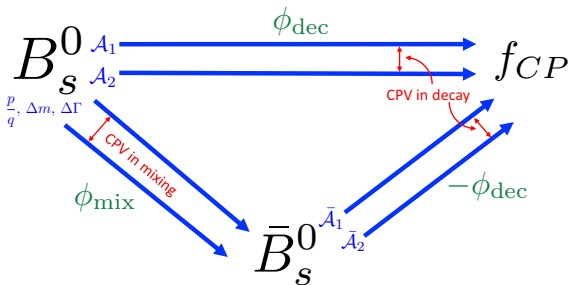
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- ▶ $|q/p| \neq 1$



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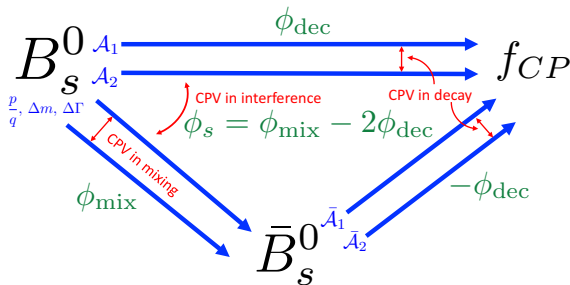
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CPV in the interference between decay and mixing:

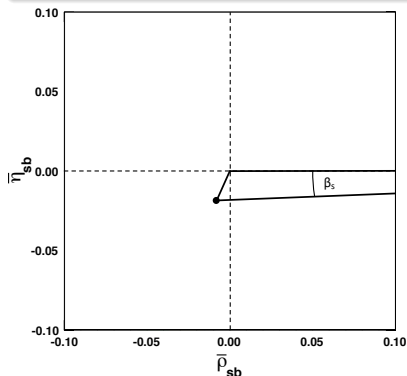
- ▶ $P(B_s^0 \rightarrow f) \neq P(B_s^0 \rightarrow \bar{B}_s^0 \rightarrow f)$
- ▶ $\arg(\lambda) \neq 0$

New Physics effects in the flavour sector

- ▶ Unitarity imposes several conditions ($V^\dagger V = \mathbb{1}$)
 - ▶ Gives rise to “unitarity” triangles
 - ▶ The triangles’ area dictates the **total amount of CPV** in the quark sector

Wolfenstein parametrisation

$$V = \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$



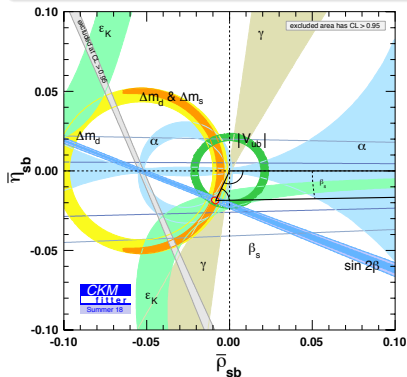
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- ▶ Potential **NP effects are large**

$$\gamma = \arg \left(-\frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*} \right)$$

- ▶ γ is **known very well**
- ▶ Can be determined entirely from tree decays
 - ▶ Unique property among all CP violation parameters
 - ▶ Hadronic parameters can be determined from data
- ▶ Negligible theoretical uncertainty (Zupan and Brod 2013)

Theory uncertainty on γ

$$\delta\gamma/\gamma \approx \mathcal{O}(10^{-7}) - [\text{arXiv:1308.5663}]$$

- ▶ γ can probe for new physics at extremely **high energy scales** (Zupan)
 - ▶ (N)MFV new physics scenarios: $\sim \mathcal{O}(10^2)$ TeV
 - ▶ gen. FV new physics scenarios: $\sim \mathcal{O}(10^3)$ TeV
- ▶ NP contributions to $C_{1,2}$ can cause **sizeable shifts** ($\mathcal{O}(4^\circ)$) in γ (Brod, Lenz et. al 2014) - [arXiv:1412.1446]

- ▶ γ is NOT known very well
- ▶ It is quite challenging to measure
- ▶ The decay rates are small

Branching ratio for suppressed γ mode

$$BR(B^- \rightarrow DK^-, D \rightarrow \pi K) \approx 2 \times 10^{-7}$$

- ▶ Small interference effect typically $\sim 10\%$
- ▶ Fully hadronic decays - hard to trigger on
- ▶ Many channels have a K_S^0 or π^0 in the final state - low efficiency at LHCb
- ▶ Many different decay channels, many observables and many hadronic unknowns make it statistically challenging
- ▶ Inputs for charm parameters are needed

Categorise decays sensitive to γ depending on the $\bar{D}^0 \rightarrow f$ final state

- ▶ GLW (Gronau, London, Wyler) [1991]
 - ▶ CP eigenstates e.g. $D \rightarrow KK$, $D \rightarrow \pi\pi$
- ▶ ADS (Atwood, Dunietz, Soni) [1997,2001]
 - ▶ CF or DCS decays e.g. $D \rightarrow K\pi$
- ▶ GGSZ (Giri, Grossman, Soffer, Zupan) [2003]
 - ▶ 3-body final states e.g. $D \rightarrow K_S^0 \pi\pi$
- ▶ TD (Time-dependent)
 - ▶ Interference between mixing and decay e.g. $B_s^0 \rightarrow D_s^- K^+$ [phase is $(\gamma - 2\beta_s)$]
 - ▶ Penguin free measurement of ϕ_s ?
- ▶ Dalitz
 - ▶ Look at 3-body B decays with D^0 or \bar{D}^0 in the final state, e.g. $B^0 \rightarrow D^0 K^+ \pi^-$

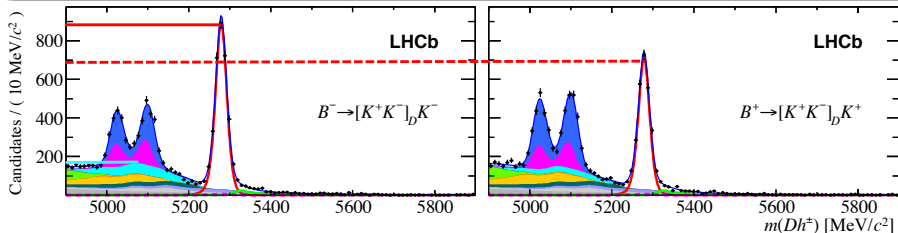
GLW Method

- ▶ CP eigenstates e.g. $D \rightarrow KK$, $D \rightarrow K_S^0 \pi^0$ ▶ [Phys. Lett. B253 (1991) 483]
- ▶ Gronau, London, Wyler (1991) ▶ [Phys. Lett. B265 (1991) 172]

GLW observables

$$A_{CP} = \frac{\Gamma(B^- \rightarrow D_{CP}^0 K^-) - \Gamma(B^+ \rightarrow D_{CP}^0 K^+)}{\Gamma(B^- \rightarrow D_{CP}^0 K^-) + \Gamma(B^+ \rightarrow D_{CP}^0 K^+)} = \frac{\pm 2r_B \sin(\delta_B) \sin(\gamma)}{1 + r_B^2 \pm 2r_B \cos(\delta_B) \cos(\gamma)} \quad (1)$$

$$R_{CP} = \frac{\Gamma(B^- \rightarrow D_{CP}^0 K^-) + \Gamma(B^+ \rightarrow D_{CP}^0 K^+)}{\Gamma(B^- \rightarrow D^0 K^-) + \Gamma(B^+ \rightarrow D^0 K^+)} = 1 + r_B^2 \pm 2r_B \cos(\delta_B) \cos(\gamma) \quad (2)$$



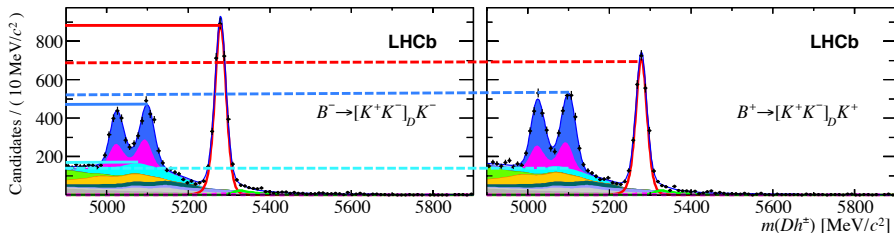
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- ▶ LHCb has recently extracted GLW observables from partially reconstructed $B^- \rightarrow D^{*0} K^-$ in the same fit - [Phys. Lett. B777 (2018) 16]

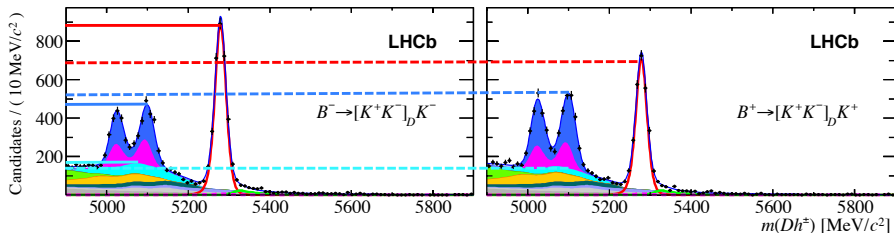
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- ▶ LHCb has recently extracted GLW observables from partially reconstructed $B^- \rightarrow D^{*0} K^-$ in the same fit - [Phys. Lett. B777 (2018) 16]
- ▶ Can extend to quasi-CP-eigenstates ($D^0 \rightarrow KK\pi^0$) if fraction of CP content, F^+ , is known

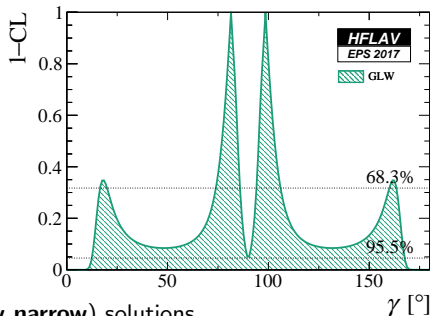
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- ▶ Multiple (**but very narrow**) solutions
- ▶ Require knowledge of F^+ from charm friends

ADS Method

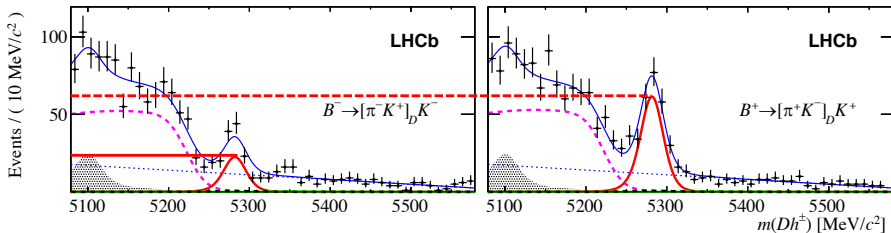
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- ▶ [Phys. Rev. D63 (2001) 036005]
- ▶ [Phys. Rev. Lett. 78 (1997) 3257]

ADS observables

$$A_{ADS} = \frac{\Gamma(B^- \rightarrow [K^+\pi^-]_D K^-) - \Gamma(B^+ \rightarrow [K^-\pi^+]_D K^+)}{\Gamma(B^- \rightarrow [K^+\pi^-]_D K^-) + \Gamma(B^+ \rightarrow [K^-\pi^+]_D K^+)} = \frac{2r_B r_D \sin(\delta_B + \delta_D) \sin(\gamma)}{r_B^2 + r_D^2 + 2r_B r_D \cos(\delta_B + \delta_D) \cos(\gamma)} \quad (3)$$

$$R_{ADS} = \frac{\Gamma(B^- \rightarrow [K^+\pi^-]_D K^-) + \Gamma(B^+ \rightarrow [K^-\pi^+]_D K^+)}{\Gamma(B^- \rightarrow [K^-\pi^+]_D K^-) + \Gamma(B^+ \rightarrow [K^+\pi^-]_D K^+)} = r_B^2 + r_D^2 + 2r_B r_D \cos(\delta_B + \delta_D) \cos(\gamma) \quad (4)$$



ADS Method

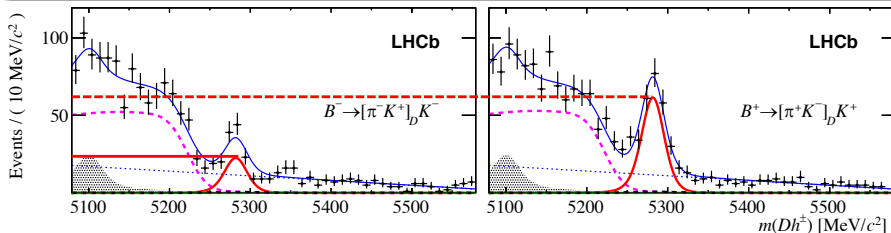
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ADS observables

$$A_{ADS} = \frac{\Gamma(B^- \rightarrow [K^+\pi^-]_D K^-) - \Gamma(B^+ \rightarrow [K^-\pi^+]_D K^+)}{\Gamma(B^- \rightarrow [K^+\pi^-]_D K^-) + \Gamma(B^+ \rightarrow [K^-\pi^+]_D K^+)} = \frac{2r_B r_D \sin(\delta_B + \delta_D) \sin(\gamma)}{r_B^2 + r_D^2 + 2r_B r_D \cos(\delta_B + \delta_D) \cos(\gamma)} \quad (3)$$

$$R_{ADS} = \frac{\Gamma(B^- \rightarrow [K^+\pi^-]_D K^-) + \Gamma(B^+ \rightarrow [K^-\pi^+]_D K^+)}{\Gamma(B^- \rightarrow [K^-\pi^+]_D K^-) + \Gamma(B^+ \rightarrow [K^+\pi^-]_D K^+)} = r_B^2 + r_D^2 + 2r_B r_D \cos(\delta_B + \delta_D) \cos(\gamma) \quad (4)$$



- ▶ Much harder to extract partially reconstructed observables because of $B_s^0 \rightarrow D^{(*)0} K^+ \pi^-$ backgrounds.

ADS Method

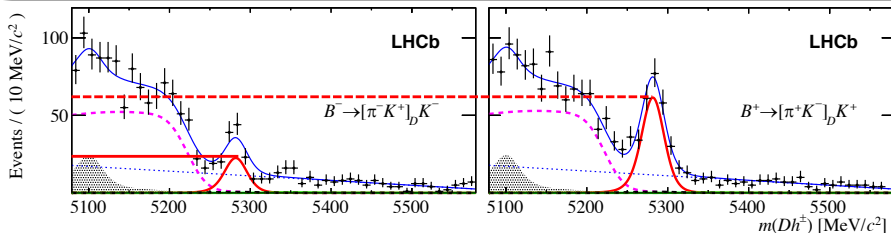
- ▶ CF or DCS decays e.g. $D \rightarrow K\pi$
- ▶ Atwood, Dunietz, Soni (1997,2001)

- ▶ [Phys. Rev. D63 (2001) 036005]
- ▶ [Phys. Rev. Lett. 78 (1997) 3257]

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- ▶ **Much harder to extract partially reconstructed observables because of $B_s^0 \rightarrow D^{(*)0} K^+ \pi^-$ backgrounds.**
- ▶ Can extend to multibody-DCS-decays ($D^0 \rightarrow K\pi\pi^0$) if dilution from interference, κ_D , is known

ADS Method

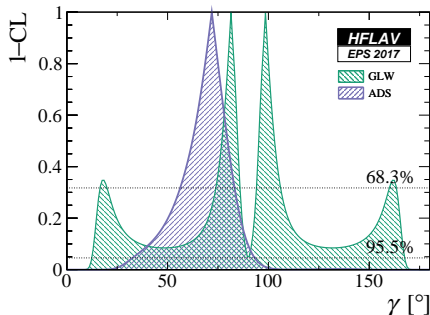
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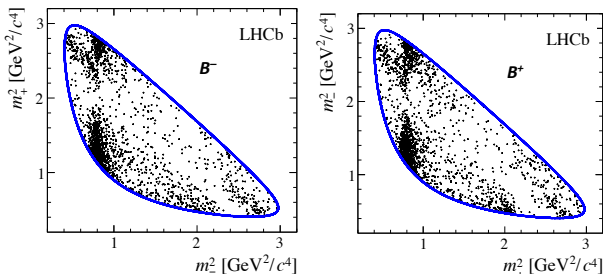
- ▶ A single (**yet broader**) solution
- ▶ Require knowledge of r_D , δ_D , κ_D from charm friends

GGSZ Method

- ▶ 3-body final states e.g. $D \rightarrow K_S^0 \pi \pi$
- ▶ Giri, Grossman, Soffer, Zupan (2003)
- ▶ [Phys. Rev. D68 (2003) 054018]

GGSZ observables (partial rate as function of Dalitz position)

$$d\Gamma_{B^\pm}(\mathbf{x}) = A_{(\pm, \mp)}^2 + r_B^2 A_{(\mp, \pm)}^2 + 2A_{(\pm, \mp)} A_{(\mp, \pm)} \left[\underbrace{r_B \cos(\delta_B \pm \gamma)}_{x_\pm} \underbrace{\cos(\delta_D(\pm, \mp))}_{c_j} + \underbrace{r_B \sin(\delta_B \pm \gamma)}_{y_\pm} \underbrace{\sin(\delta_D(\pm, \mp))}_{s_j} \right] \quad (5)$$



- ▶ Essentially a GLW/ADS type analysis across the D decay phase space
- ▶ Excellent sensitivity from interference between various contributions

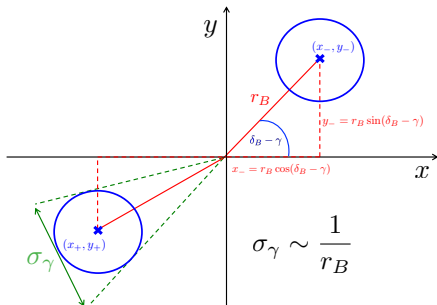
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$$\sigma_\gamma \sim \frac{1}{r_B}$$

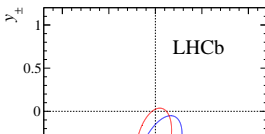
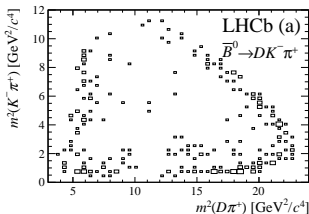
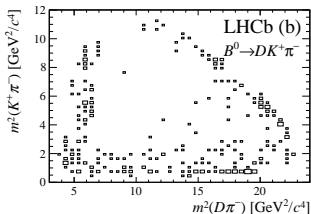
- ▶ $x_\pm + iy_\pm = r_B e^{i(\delta_B \pm \gamma)}$
- ▶ **Uncertainty on γ is inversely proportional to central value of hadronic unknown!!**
- ▶ Fluctuation in nuisance parameter = fluctuation in error on parameter of interest!

Dalitz (GW) Method

- ▶ Use Dalitz structure of **B** decays
- ▶ $B^0 \rightarrow D^0 K^+ \pi^-$
- ▶ Get multiple interfering resonances which increase sensitivity to γ
 - ▶ $D_0^*(2400)^-, D_2^*(2460)^-, K^*(892)^0, K^*(1410)^0, K_2^*(1430)^0$
- ▶ Fit B decay Dalitz Plot for cartesian parameters (similar to GGSZ except for the B not the D)
 - ▶ $D \rightarrow K^+ K^-, D \rightarrow \pi^+ \pi^-$ - GLW-Dalitz (done by LHCb - [arXiv:1602.03455])
 - ▶ $D \rightarrow K^\pm \pi^\mp$ - ADS-Dalitz (difficult due to backgrounds from $B_s^0 \rightarrow D^{(*)0} K^+ \pi^-$)
 - ▶ $D \rightarrow K_S^0 \pi^+ \pi^-$ - GGSZ-Dalitz (double Dalitz!)

▶ Gershon, Williams (2009)

▶ [Phys. Rev. D80 (2009) 092002]

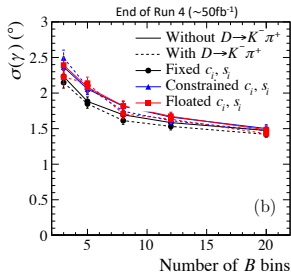
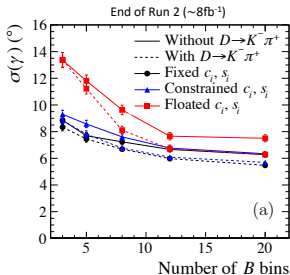


Dalitz (GW) Method

- ▶ Some studies of future prospects of the B Dalitz method with GGSZ modes in [\[arXiv:1712.07853\]](#)
- ▶ Can include GLW, ADS and GGSZ modes in single framework to improve constraints on B Dalitz bins, κ_j and σ_j
- ▶ The double Dalitz method has **sufficient information** (large number of bins) to extract c_i and s_i

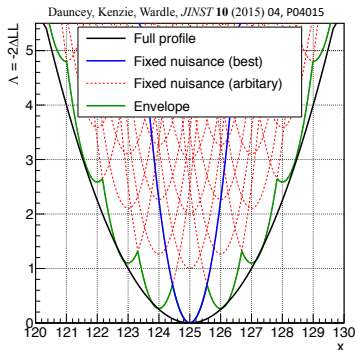
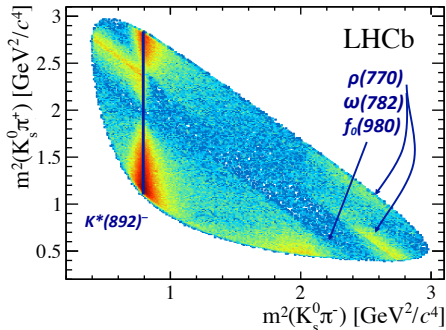
Double Dalitz observables (partial rate as function of both Dalitz positions)

$$|A|^2 = |A_B|^2 |A_D|^2 + |\bar{A}_B|^2 |\bar{A}_D|^2 + 2|A_B| |A_D| |\bar{A}_B| |\bar{A}_D| [(\kappa c - \sigma s) \cos(\gamma) - (\kappa s + \sigma c) \sin(\gamma)]$$



Amplitude measurements of γ

- ▶ Most sensitive method to measure γ is a full kinematic analysis
- ▶ Take advantage of the rich structure in the kinematic plane
- ▶ Make use of “discrete profiling method” I developed at Imperial College
- ▶ Build upon expertise in amplitude models at Cambridge



- ▶ Exploit several decay modes
 - ▶ $B^- \rightarrow D^0 K^-$, $B^- \rightarrow D^0 K^{*-}$, $B^- \rightarrow D^{*0} K^-$, $B^0 \rightarrow D^0 K^{*0}$

Status of γ at LHCb

Method		B Decay D Decay		Highest Statistics	Poorer sensitivity		High potential (Dalitz structure of B)		Low stats (multibody B)	
				$B^- \rightarrow D^0 K^-$	$B^- \rightarrow D^0 K^{*-}$ [$K^{*-} \rightarrow K_s^0 \pi^-$]	$B^- \rightarrow D^{*0} K^-$ [$D^{*0} \rightarrow D^0 \pi^0$], [$D^{*0} \rightarrow D^0 \gamma$]		$B^0 \rightarrow D^0 K^+ \pi^-$		$B^- \rightarrow D^0 K^+ \pi^-$
						part-rec	full-rec	K^{*0} res	Dalitz	
GLW	(+)	$D^0 \rightarrow K^+ K^-$	5 fb ⁻¹	5 fb ⁻¹	5 fb ⁻¹	•	3 fb ⁻¹ (•)	3 fb ⁻¹	3 fb ⁻¹	
		$D^0 \rightarrow \pi^+ \pi^-$	5 fb ⁻¹	5 fb ⁻¹	5 fb ⁻¹	•	3 fb ⁻¹ (•)	3 fb ⁻¹	3 fb ⁻¹	
		$D^0 \rightarrow K^+ K^- \pi^0$	3 fb ⁻¹ (•)	-	-	-	-	-	-	
		$D^0 \rightarrow \pi^+ \pi^- \pi^0$	3 fb ⁻¹	-	-	-	-	-	-	
		$D^0 \rightarrow K^+ K^- \pi^+ \pi^-$	•	-	-	-	-	-	-	
		$D^0 \rightarrow \pi^+ \pi^- \pi^+ \pi^-$	3 fb ⁻¹ (•)	5 fb ⁻¹	•	•	•	-	-	
	(-)	$D^0 \rightarrow K_s^0 \pi^0$	•	-	-	-	-	-	-	
ADS		$D^0 \rightarrow K^+ \pi^-$	3 fb ⁻¹ (•)	5 fb ⁻¹	•	•	3 fb ⁻¹ (•)	•	3 fb ⁻¹	
		$D^0 \rightarrow K^+ \pi^- \pi^0$	3 fb ⁻¹	-	-	-	-	-	-	
		$D^0 \rightarrow K^+ \pi^- \pi^+ \pi^-$	3 fb ⁻¹ (•)	5 fb ⁻¹	•	•	•	-	-	
GGSZ		$D^0 \rightarrow K_s^0 \pi^+ \pi^-$	5 fb ⁻¹	•	-	•	3 fb ⁻¹ (•)	•	•	
		$D^0 \rightarrow K_s^0 K^+ K^-$	5 fb ⁻¹	•	-	•	3 fb ⁻¹ (•)	•	•	
		$D^0 \rightarrow K_s^0 \pi^+ \pi^- \pi^0$	•	-	-	-	-	-	-	
		$D^0 \rightarrow K_s^0 K^+ K^- \pi^0$	•	-	-	-	-	-	-	

KEY: •: (update) in progress

•: requires input from Charm sector (r_D, δ_D, κ_D)

NOTE: TD result with $B_s^0 \rightarrow D_s^- K^+ 3 \text{ fb}^{-1}$ (•)

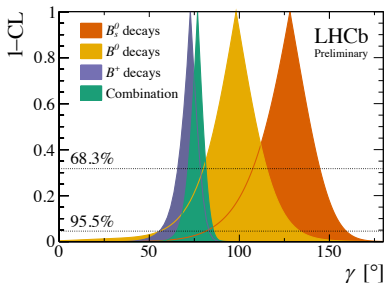
TD result with $B^0 \rightarrow D^- \pi^+ 3 \text{ fb}^{-1}$

GLS result from $B^- \rightarrow D^0 K^-$ with $D^0 \rightarrow K_s^0 K^\pm \pi^\mp 3 \text{ fb}^{-1}$ (•)

Working on $B^- \rightarrow D^0 K^{*-}$ with $K^{*-} \rightarrow K^- \pi^0$ •

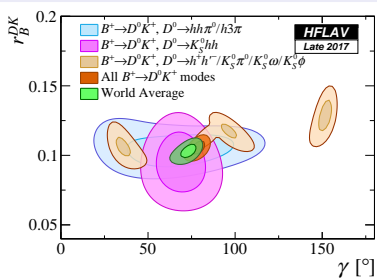
LHCb Average

$$\gamma = (76.8^{+5.1}_{-5.7})^\circ$$



World Average (HFLAV)

$$\gamma = (73.5^{+4.3}_{-5.0})^\circ$$



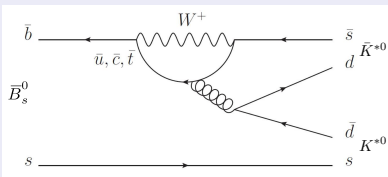
Indirect constraints are: $\gamma = (65.3^{+1/0}_{-2.5})^\circ (\sim 2\sigma)$

Comparison between B_s^0 and B^+ initial states $\sim 2\sigma$

$B_s^0 \rightarrow (K^+\pi^-)(K^-\pi^+)$ decays

- ▶ **Pure penguin decay** - $b \rightarrow sd\bar{d}$ transition
- ▶ New Physics can be significantly enhanced and entirely different from $B_s^0 \rightarrow J/\psi\phi$ and $B_s^0 \rightarrow \phi\phi$
- ▶ Expect similar statistical precision to $B_s^0 \rightarrow \phi\phi$
- ▶ CPV in decay is also possible

$$B_s^0 \rightarrow K^{*0} \bar{K}^{*0}$$



$$\phi_s^{d\bar{d}} = ?$$

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Experimentally challenging:

- ▶ Low branching fraction (100 times smaller than $B_s^0 \rightarrow J/\psi\phi$)
- ▶ Purely hadronic final state
- ▶ K^* is fairly wide (several resonant and non-resonant components)
- ▶ Several peaking backgrounds

$$\phi_s^{c\bar{c}} \neq \phi_s^{s\bar{s}} \neq \phi_s^{d\bar{d}}$$

Ingredients required for a ϕ_s analysis

- ▶ In the **simplest case**, and **only** if there is no CP -violation in decay, the time-dependent CP -asymmetry

$$A_{CP}(t) = \frac{\Gamma(\bar{B}_s^0 \rightarrow f) - \Gamma(B_s^0 \rightarrow f)}{\Gamma(\bar{B}_s^0 \rightarrow f) + \Gamma(B_s^0 \rightarrow f)} = \eta_f \sin(\phi_s) \sin(\Delta m_s t)$$

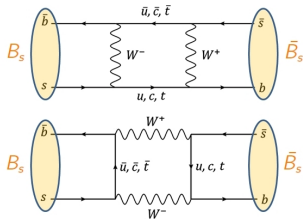
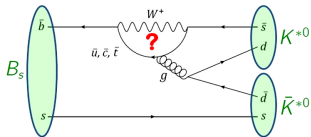
- ▶ Experimentally

$$A_{CP}(t) \approx (1 - 2w) e^{-\frac{1}{2} \Delta m_s^2 \sigma_t^2} \eta_f \sin(\phi_s) \sin(\Delta m_s t)$$

- ▶ w : Probability the initial B flavour was tagged incorrectly
- ▶ σ_t : Decay-time resolution
- ▶ η_f : CP -eigenvalue \implies angular analysis
- ▶ **Important requirements**
 - ▶ Good decay time resolution
 - ▶ Good flavour tagging
 - ▶ Sufficient statistics for an angular analysis
 - ▶ Good particle identification

The $B_s^0 \rightarrow K^{*0} \bar{K}^{*0}$ decay

- ▶ **Interference between $B_s^0 \rightarrow K^{*0} \bar{K}^{*0}$ and $B_s^0 \rightarrow \bar{B}_s^0 \rightarrow K^{*0} \bar{K}^{*0}$**
 - ▶ where $K^{*0} \rightarrow K^+ \pi^-$ and $\bar{K}^{*0} \rightarrow K^- \pi^+$
- ▶ **Gives access to CP-violating phase $\phi_s^{d\bar{d}}$**
- ▶ First discovered by LHCb in [Phys. Lett. **B709** (2012) 50]
 - ▶ Update in [JHEP **07** (2015) 166]
- ▶ Discussed extensively in the literature as a promising mode for New Physics
 - ▶ Fleisher et. al. [Phys. Lett. **B660** (2008) 212]
 - ▶ Ciuchini et. al. [Phys. Rev. Lett. **100** (2008) 031802]
 - ▶ Descotes-Genon et. al. [Phys. Rev. **D85** (2012) 034010]
 - ▶ Bhattacharya et. al. [Phys. Lett. **B717** (2012) 403]



SM expectation:

$$\lambda = \frac{p \bar{\mathcal{A}}_f}{q \mathcal{A}_f} \approx 1$$

$$\phi_s^{d\bar{d}} = \phi_{\text{mix}} - 2\phi_{\text{decay}} \approx 0$$

Current key responsibilities in LHCb

Physics working group convenor (Jan 2017 - Jan 2019)

- ▶ Nominated “ B to open charm” (γ analysis) WG convenor in November 2016
- ▶ **One of the eight top level physics analysis groups in LHCb**
- ▶ Member of the Physics Planning Group → liase between WG and management
- ▶ Manage ~ 80 physicists studying CP -violation (including all γ analyses) in B decays

Statistics expert

- ▶ Develop and manage the “GammaCombo” statistical package [[gammacombio.github.io](https://github.com/gammacombio/gammacombio)]
- ▶ Advise and liase with several analysis groups

Trigger expert on call

- ▶ Developed lifetime unbiased triggering in LHCb